

*Tell us what the future holds, so we may know that you are gods... (Isaiah 41:23)*

Everyday mathematics and data combine to help us envision what might be

# Forecasting the required tank container and trucking capacity for an intermodal logistics service provider

27/08/2019

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Introduction  
and problem  
description



Proposed  
forecasting  
methodology



Completing the  
circle: benefits &  
implementation



Discussion



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circle: benefits &  
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Discussion

# H&S Foodtrans is a logistics service provider engaged in intermodal transportation of liquid foodstuff

*Introduction to H&S*



# Forecasting the required tank container and trucking capacity

*Problem statement*



*Problem statement:*

“How can forecasting be used to predict the short-term required **trucking and tank container** capacity for an intermodal logistics service provider?”

# To provide an answer to the problem statement, 3 main steps were taken in this research

Research steps



## Problem statement

“How can forecasting be used to predict the short-term required **trucking and tank container** capacity for an intermodal logistics service provider?”



## Research steps

### Step 1

Forecasting the loadings and deliveries based on *historical data*

### Step 2

Adjusting the forecast of step 1 by utilizing *advance demand information*

### Step 3

Translate the adjusted forecast of step 2 into:

- A prediction for the required trucking capacity
- A prediction for the required tank container capacity



Introduction  
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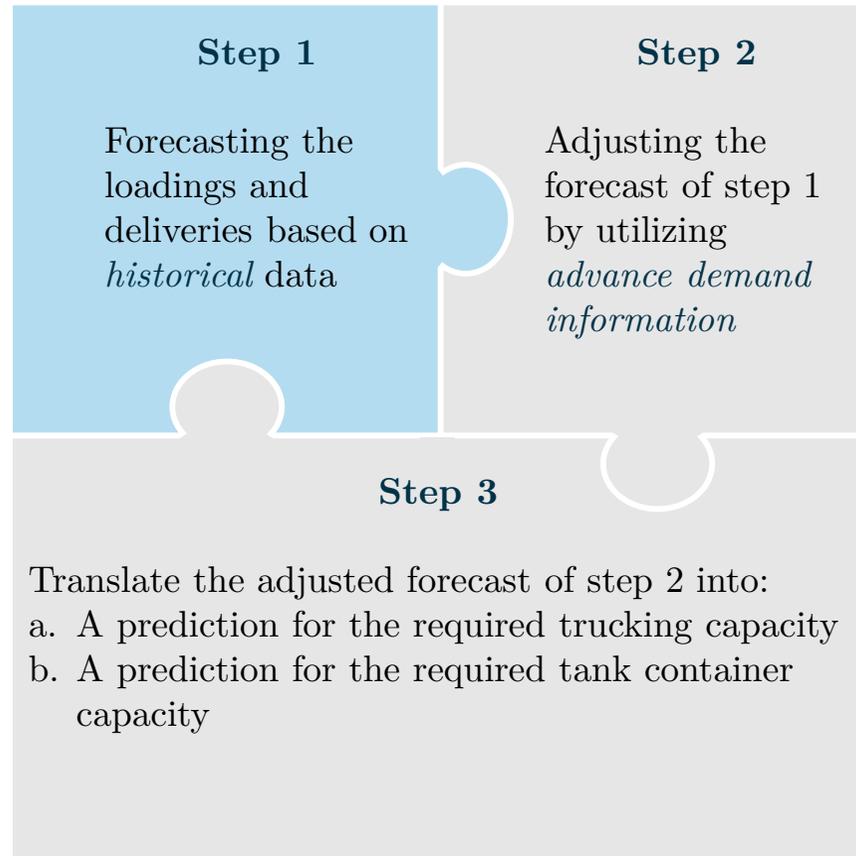
Completing the  
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Discussion

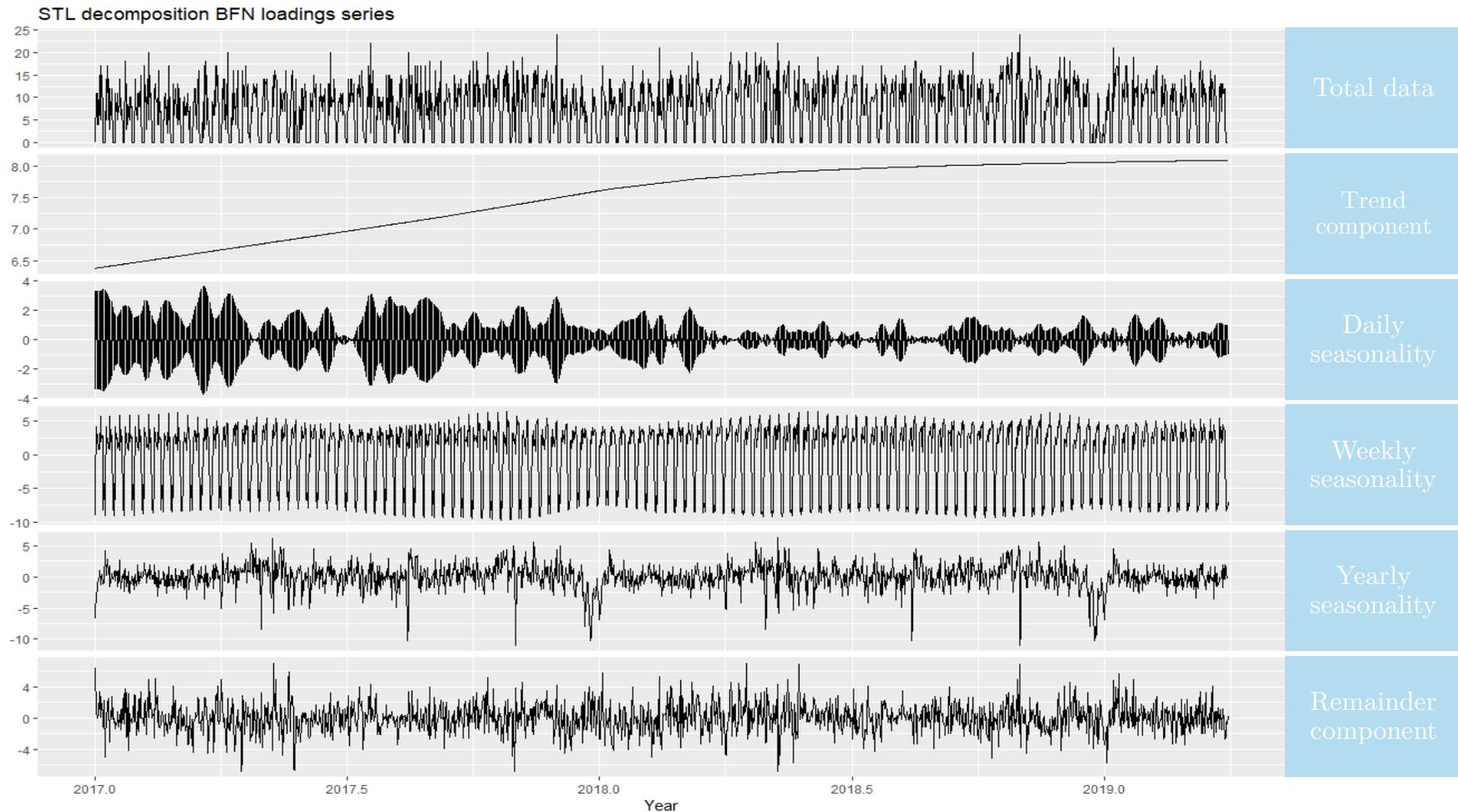
# Step 1: How can the number of loadings and deliveries be forecasted from historical data?

Step 1



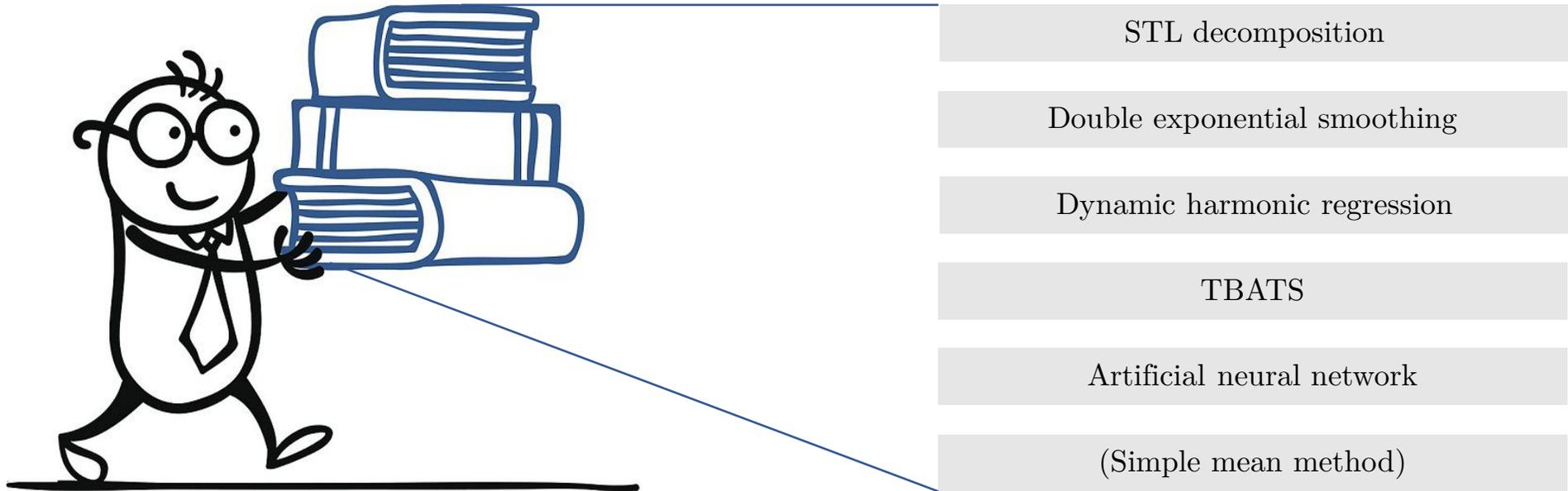
# The data exhibits multiple seasonal patterns

*STL decomposition BFN loadings series*



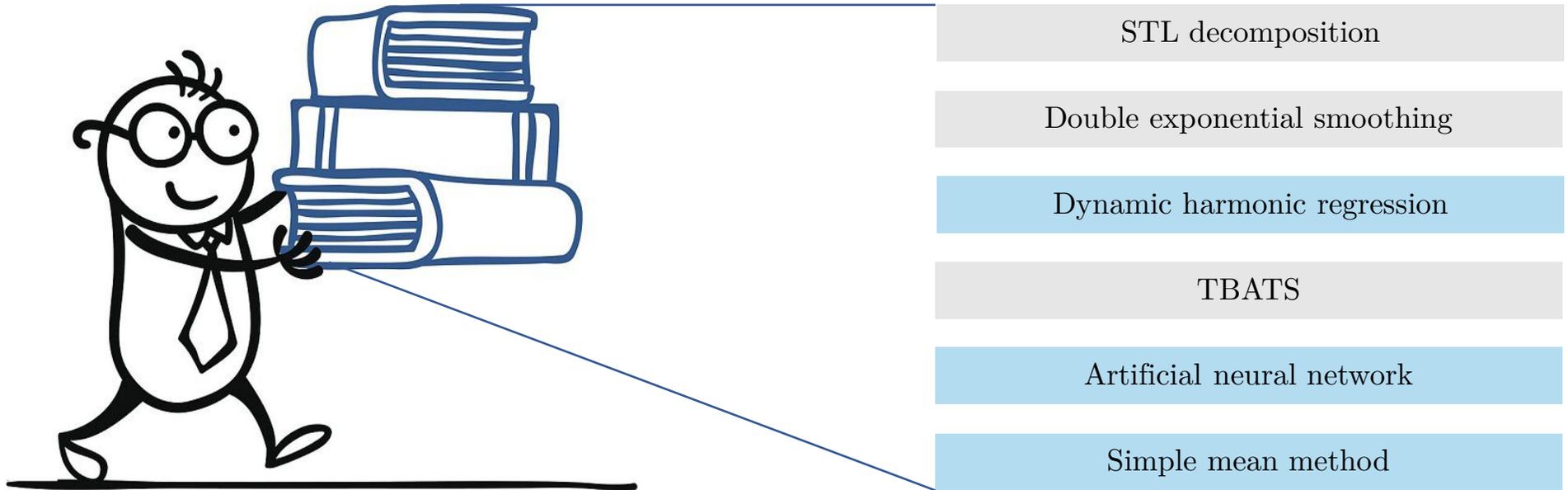
# The literature was consulted to identify forecasting models that can account for time series with multiple (seasonal) components

*Literature review*



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*Literature review*



# Artificial neural networks, Dynamic harmonic regression and the Simple mean method turned out to be the most accurate models in step 1

*Best performing models for predicting orders from historical data*



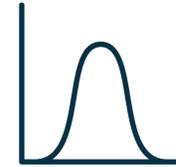
## Artificial Neural Networks

-  Best performing model in most series
-  More difficult to implement for practitioners
-  Lack of explanatory capabilities



## Dynamic Harmonic Regression

-  Fairly accurate in most series
-  Explanatory capabilities (interpretation coefficients)
-  More difficult to implement for practitioners

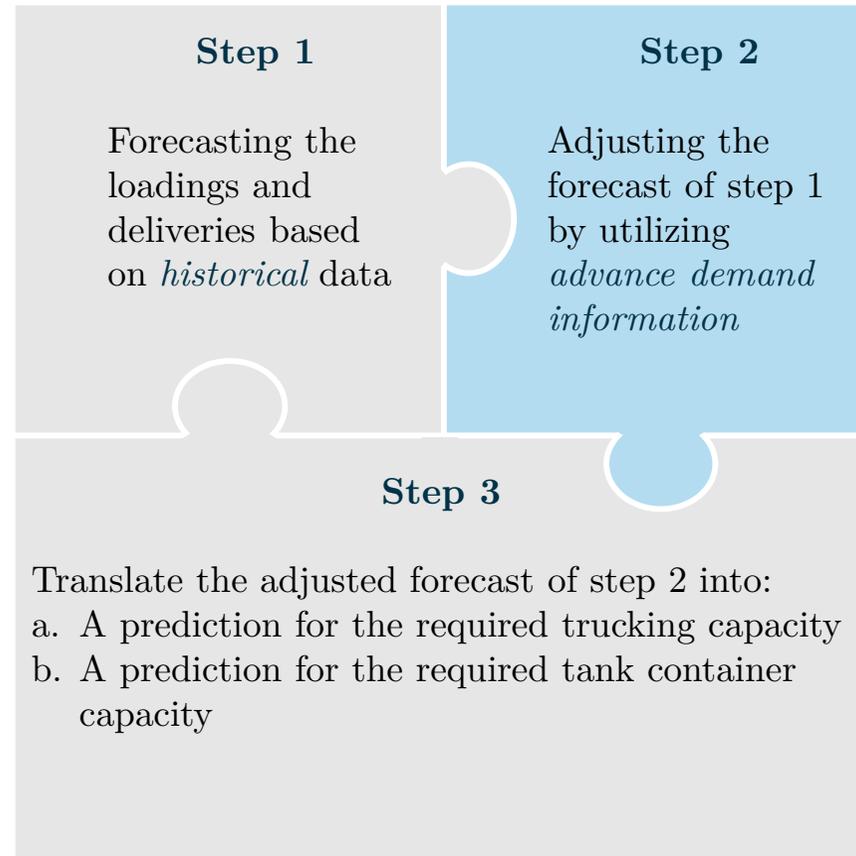


## Simple Mean Method

-  Fairly accurate in most series
-  Easy to understand for practitioners
-  Easy to implement for all planning regions
-  Intuitively captures strongest seasonal components

## Step 2: How can advance demand information be utilized to enhance the initial forecast of the loadings and deliveries?

*Step 2*



# Using the Advance Demand Information

## *Method 1: Bayesian Adjustment*

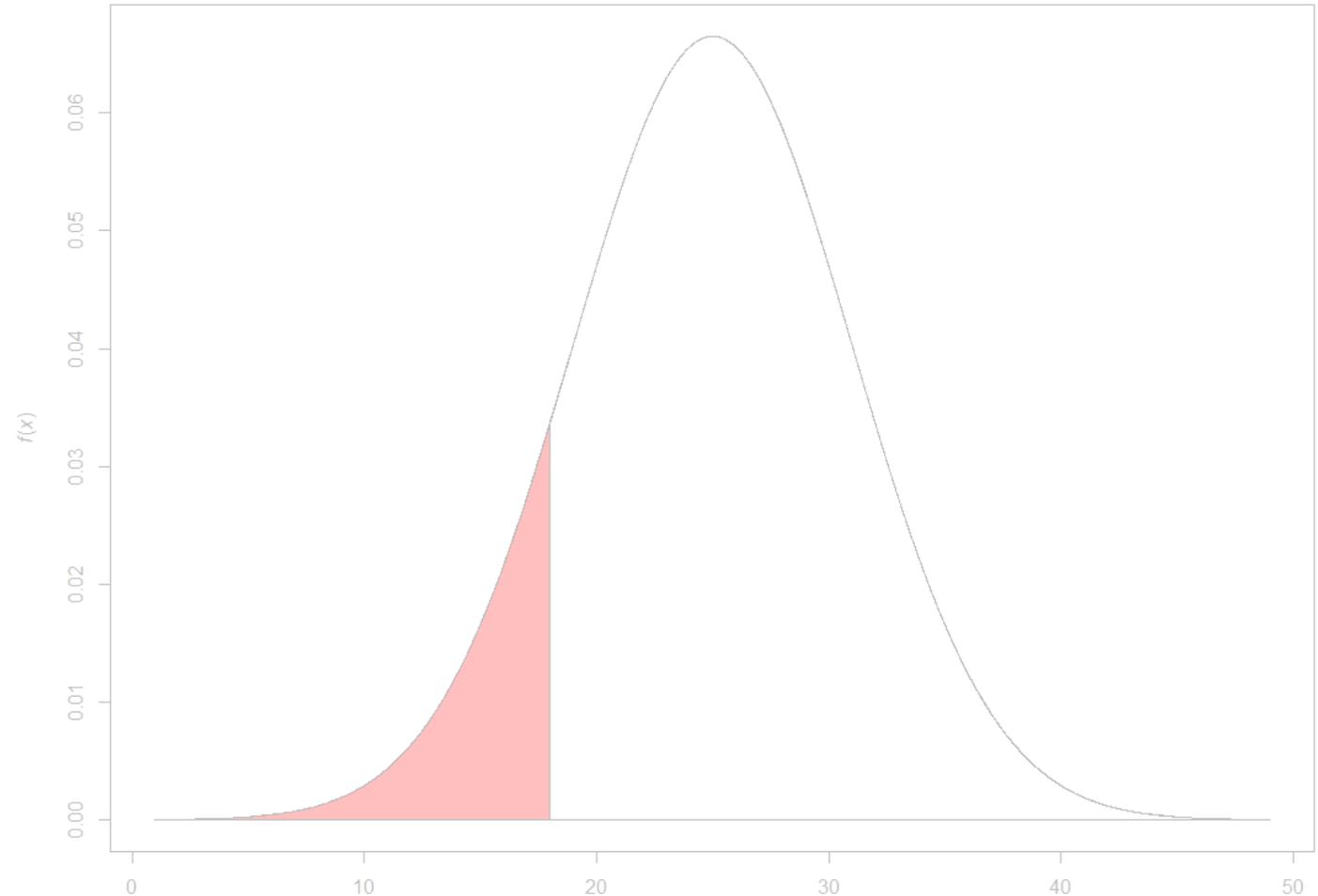


# Intuitive explanation of the idea behind the Bayesian adjustment

*Bayesian technique explained*

Consider the following situation:

- Today (27/08) we want to forecast the loadings in region  $x$  for Friday (30/08)
- The initial forecast equals **25** loadings
- At present, **18** loadings are already in the system for Friday (30/08)

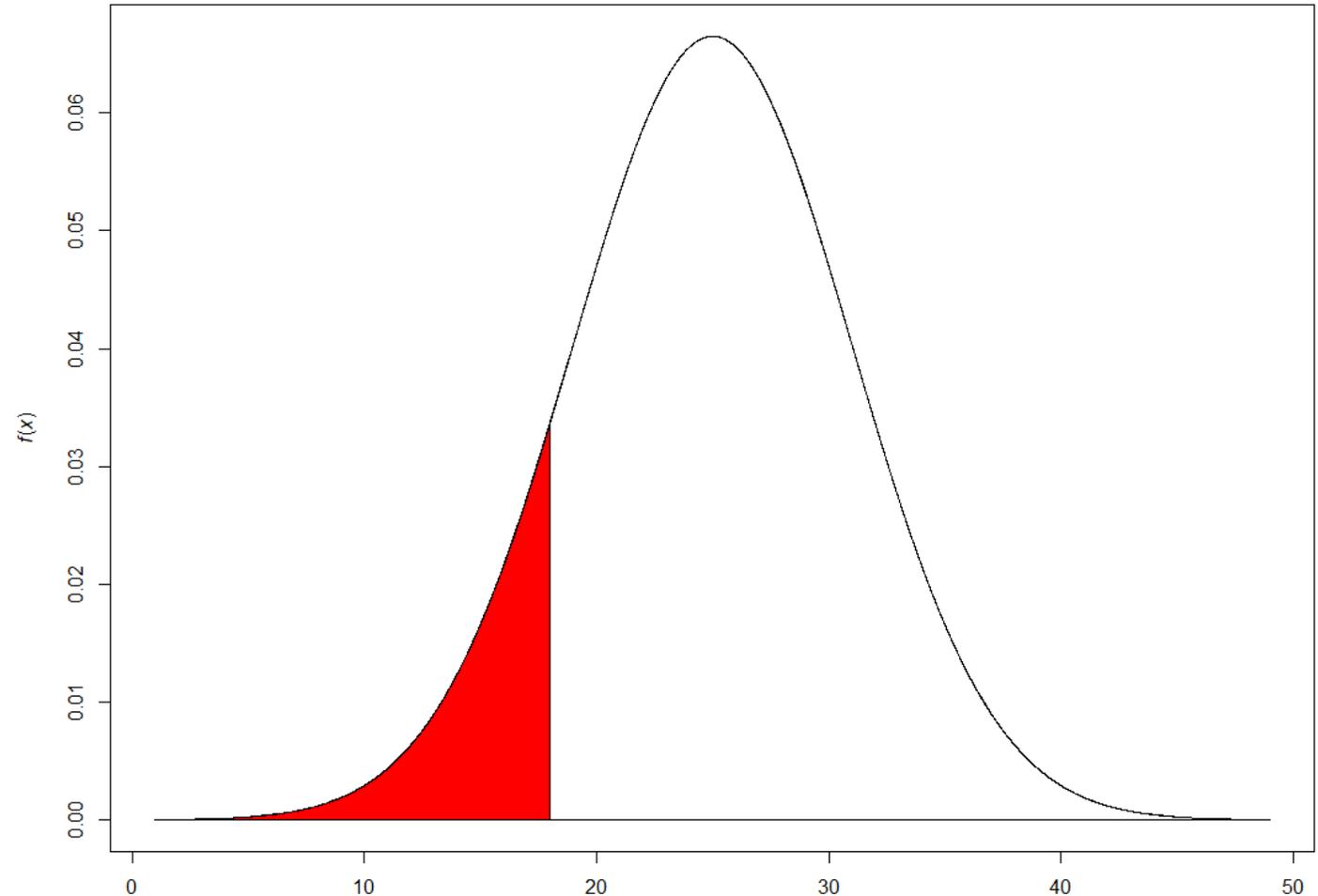


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# First, the probability distribution for the number of orders (i.e. loadings or deliveries) is estimated

1

*Estimate the probability distribution for the number of orders ( $n$ ) and their corresponding probabilities.*

Fit a distribution with mean equal to the initial forecast.

- If the initial forecast is smaller than 10: **Poisson distribution**
- If the initial forecast is greater or equal to 10: **Normal distribution**

# Subsequently, the probability that an order for a future time period is already known at present is approximated

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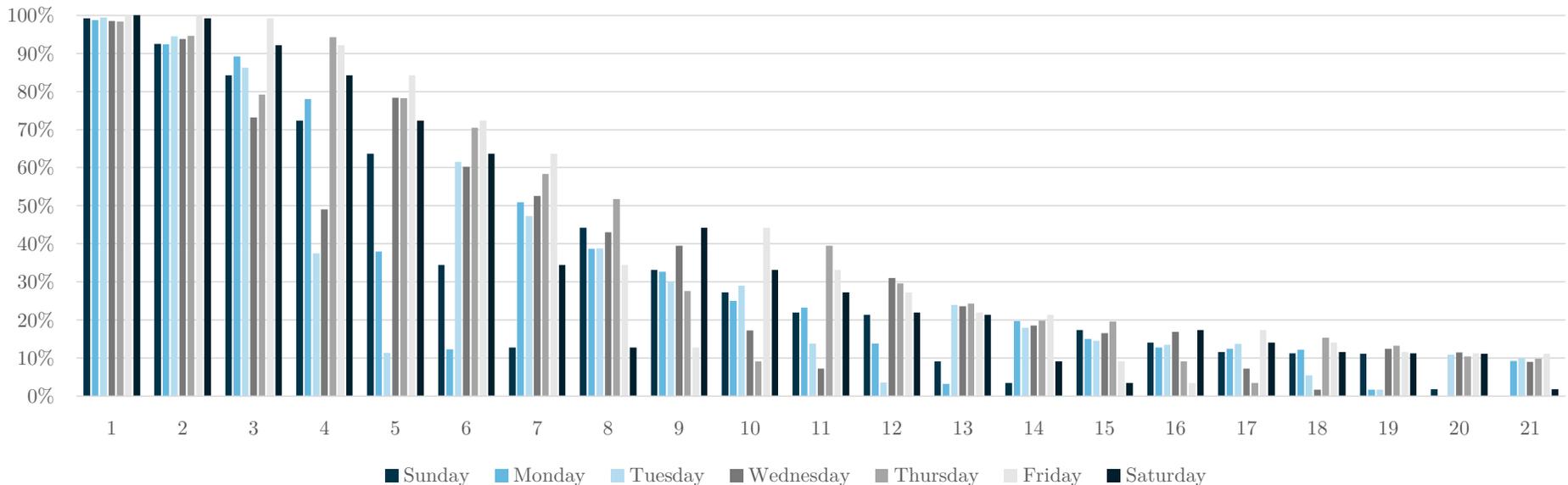
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2

*Estimate the probability that an order for future period  $\tau$  is already known as of time  $T$*

- This probability is denoted by  $\Theta$
- Computed separately for each day of the week



## Third, the conditional probability of the advanced number of orders is calculated using the binomial distribution

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*Estimate the conditional probability of the advanced number of orders, for each possible value that the number of orders for period  $\tau$  can take*

$$P\langle n_{a\tau} | n_j \rangle = \binom{n_j}{n_{a\tau}} \theta_\tau^{n_{a\tau}} (1 - \theta_\tau)^{n_j - n_{a\tau}}$$

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# Fourth, Bayes' Theorem is used to derive the probability of the number of orders, given the advanced number of orders

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4

*Estimate the probability of the number of orders, given the advanced number of orders*

$$P\langle n_j | n_{a\tau} \rangle = \frac{P\langle n_{a\tau} | n_j \rangle * P\langle n_j \rangle}{P\langle n_{a\tau} \rangle} \quad \text{where, } P\langle n_{a\tau} \rangle = \sum_j P\langle n_{a\tau} | n_j \rangle * P\langle n_j \rangle$$

# Finally, the expected value of the rescaled distribution is calculated to derive the adjusted forecast

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<p>2 <i>Estimate the probability that an order for future period <math>\tau</math> is already known as of time <math>T</math></i></p>	<ul style="list-style-type: none"> <li>• This probability is denoted by <math>\Theta</math></li> <li>• Computed separately for each day of the week</li> </ul>
<p>3 <i>Estimate the conditional probability of the advanced number of orders, for each possible value that the number of orders for period <math>\tau</math> can take</i></p>	$P\langle n_{a\tau}   n_j \rangle = \binom{n_j}{n_{a\tau}} \theta_\tau^{n_{a\tau}} (1 - \theta_\tau)^{n_j - n_{a\tau}}$
<p>4 <i>Estimate the probability of the number of orders, given the advanced number of orders</i></p>	$P\langle n_j   n_{a\tau} \rangle = \frac{P\langle n_{a\tau}   n_j \rangle * P\langle n_j \rangle}{P\langle n_{a\tau} \rangle} \quad \text{where, } P\langle n_{a\tau} \rangle = \sum_j P\langle n_{a\tau}   n_j \rangle * P\langle n_j \rangle$
<p>5 <i>Estimate the expected number of orders for future period <math>\tau</math></i></p>	$E\langle n   n_{a\tau} \rangle = \sum_j n_j P\langle n_j   n_{a\tau} \rangle$

# Summary of the Bayesian adjustment

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*Estimate the probability distribution for the number of orders ( $n$ ) and their corresponding probabilities.*

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*Estimate the probability of the number of orders, given the advanced number of orders*

$$P\langle n_j | n_{a\tau} \rangle = \frac{P\langle n_{a\tau} | n_j \rangle * P\langle n_j \rangle}{P\langle n_{a\tau} \rangle} \quad \text{where, } P\langle n_{a\tau} \rangle = \sum_j P\langle n_{a\tau} | n_j \rangle * P\langle n_j \rangle$$

5

*Estimate the expected number of orders for future period  $\tau$*

$$E\langle n | n_{a\tau} \rangle = \sum_j n_j P\langle n_j | n_{a\tau} \rangle$$

# The Bayesian technique significantly improves the initial forecast

*Performance Bayesian technique*



## Type of forecast

**sub-daily** (AM / PM) number of loadings and deliveries forecast for **1 week ahead**

**daily** number of loadings and deliveries forecast for **3 weeks ahead**

## Improvement after Bayesian technique

Initial forecast was improved by **64%**

Initial forecast was improved by **27%**

# Recall that the output of the Bayesian algorithm is a forecast of the expected number of loadings and deliveries

Recap step 1 and 2

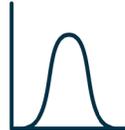
## Historical data forecast



Artificial Neural Network



Dynamic Harmonic Regression



Simple Mean Method



## Bayesian algorithm

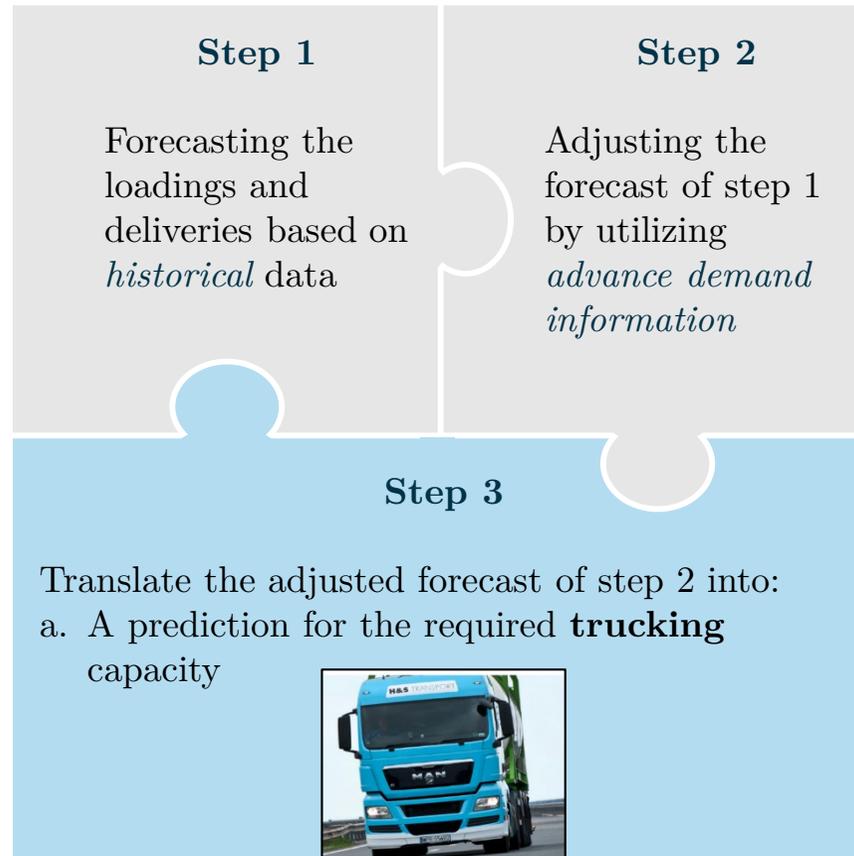


## Output

The forecasted number of **loadings** and **deliveries** in a certain region in a given period

# Step 3a: How can the forecasted loadings and deliveries be used to predict the required trucking capacity?

Step 3a



# The historical trucking capacity is estimated based on actuals and a number of theoretical assumptions

Estimation of historical trucking capacity

		Assumptions	Actuals
1	Estimation of the historical trucking capacity	• Pickup: 45 min	• Loading action
		• Drop: 45 min	• Delivery action
		• Clean: 60 min	• Location and sequence of actions
		• Speed truck: 60 km/h	

$$\delta_T(\tau) = \beta_0 + \beta_1 * Lo(\tau) + \beta_2 * De(\tau) + \beta_3 * Lo_{D(\tau)} + \beta_4 * De_{D(\tau)} + \beta_5 * \delta(\tau - 14) + \beta_6 * \delta(\tau - 28) + \sum_{k=1}^8 \beta_{6+k} x_k(\tau) + \varepsilon_T(\tau)$$

2	$\delta_T(\tau)$	the forecasted trucking capacity in hours for period $\tau$ as of time T	$x_2(\tau)$	1 if $D(\tau)$ is a Tuesday, 0 otherwise
	$Lo(\tau)$	the number of loadings during period $\tau$	$x_3(\tau)$	1 if $D(\tau)$ is a Wednesday, 0 otherwise
	$De(\tau)$	the number of deliveries during period $\tau$	$x_4(\tau)$	1 if $D(\tau)$ is a Thursday, 0 otherwise
	$Lo_{D(\tau)}$	the number of loadings during $D(\tau)$ , but not in period $\tau$	$x_5(\tau)$	1 if $D(\tau)$ is a Friday, 0 otherwise
	$De_{D(\tau)}$	the number of deliveries during $D(\tau)$ , but not in period $\tau$	$x_6(\tau)$	1 if $D(\tau)$ is a Saturday, 0 otherwise
	$\delta(\tau - 14)$	the actual trucking capacity in hours in period $\tau - 14$ (i.e. one week ago)	$x_7(\tau)$	1 if $D(\tau)$ is a holiday, 0 otherwise
	$\delta(\tau - 28)$	the actual trucking capacity in hours in period $\tau - 28$ (i.e. two weeks ago)	$x_8(\tau)$	1 if period $\tau$ falls within AM, 0 otherwise
	$x_1(\tau)$	1 if $D(\tau)$ is a Monday, 0 otherwise	$\varepsilon_T(\tau)$	error term

# A multiple linear regression model was developed to predict the required trucking capacity

Multiple linear regression model

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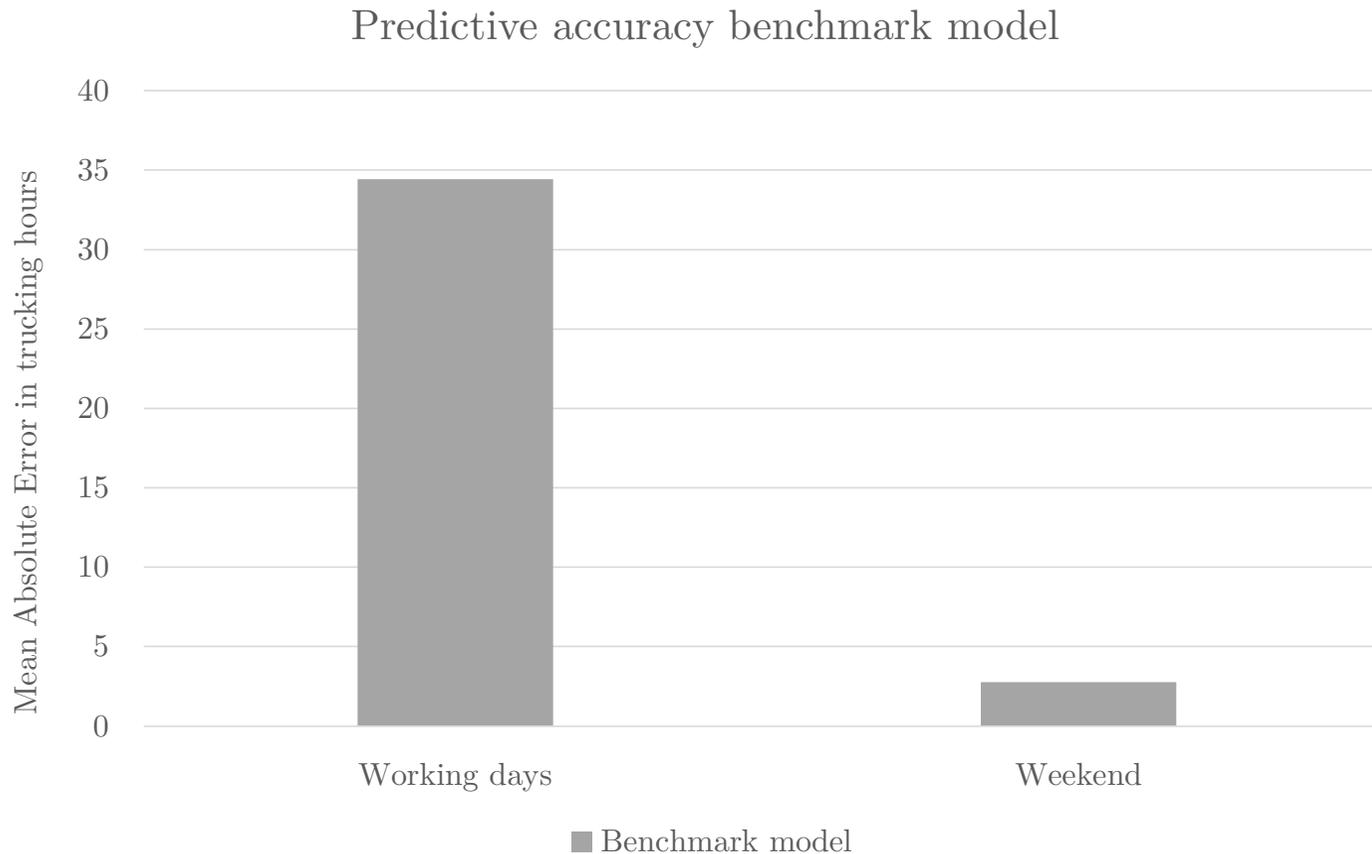
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	$\delta(\tau - 28)$	the actual trucking capacity in hours in period $\tau - 28$ (i.e. two weeks ago)
$x_1(\tau)$	1 if $D(\tau)$ is a Monday, 0 otherwise	

$x_2(\tau)$	1 if $D(\tau)$ is a Tuesday, 0 otherwise
$x_3(\tau)$	1 if $D(\tau)$ is a Wednesday, 0 otherwise
$x_4(\tau)$	1 if $D(\tau)$ is a Thursday, 0 otherwise
$x_5(\tau)$	1 if $D(\tau)$ is a Friday, 0 otherwise
$x_6(\tau)$	1 if $D(\tau)$ is a Saturday, 0 otherwise
$x_7(\tau)$	1 if $D(\tau)$ is a holiday, 0 otherwise
$x_8(\tau)$	1 if period $\tau$ falls within AM, 0 otherwise
$\varepsilon_T(\tau)$	error term

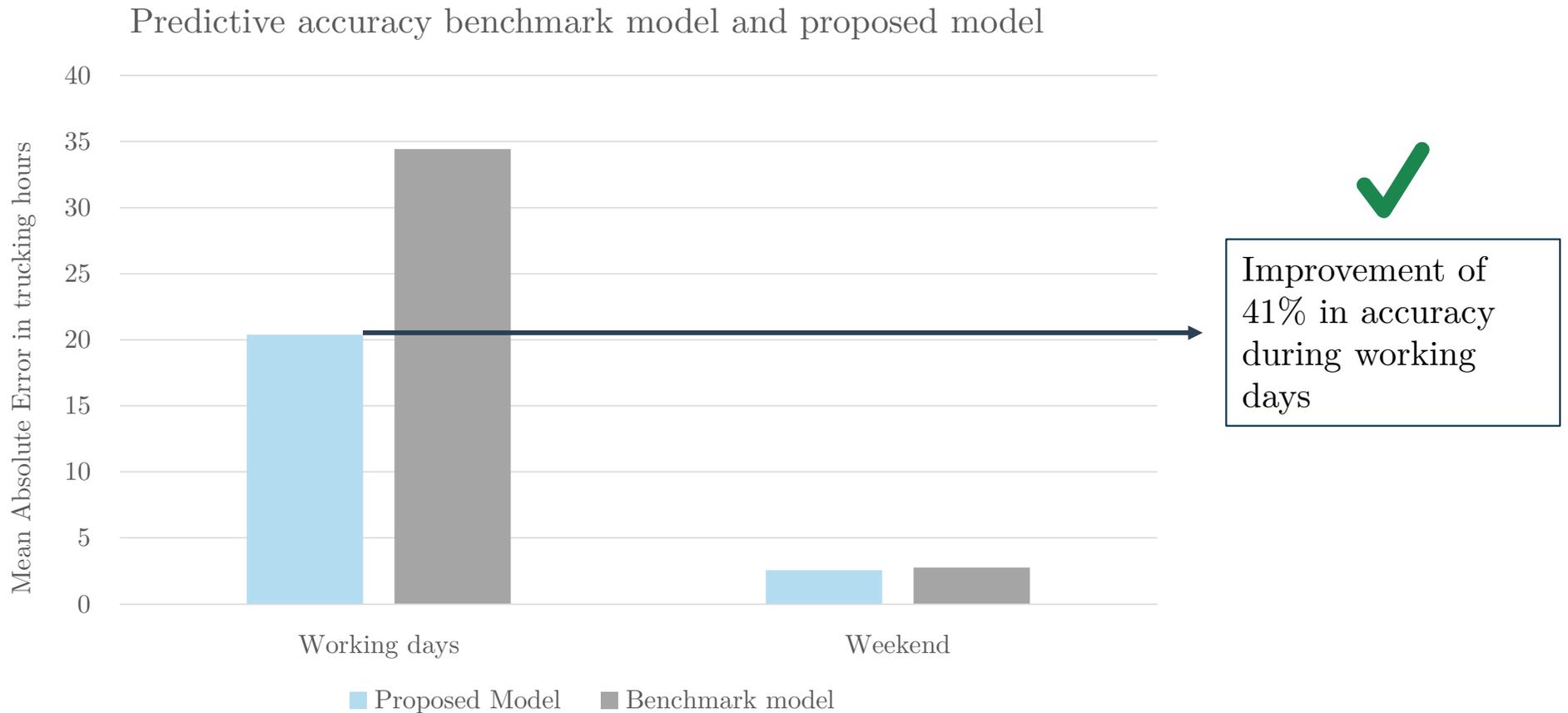
# The proposed forecasting model is compared against a benchmark model that is currently used at H&S

*Accuracy proposed forecasting methodology BFN region*



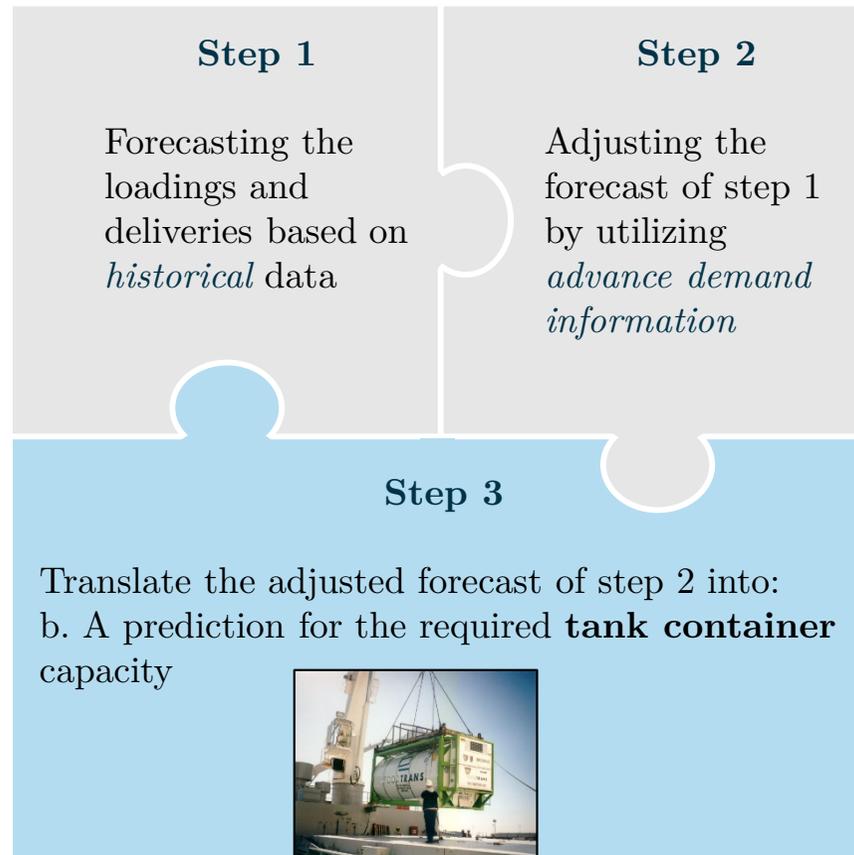
# The proposed forecasting model is 41% more accurate than the current model in the BFN region

*Accuracy proposed forecasting methodology BFN region*



# Step 3b: How can the forecasted loadings be converted to the required tank container capacity?

Step 3b



# Recall that the output of the Bayesian algorithm is a forecast of the expected number of loadings (and deliveries)

*Recap Bayesian of step 1 and 2*

Historical data forecast



Artificial Neural Network



Dynamic Harmonic Regression



Simple Mean Method



Bayesian algorithm



Output

The forecasted number of **loadings** (and deliveries) in a certain region in a given period

# Every (forecasted) loading represents the need for exactly one tank container

*Idea tank container forecast*

Historical data forecast



Artificial Neural Network



Dynamic Harmonic Regression



Simple Mean Method



Bayesian algorithm



Output

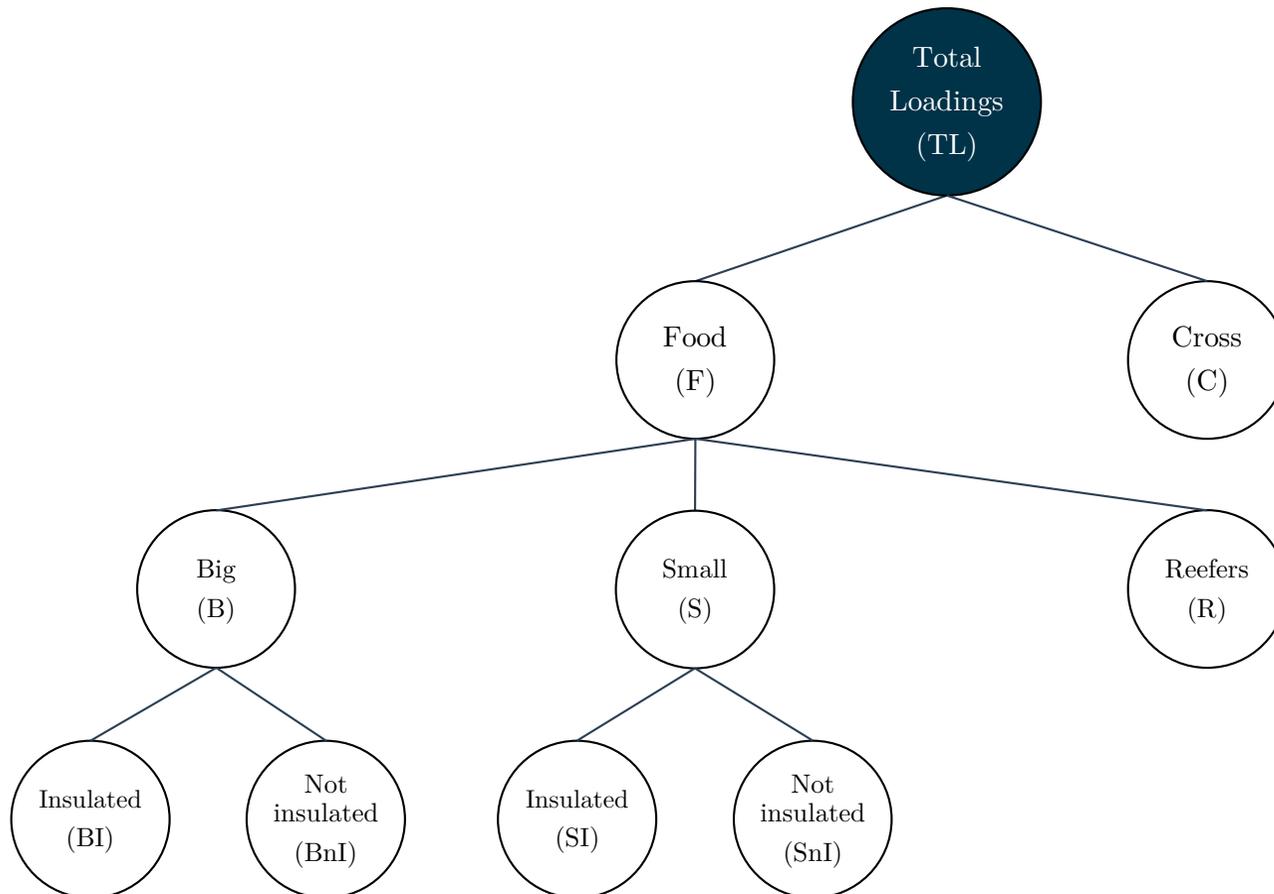
The forecasted number of **loadings** (and deliveries) in a certain region in a given period



*Assumption:* every (forecasted) loading in a certain region represents the need for exactly 1 tank container

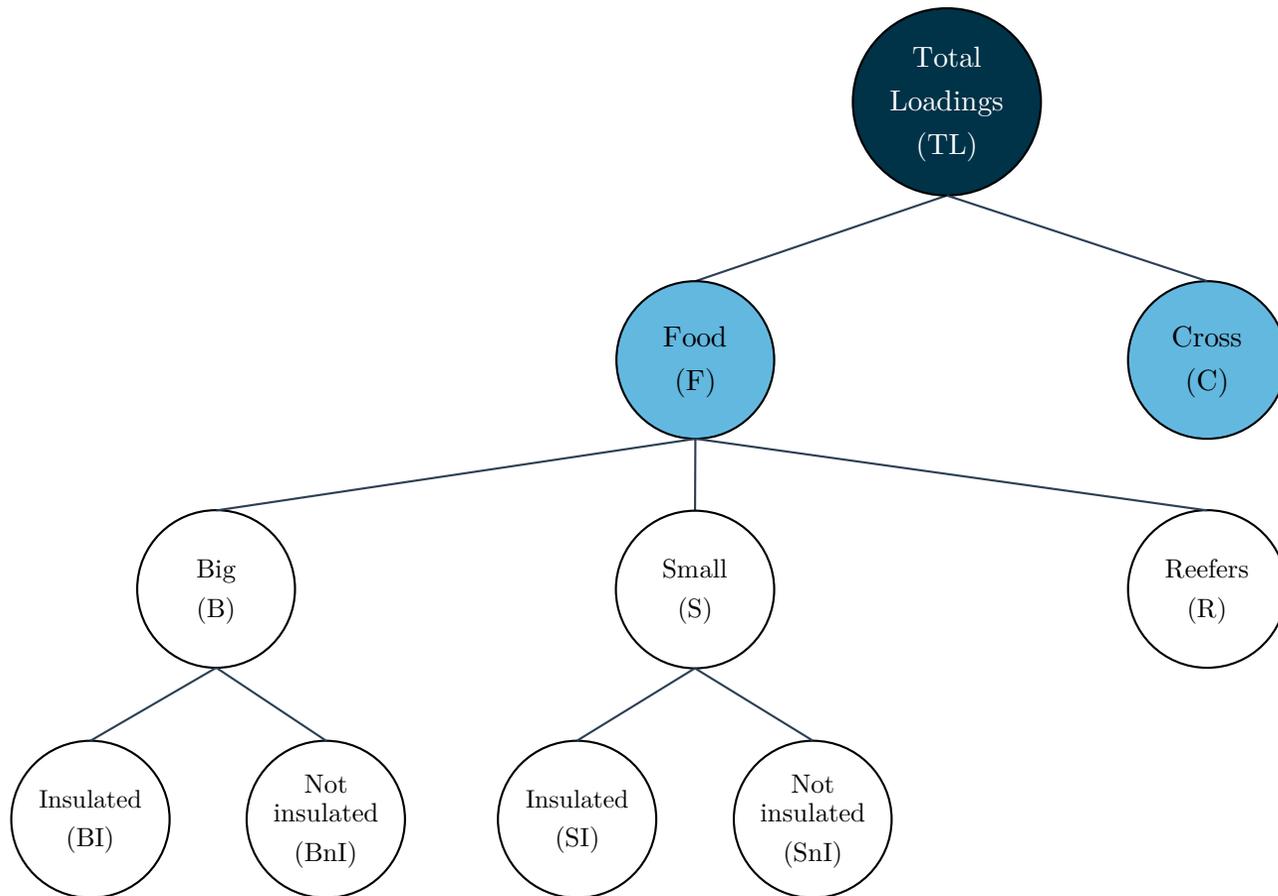
# The total number of loadings can be disaggregated by type of tank container

*Hierarchical time series tank container types H&S*



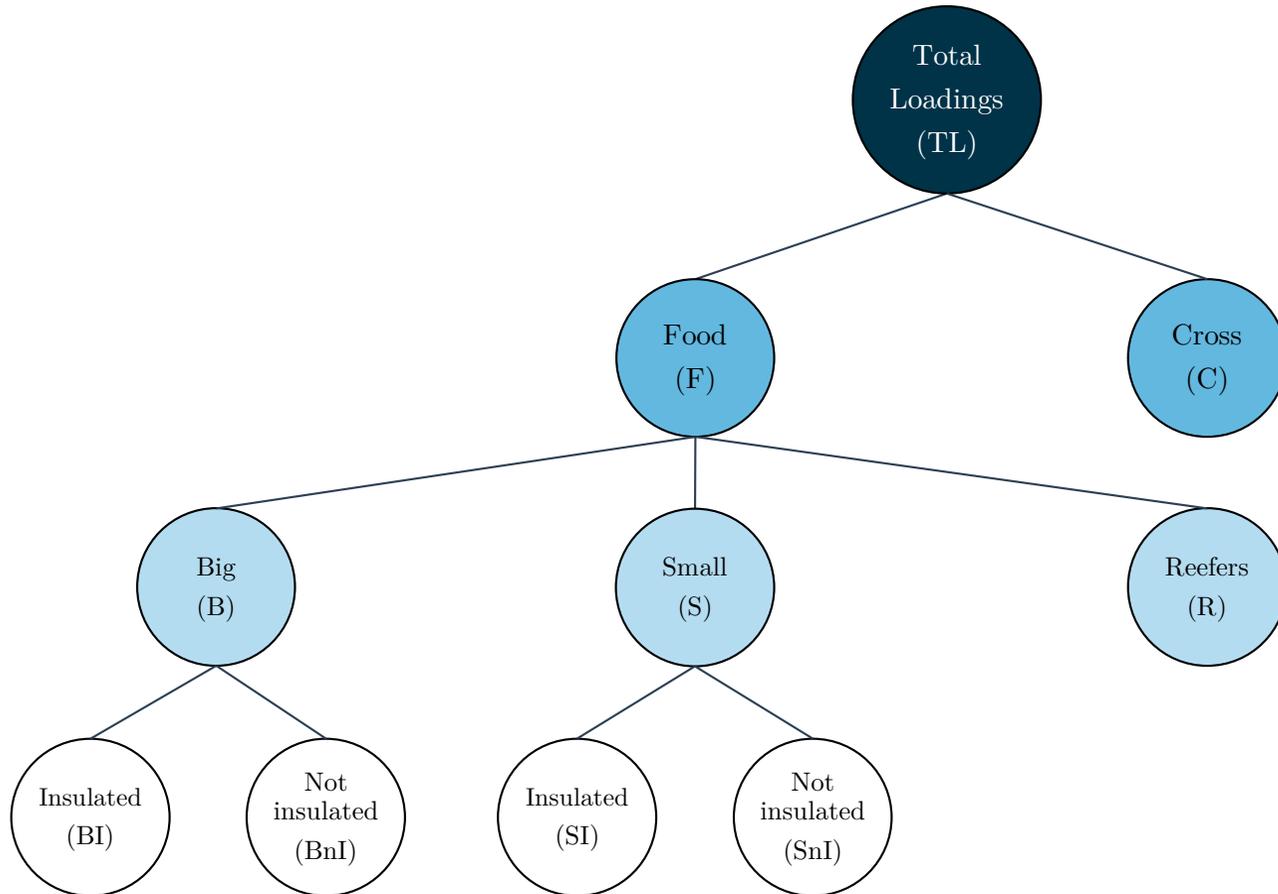
# The total number of loadings can be disaggregated by type of tank container

*Hierarchical time series tank container types H&S*



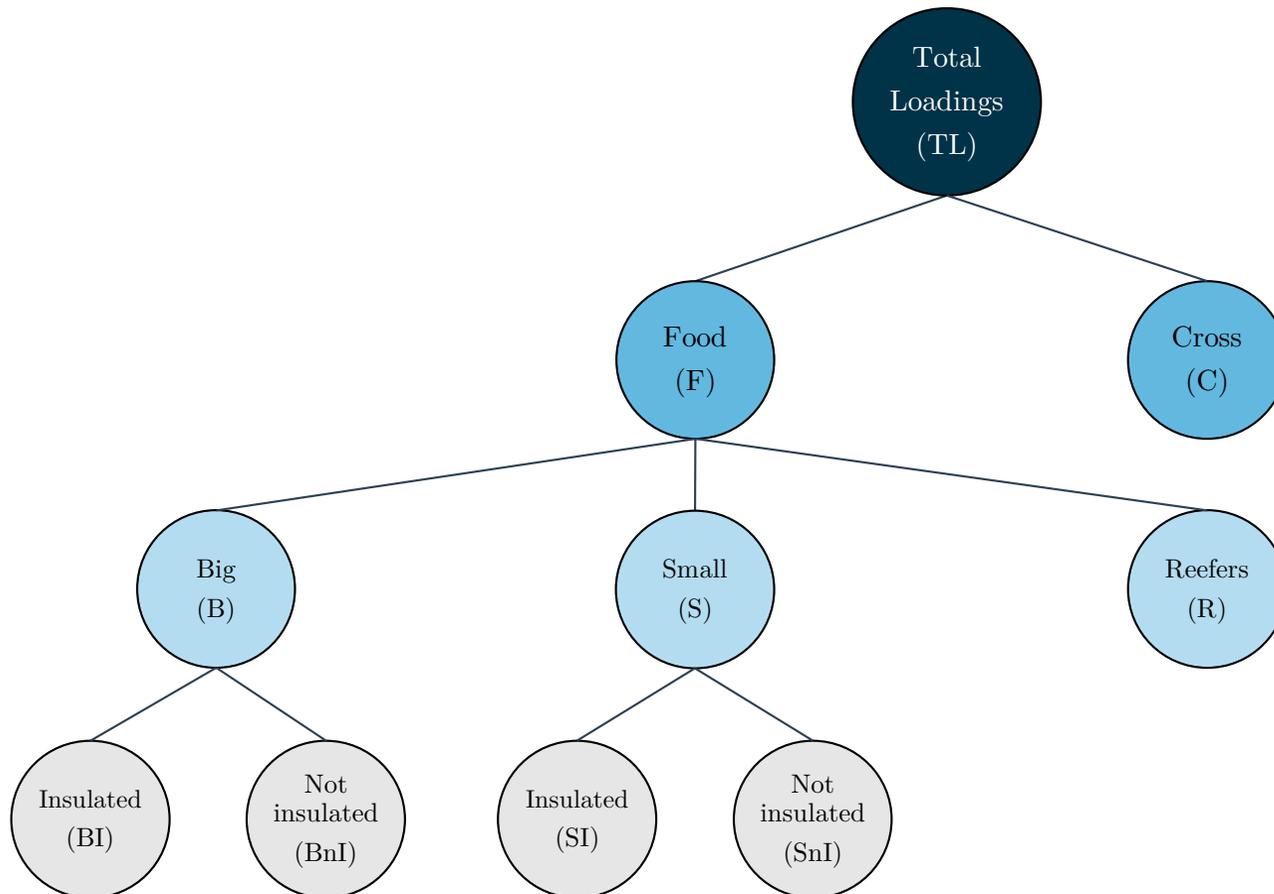
# The total number of loadings can be disaggregated by type of tank container

*Hierarchical time series tank container types H&S*



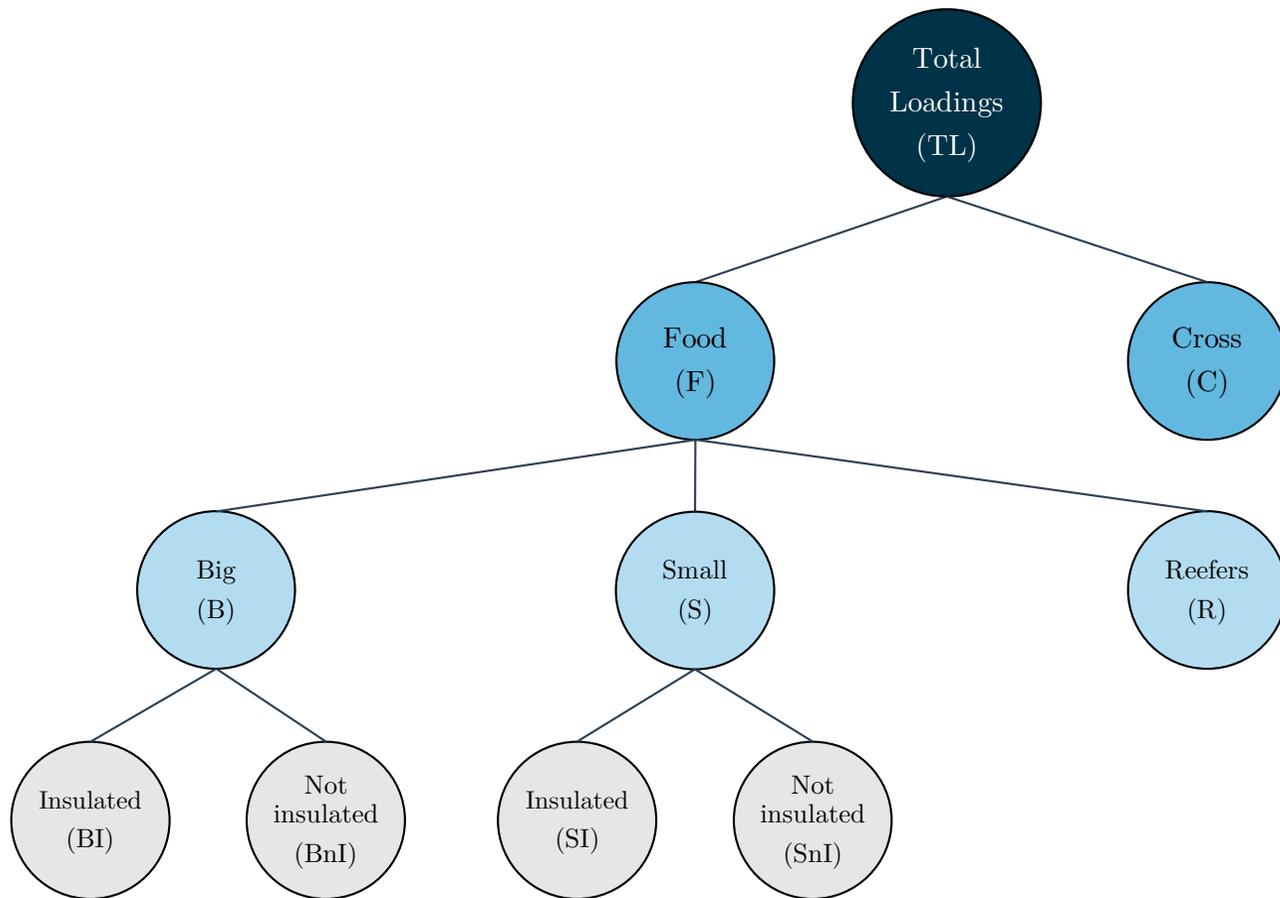
# The total number of loadings can be disaggregated by type of tank container

*Hierarchical time series tank container types H&S*



# How can a forecast be obtained for every type of tank container?

*Tank container forecast*



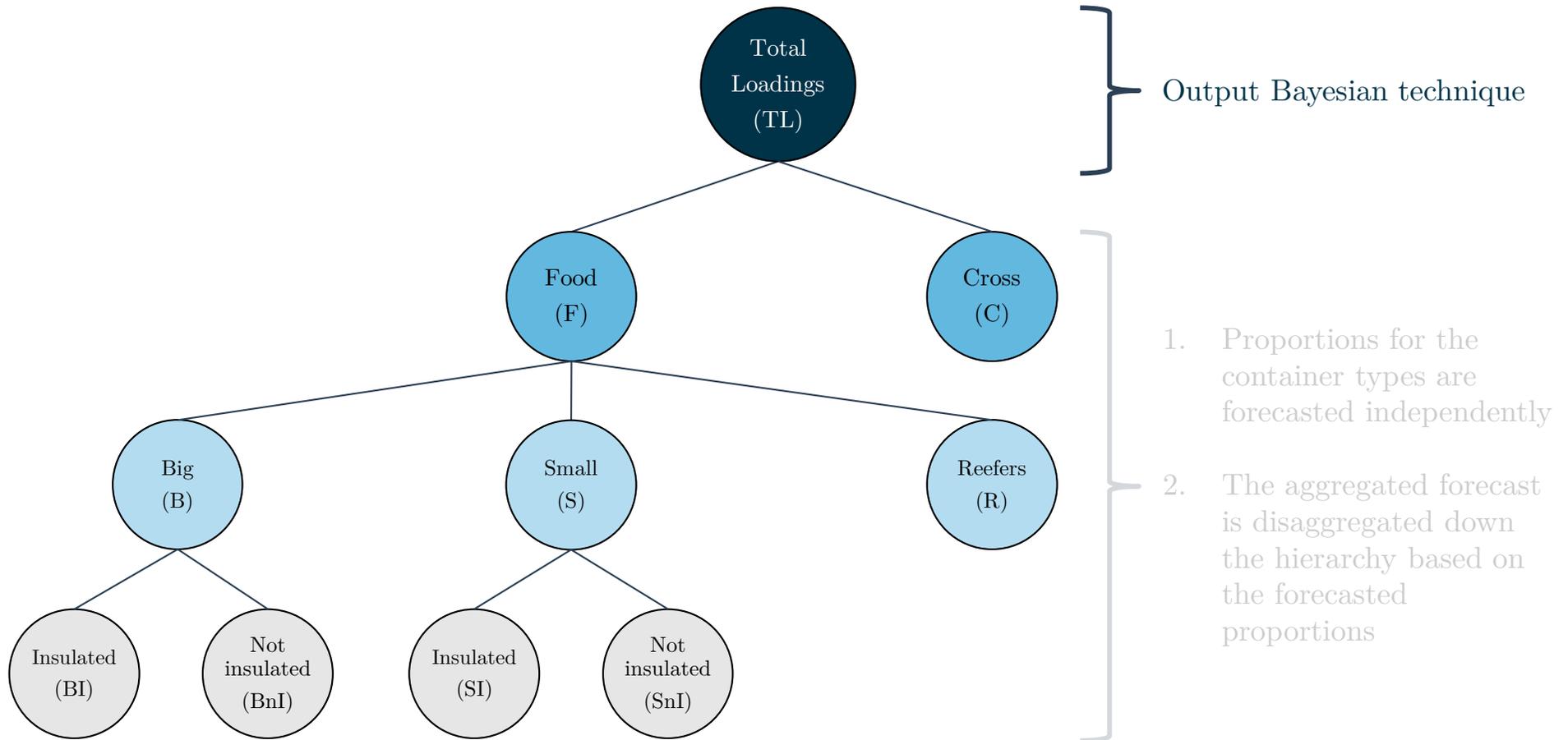
Tank container forecast

Output Bayesian technique

1. Proportions for the container types are forecasted independently
2. The aggregated forecast is disaggregated down the hierarchy based on the forecasted proportions

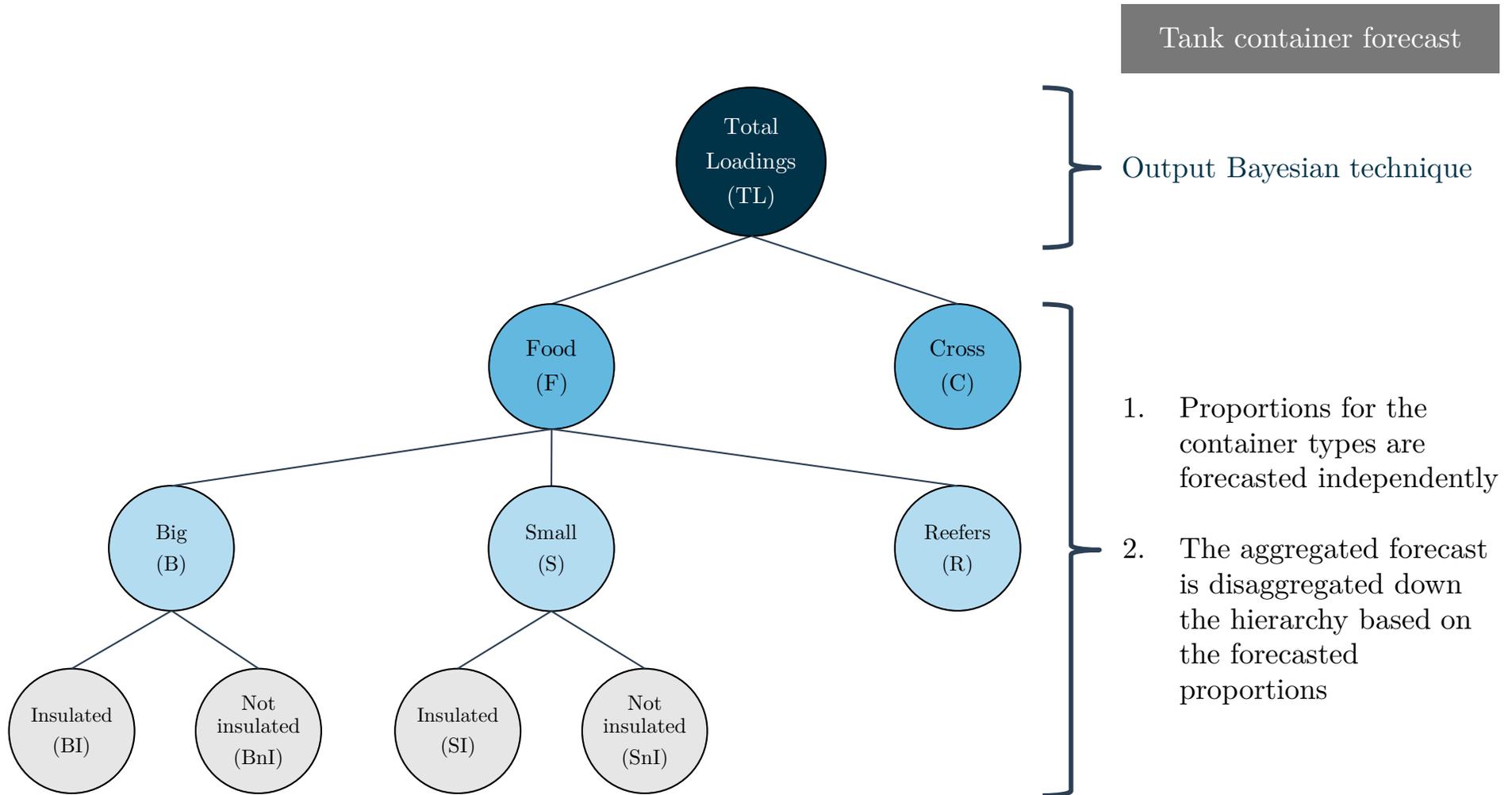
# The next question to answer is how the total number of loadings should be disaggregated to obtain a forecast per tank container type

*Tank container forecast*

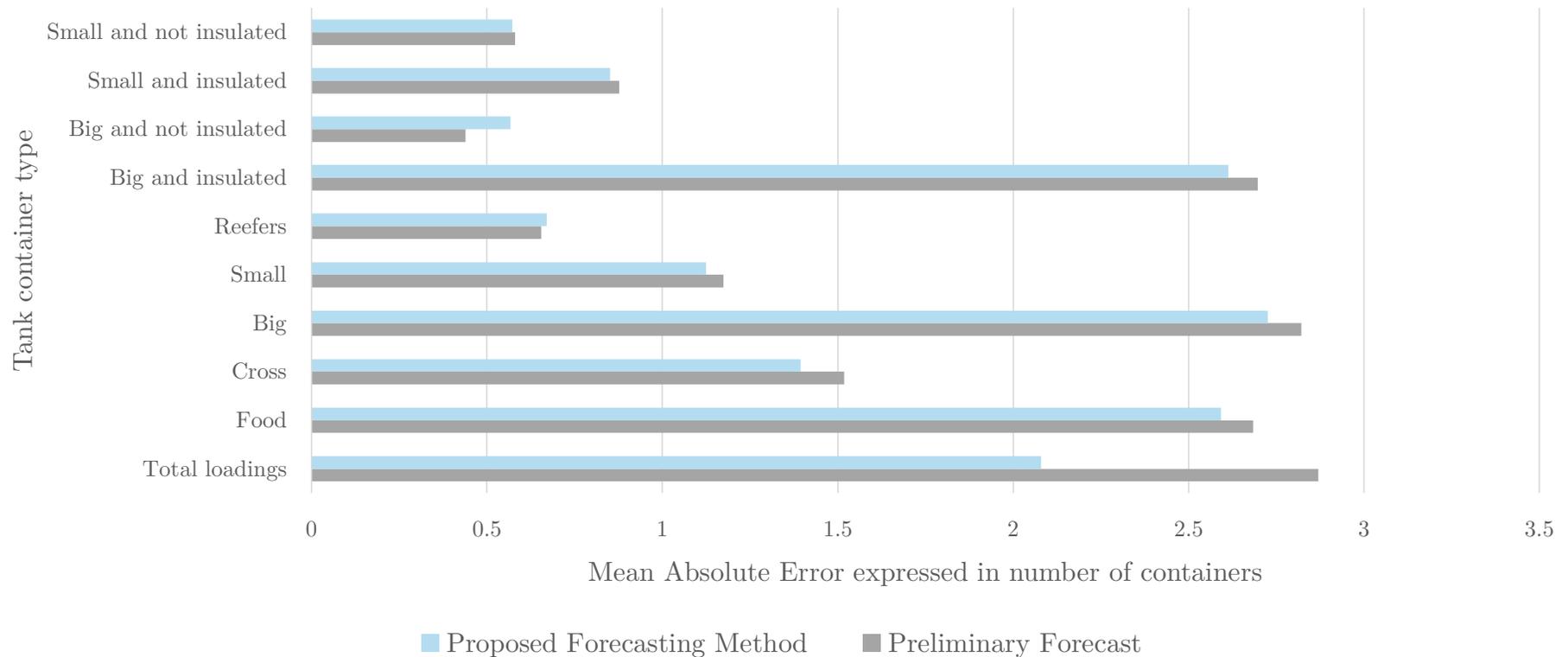


# The next question to answer is how the total number of loadings should be disaggregated to obtain a forecast per tank container type

*Tank container forecast*



# Predictive accuracy tank container forecast in the Rotterdam planning region



- Mean Absolute Error differs per type of tank container
- For most aggregation levels it outperforms the preliminary forecast, albeit not by much



Introduction  
and problem  
description



Proposed  
forecasting  
methodology



Completing the  
circle: benefits &  
implementation



Discussion

# Account managers might use the forecast to create a more balanced workload which might in turn lead to a reduction in trucking costs

Who will use the forecast?



Account managers

Which decisions will the forecast support?

Proactively (re)plan orders to **smooth workload** throughout the day and week

What will be the benefits?

- Decrease in the number of trucks needed → reduction in costs
- 5% improvement in balance between AM & PM results in approximately €750,000



TCP and MMP planners

- **Book charters** earlier in the process
- Assist Guido and Samara to make more **efficient repositioning decisions** of empty tanks (yearly costs > €11,000,000)

- Lower charter costs and increased quality
- Enhanced performance towards clients
- **Reduction in empty tank container repositioning costs**
- Reduces risk



Commercial managers

Proactively look for work for periods in which the demand is expected to be low (i.e. **commercial focus on filling gaps**)

- Workload more equally divided
- Increased utilization of own trucks



Purchasing managers

Book charters earlier in the process (i.e. **purchasing decisions of charters**)

- Lower charter costs and increased quality
- Enhanced performance towards clients

# TCP and MMP planners might use the forecast to book charters at an earlier stage and make more efficient tank container repositioning decisions

Who will use the forecast?



Account managers

Which decisions will the forecast support?

Proactively (re)plan orders to **smooth workload** throughout the day and week

What will be the benefits?

- Decrease in the number of trucks needed → reduction in costs
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# Commercial managers might use the forecast to proactively look for work for periods in which the demand is expected to be low

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- Workload more equally divided
- Increased utilization of own trucks



Purchasing managers

Book charters earlier in the process (i.e. **purchasing decisions of charters**)

- Lower charter costs and increased quality
- Enhanced performance towards clients

# In addition to TCP planners, purchasing managers might also use the forecast to book charters at an earlier stage

Who will use the forecast?



Account managers

Which decisions will the forecast support?

Proactively (re)plan orders to **smooth workload** throughout the day and week

What will be the benefits?

- Decrease in the number of trucks needed → reduction in costs
- 5% improvement in balance between AM & PM results in approximately €750,000



TCP and MMP planners

- **Book charters** earlier in the process
- Assist Guido and Samara to make more **efficient repositioning decisions** of empty tanks (yearly costs > €11,000,000)

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Commercial managers

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- Workload more equally divided
- Increased utilization of own trucks



Purchasing managers

Book charters earlier in the process (i.e. **purchasing decisions of charters**)

- Lower charter costs and increased quality
- Enhanced performance towards clients

# The forecasting methodology proposed by this research is now being implemented at H&S (and Den Hartogh)

*Implementation project*

## Stakeholders implementation project



## Timeline implementation project





Introduction  
and problem  
description



Proposed  
forecasting  
methodology



Completing the  
circle: benefits &  
implementation



Discussion



# Forecasting the required tank container and trucking capacity for an intermodal logistics service provider

27/08/2019

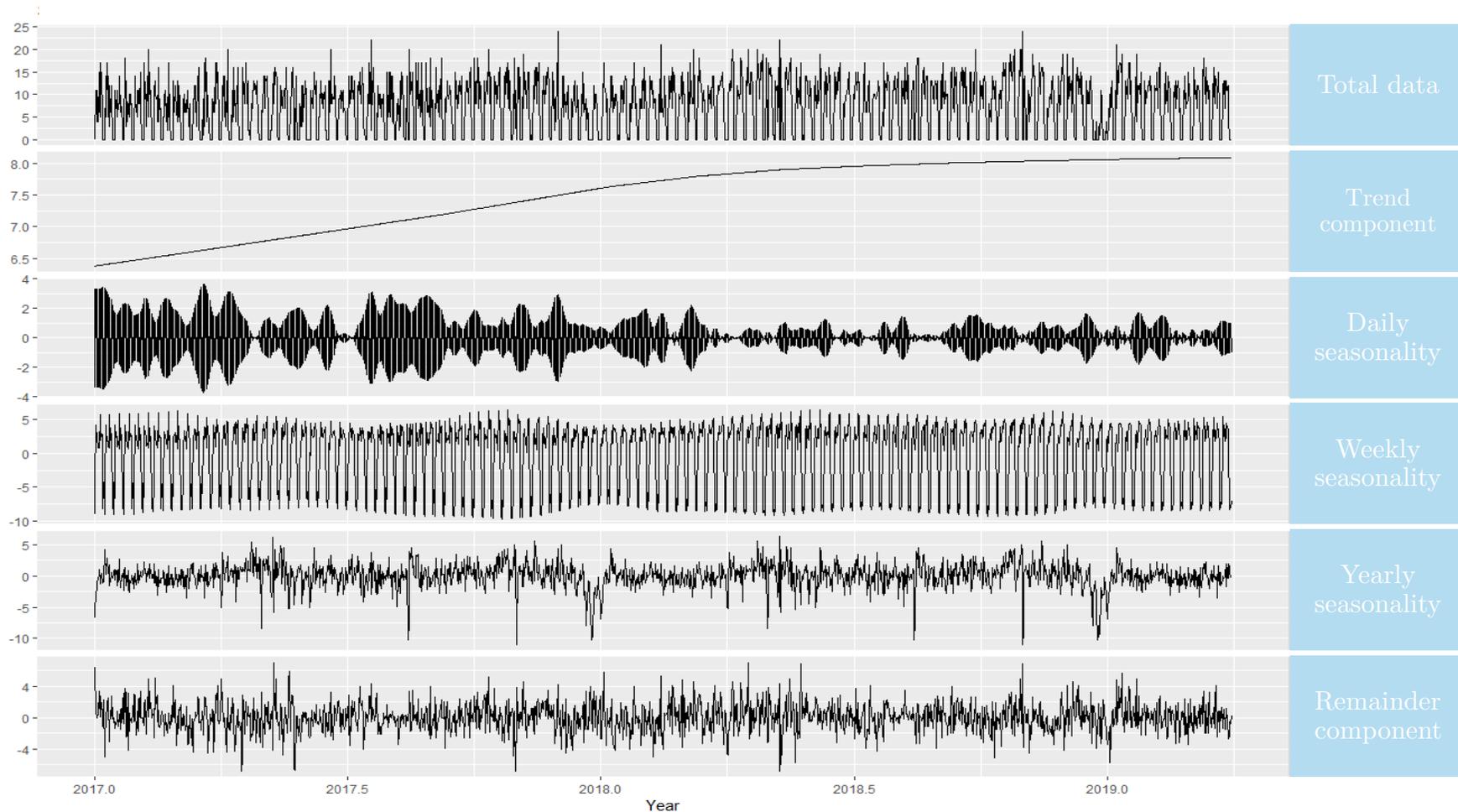
Rijk van der Meulen, MSc student Operations Management & Logistics

# APPENDIX A

*Forecasting accuracy models based on historical data*

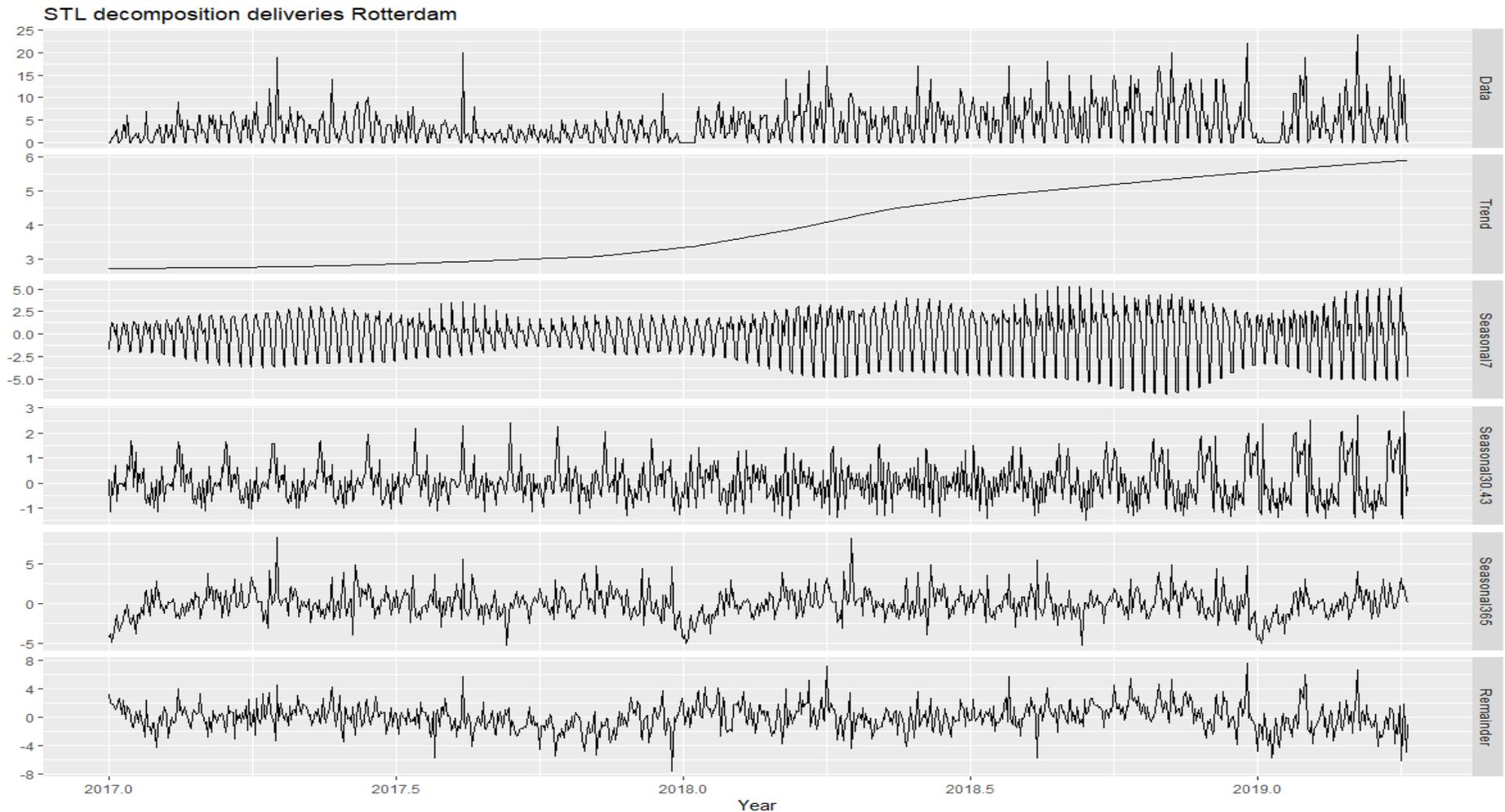
# The various seasonal components were analysed in each series using time series decomposition

*STL decomposition BFN loadings series*



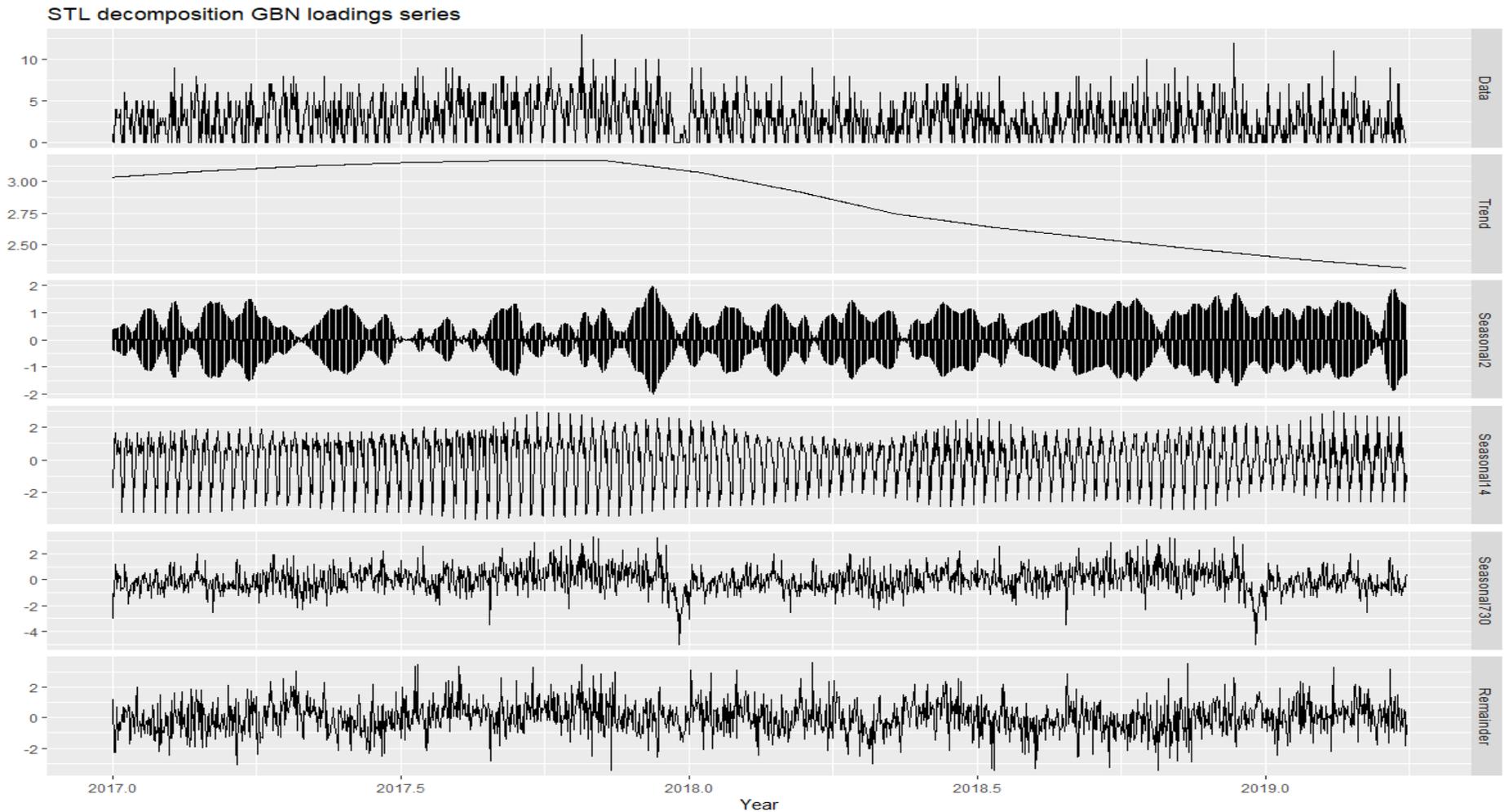
# Seasonal Trend Decomposition deliveries Rotterdam

*STL decomposition using Loess*



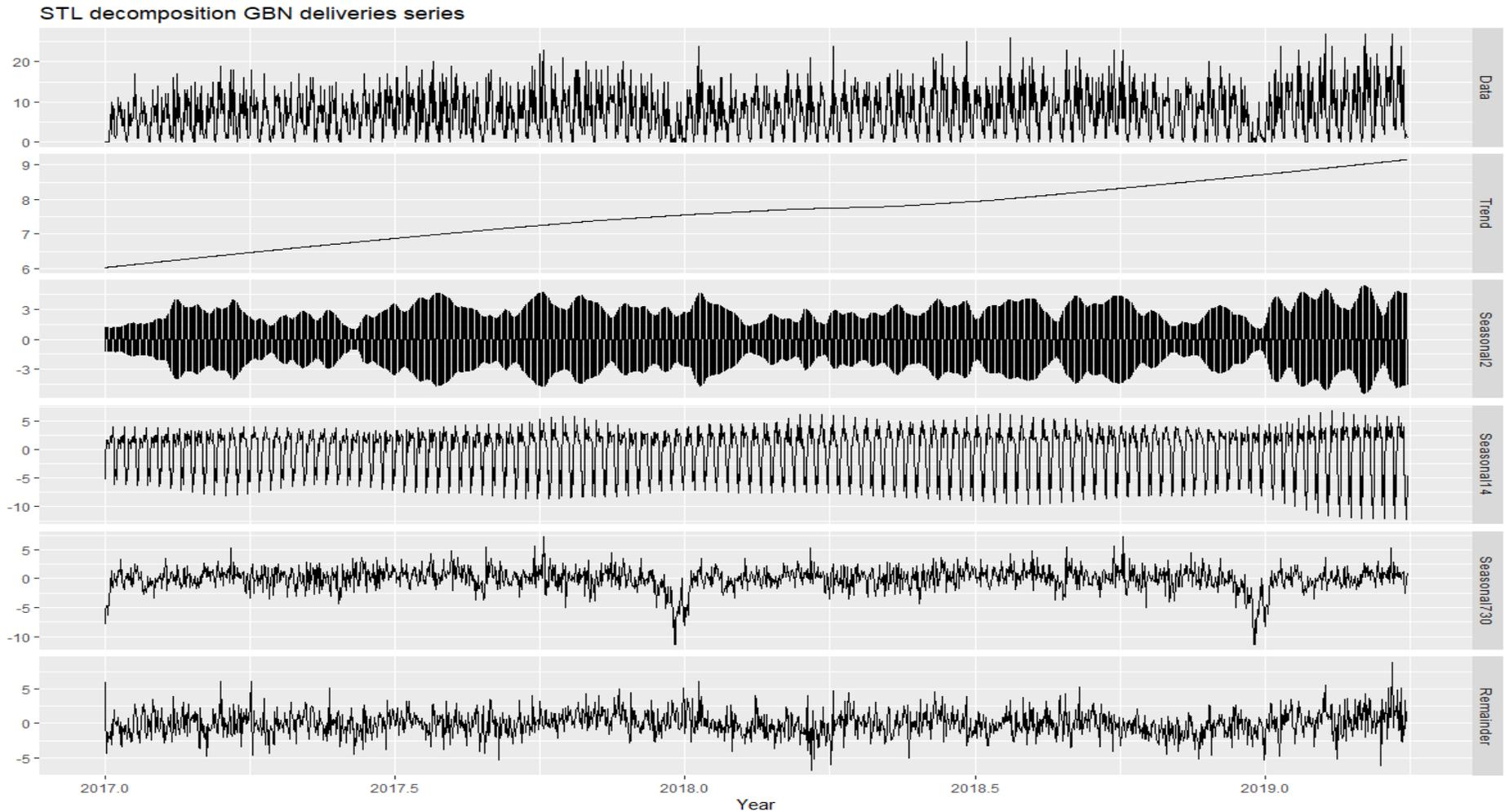
# Seasonal Trend Decomposition loadings GBN

*STL decomposition using Loess*



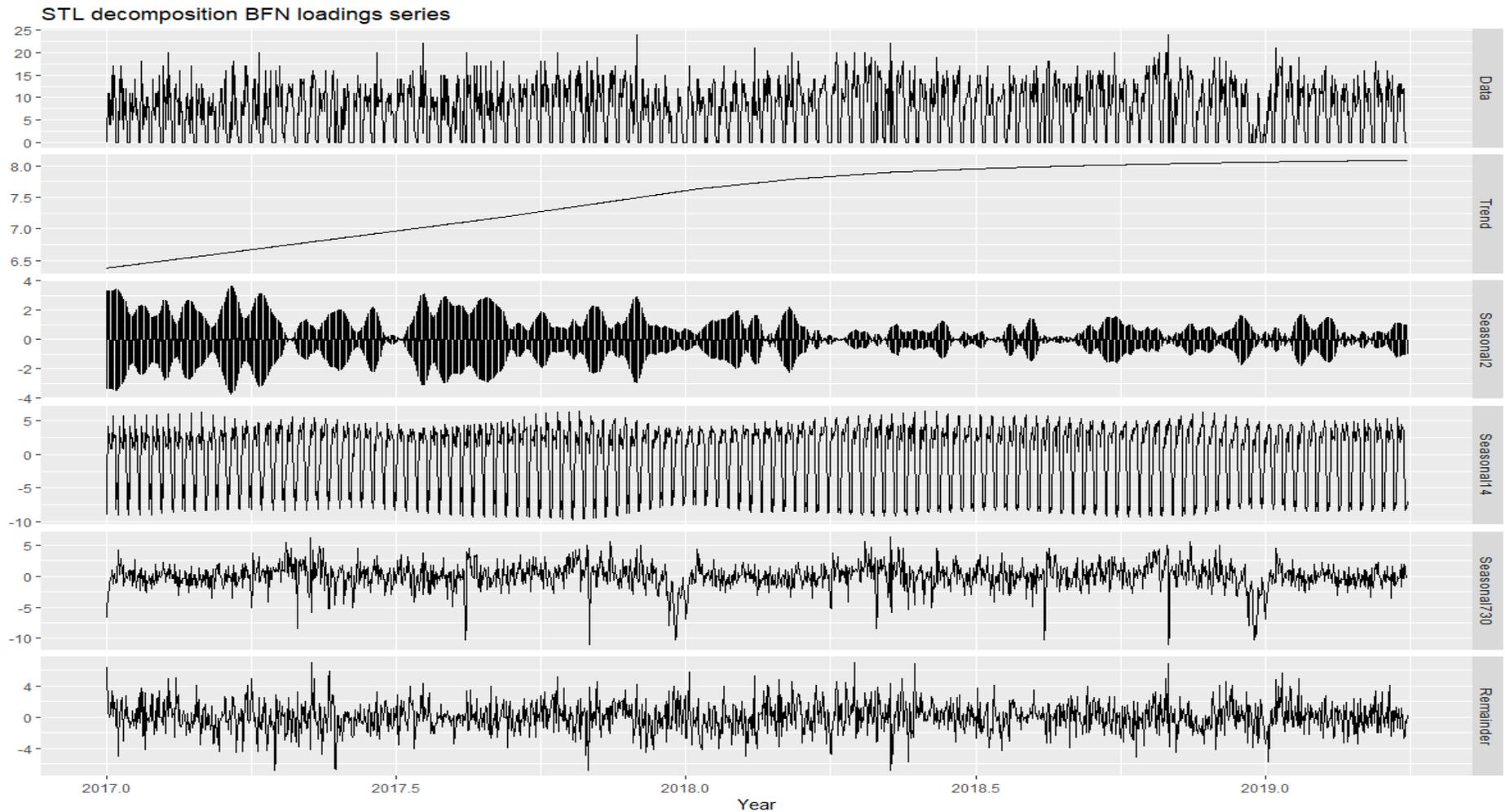
# Seasonal Trend Decomposition deliveries GBN

*STL decomposition using Loess*



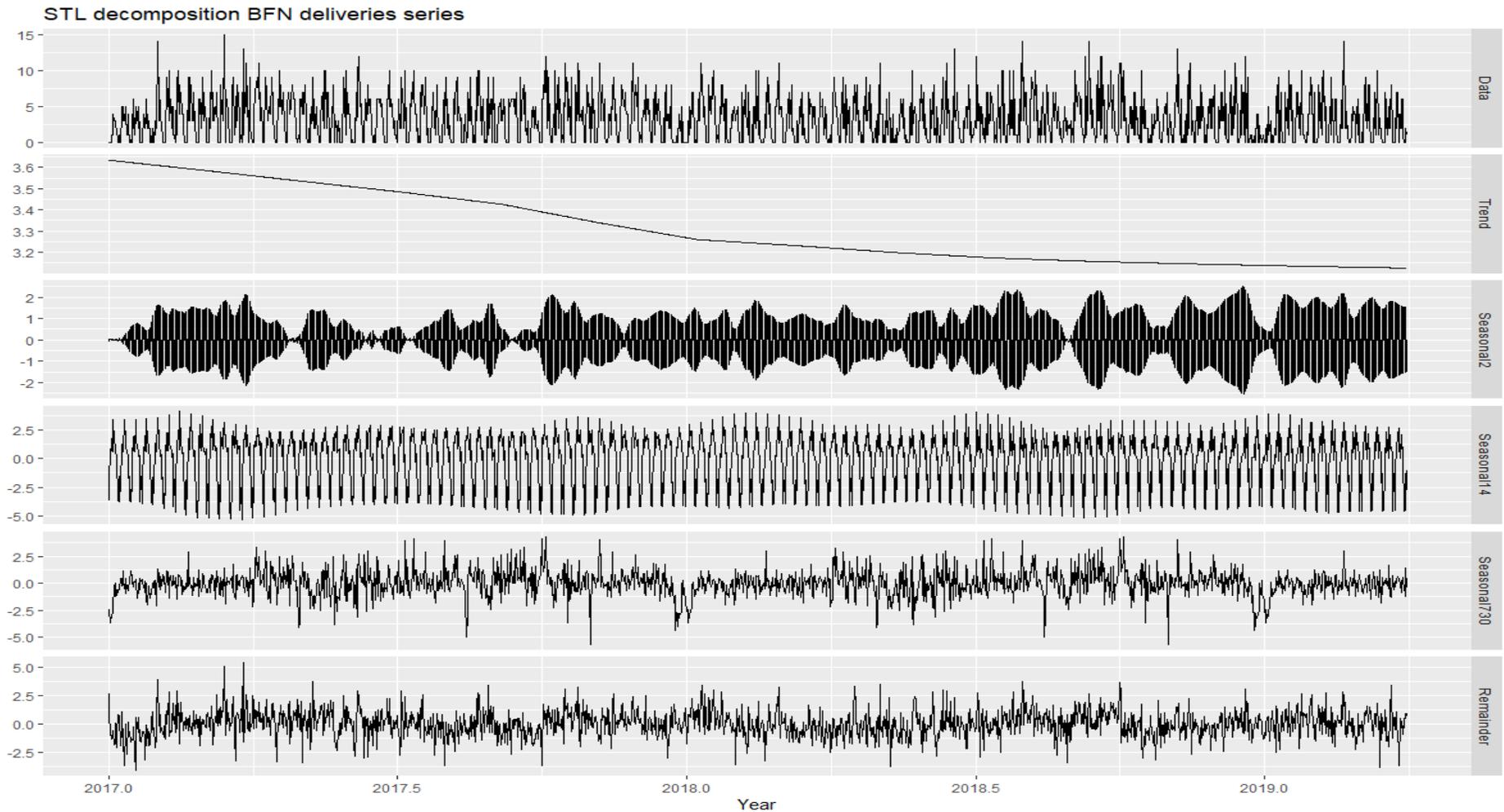
# Seasonal Trend Decomposition loadings BFN

*STL decomposition using Loess*

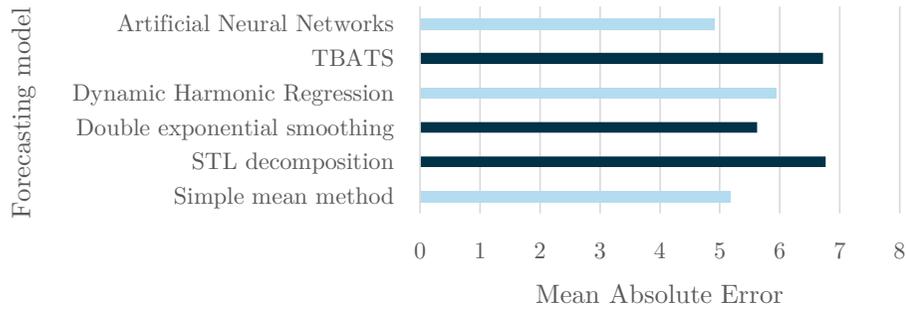


# Seasonal Trend Decomposition deliveries BFN

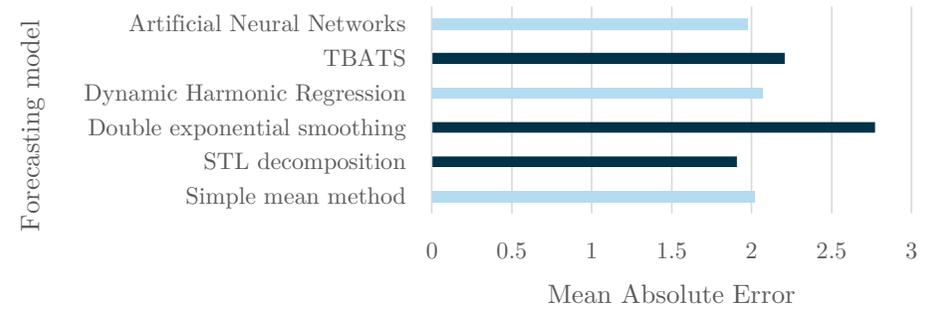
*STL decomposition using Loess*



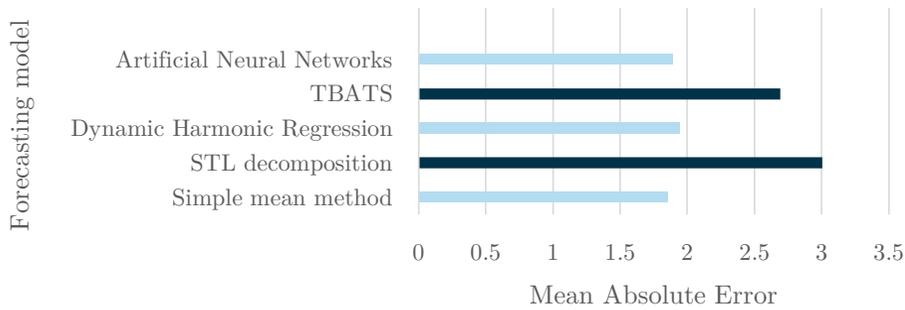
Rotterdam loadings series



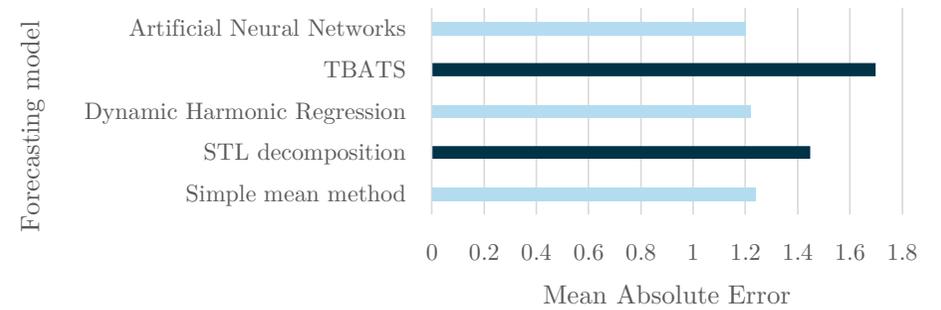
Rotterdam deliveries series



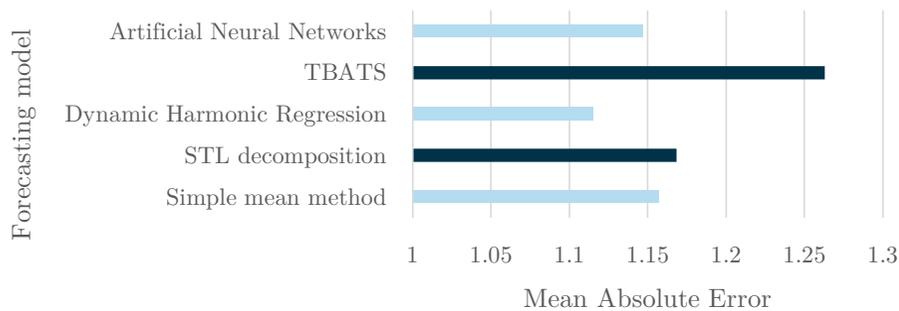
BFN loadings series



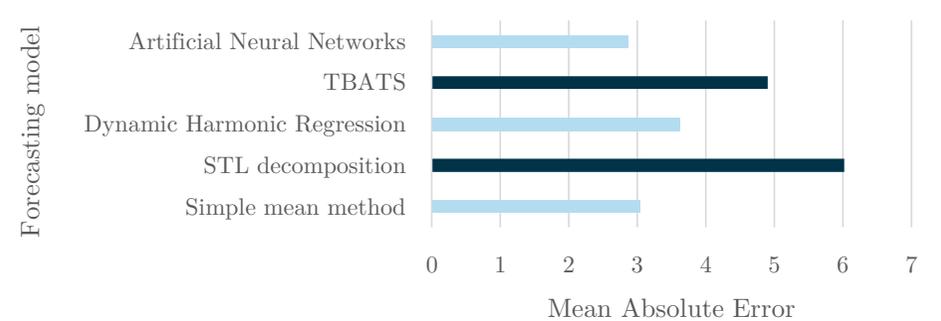
BFN deliveries series



GBN loadings series



GBN deliveries series



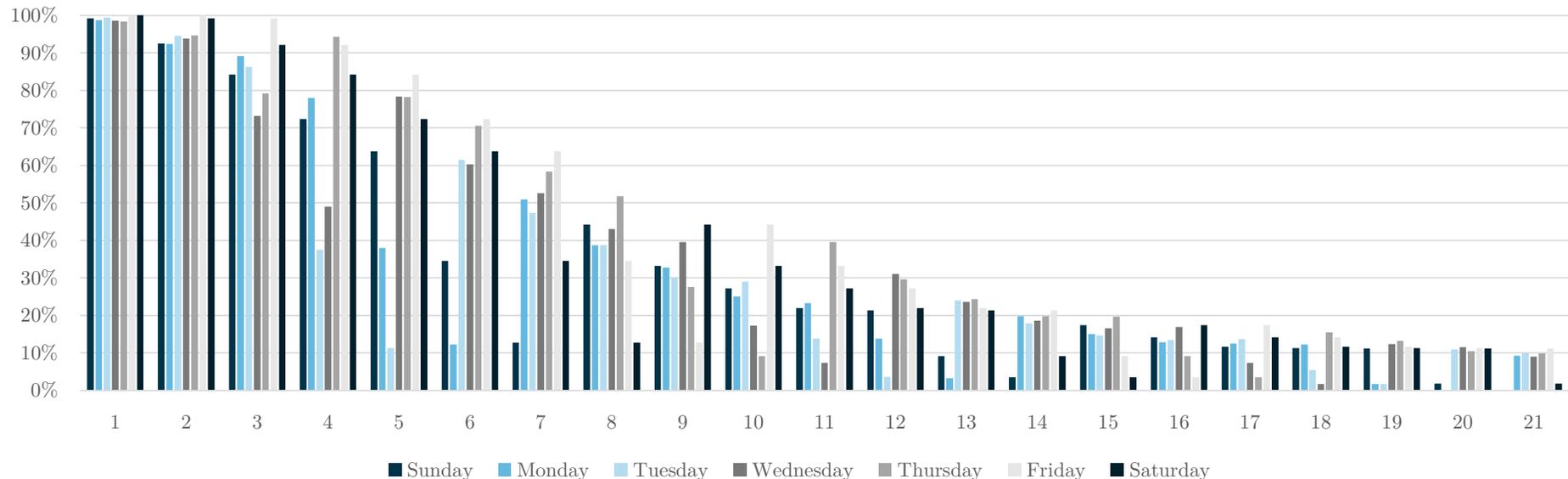
# APPENDIX B

*Utilizing the advance demand information*

# How long in advance are orders (i.e. loadings and deliveries) known?

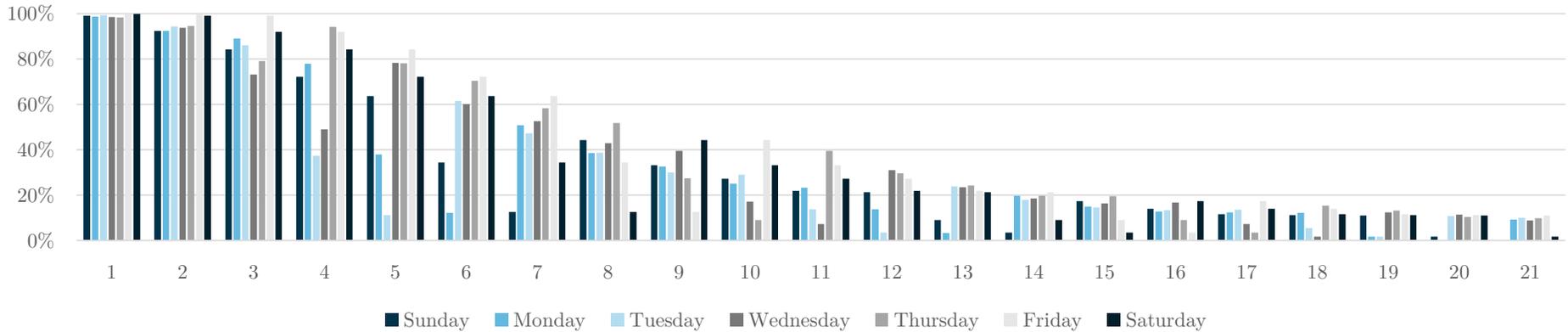
*Analysis order flow H&S*

- Depends on day of the week
- Varies per planning region
- Deliveries are known longer in advance than loadings (obviously)
- Note: estimated based on how long orders are placed in advance: this doesn't say anything regarding how often orders are changed after they have initially been placed! →
  - Changes due to planners' initiative: no problem since this doesn't represent customers demand?
  - Changes due to customers' initiative: more problematic as this does represent customers demand?

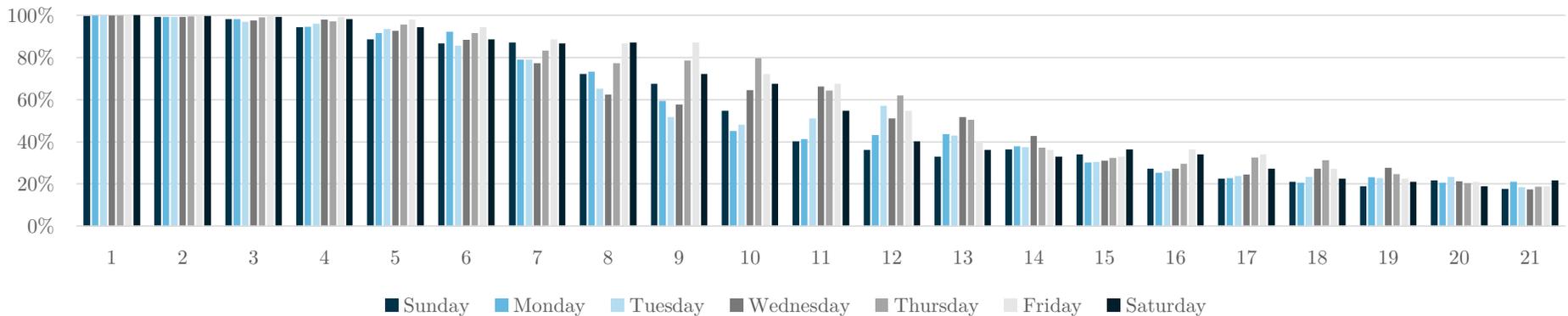


# How long in advance are loadings and deliveries known in the Rotterdam planning region?

## Loadings

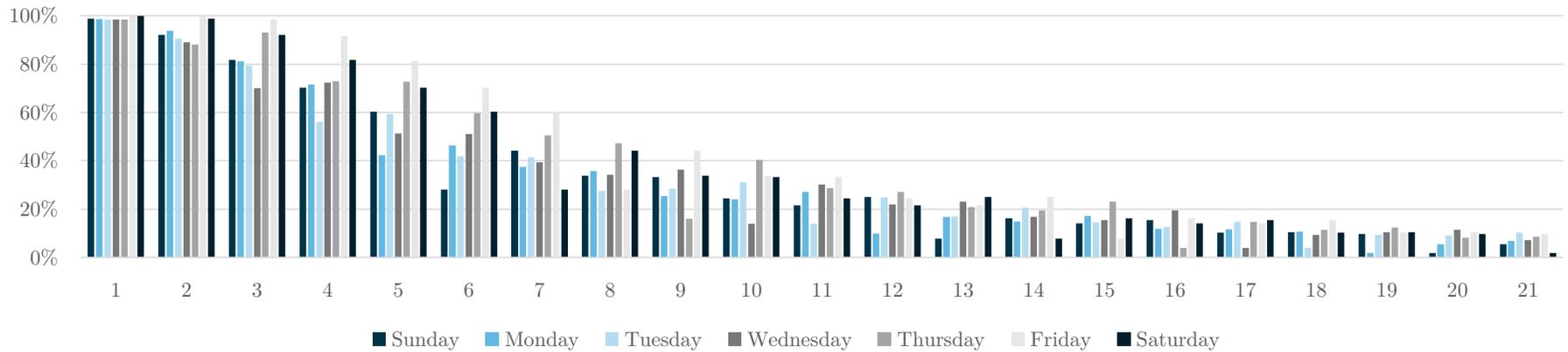


## Deliveries

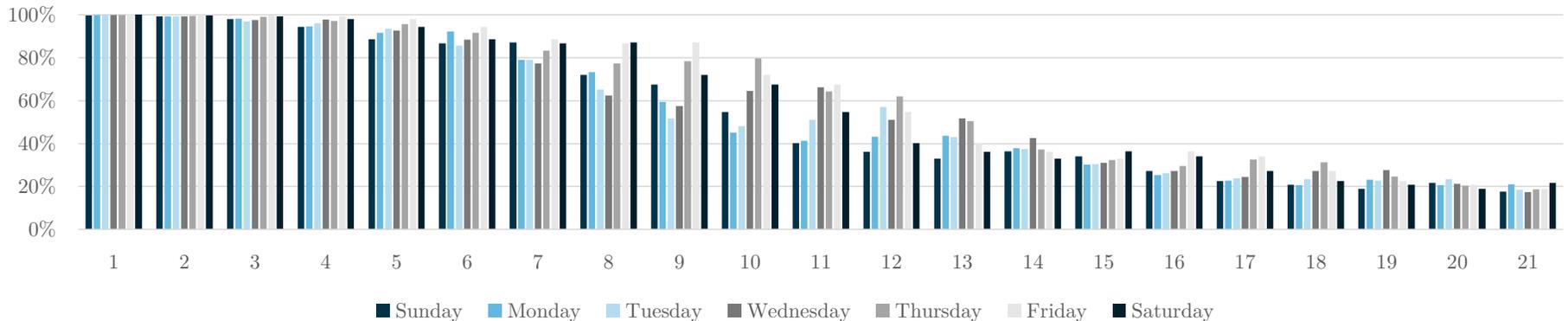


# How long in advance are loadings and deliveries known in the GBN planning region?

## Loadings

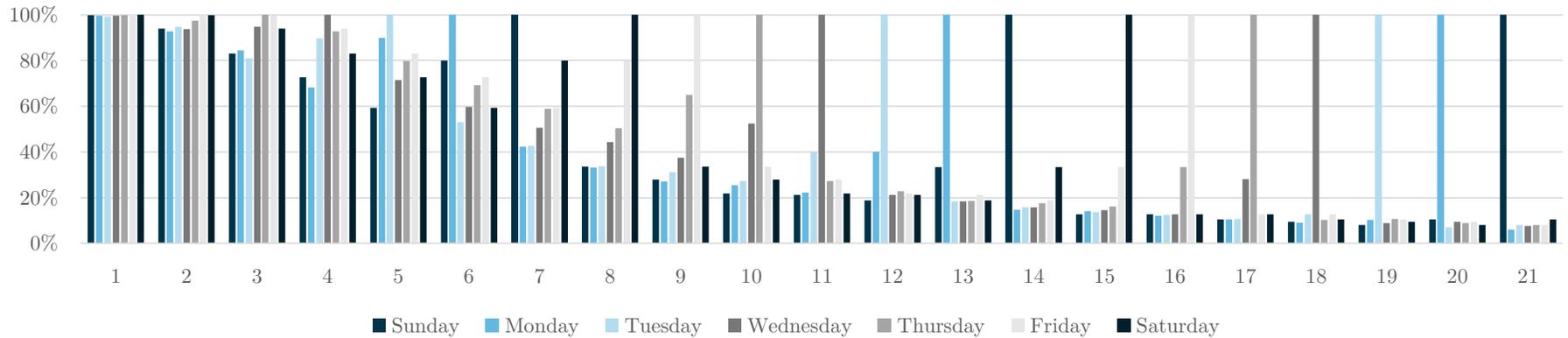


## Deliveries

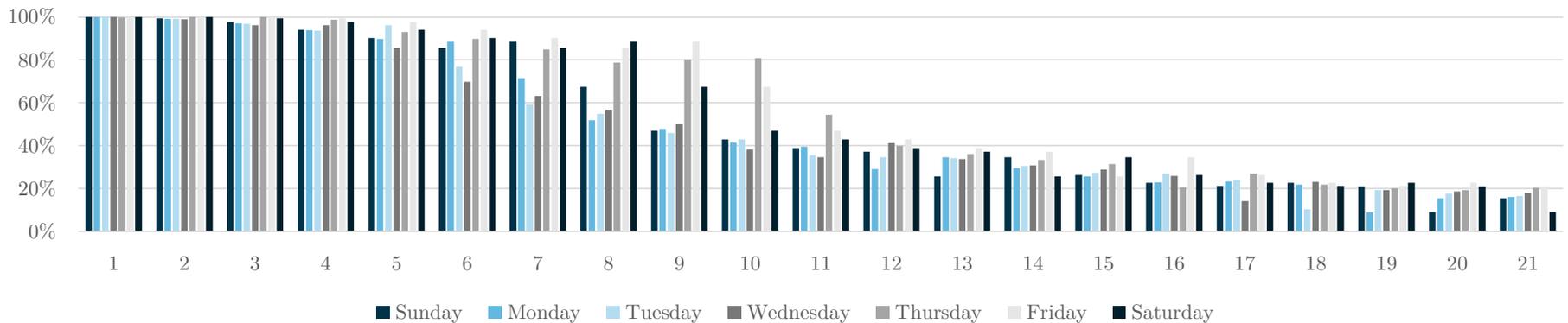


# How long in advance are loadings and deliveries known in the BFN planning region?

## Loadings



## Deliveries



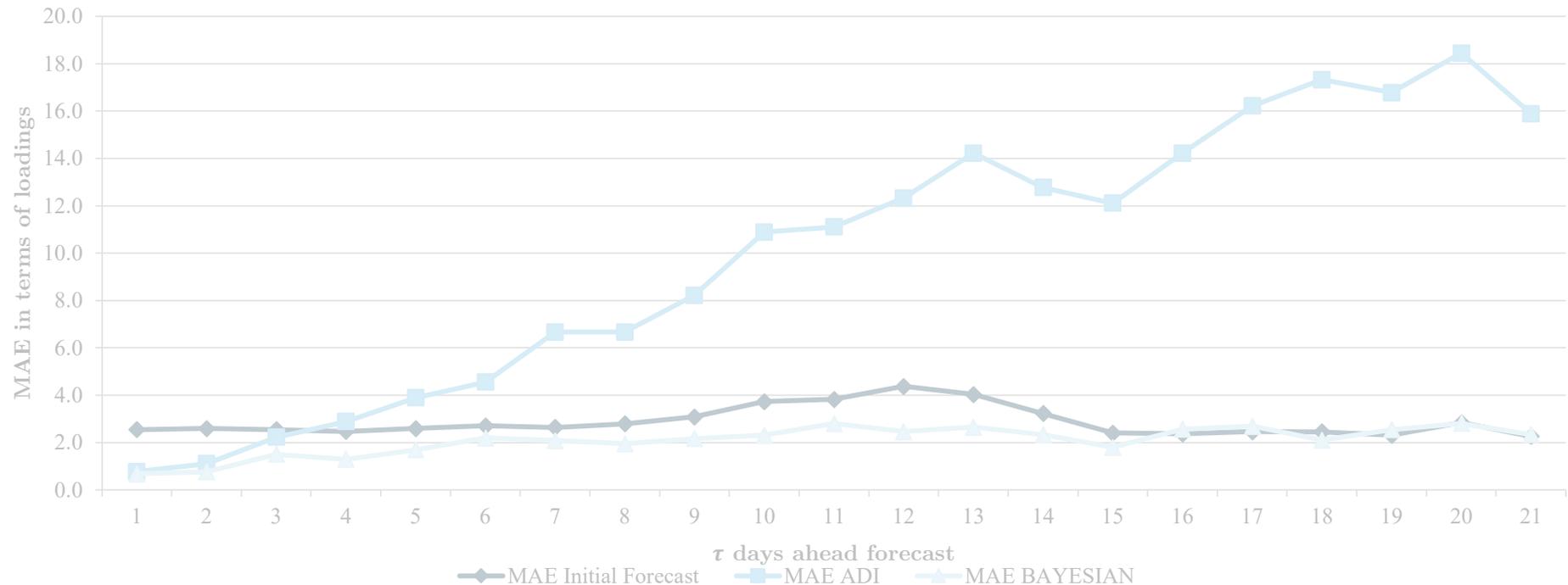
# Example Bayesian adjustment with $n_{a\tau} = 2$ , Initial forecast = 4 & Theta = 0.6

$n_j$	$P\langle n_j \rangle$	$P\langle n_{a\tau}   n_j \rangle$	$P\langle n_{a\tau}   n_j \rangle * P\langle n_j \rangle$	$P\langle n_j   n_{a\tau} \rangle$	$n_j P\langle n_j   n_{a\tau} \rangle$
0	-	-	-	-	-
1	-	-	-	-	-
2	0.146525	0.36	0.052749	0.201897	0.403793
3	0.195367	0.432	0.084398	0.323034	0.969103
4	0.195367	0.3456	0.067519	0.258428	1.03371
5	0.156293	0.2304	0.03601	0.137828	0.68914
6	0.104196	0.13824	0.014404	0.055131	0.330787
7	0.05954	0.077414	0.004609	0.017642	0.123494
8	0.02977	0.041288	0.001229	0.004705	0.037636
9	0.013231	0.021234	0.000281	0.001075	0.009678
10	0.005292	0.010617	5.62E-05	0.000215	0.002151
11	0.001925	0.00519	9.99E-06	3.82E-05	0.000421
12	0.000642	0.002491	1.6E-06	6.12E-06	7.34E-05
13	0.000197	0.001178	2.32E-07	8.9E-07	1.16E-05
14	5.64E-05	0.00055	3.1E-08	1.19E-07	1.66E-06
15	1.5E-05	0.000254	3.81E-09	1.46E-08	2.19E-07
16	3.76E-06	0.000116	4.36E-10	1.67E-09	2.67E-08
17	8.85E-07	5.26E-05	4.65E-11	1.78E-10	3.03E-09
18	1.97E-07	2.37E-05	4.65E-12	1.78E-11	3.2E-10
19	4.14E-08	1.06E-05	4.38E-13	1.68E-12	3.18E-11
20	8.28E-09	4.7E-06	3.89E-14	1.49E-13	2.98E-12
			$\sum_j P\langle n_{a\tau}   n_j \rangle * P\langle n_j \rangle =$ 0.261		$\sum_j n_j P\langle n_j   n_{a\tau} \rangle = 3,6$

# Accuracy of the Bayesian adjustment for the Rotterdam planning region: 21 days ahead (average over $\tau$ )

Accuracy Bayesian technique Rotterdam

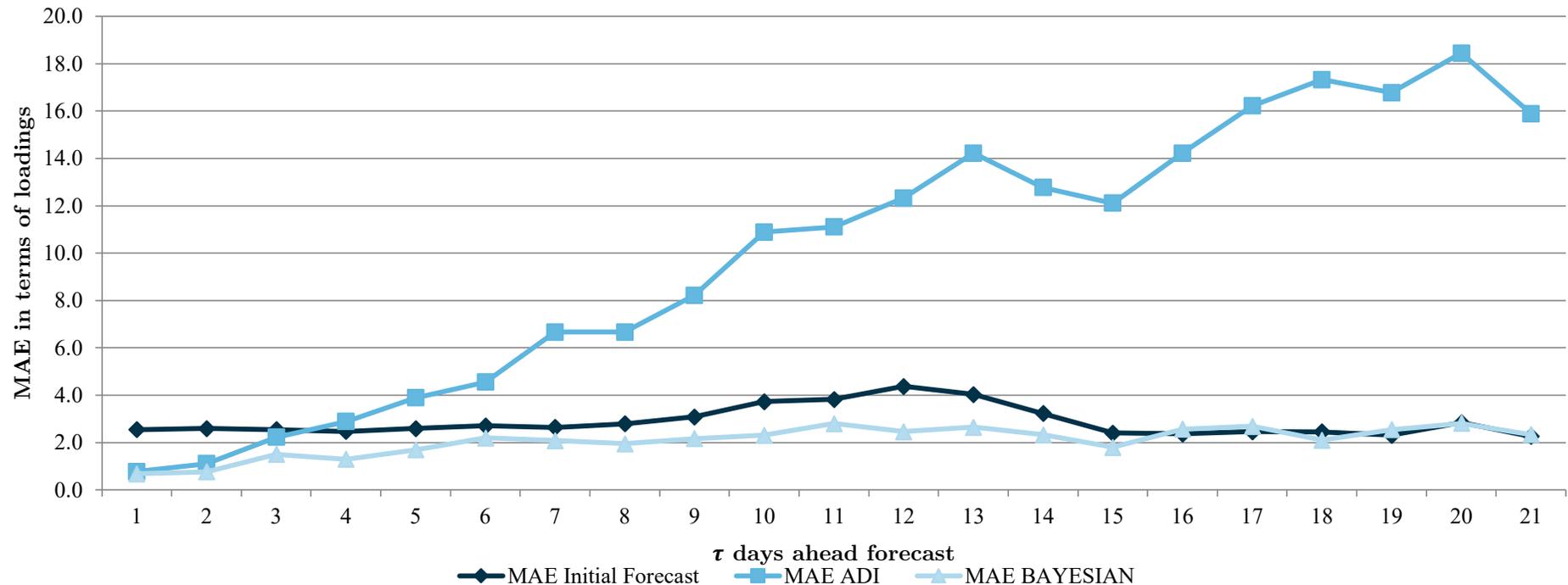
Accuracy averaged over $\tau$	
Method	Mean Absolute Error
Initial forecast	2.87
Only using advance demand information	9.97
Bayesian adjustment	2.08



# Accuracy of the Bayesian adjustment for the Rotterdam planning region: 21 days ahead

Accuracy Bayesian technique Rotterdam

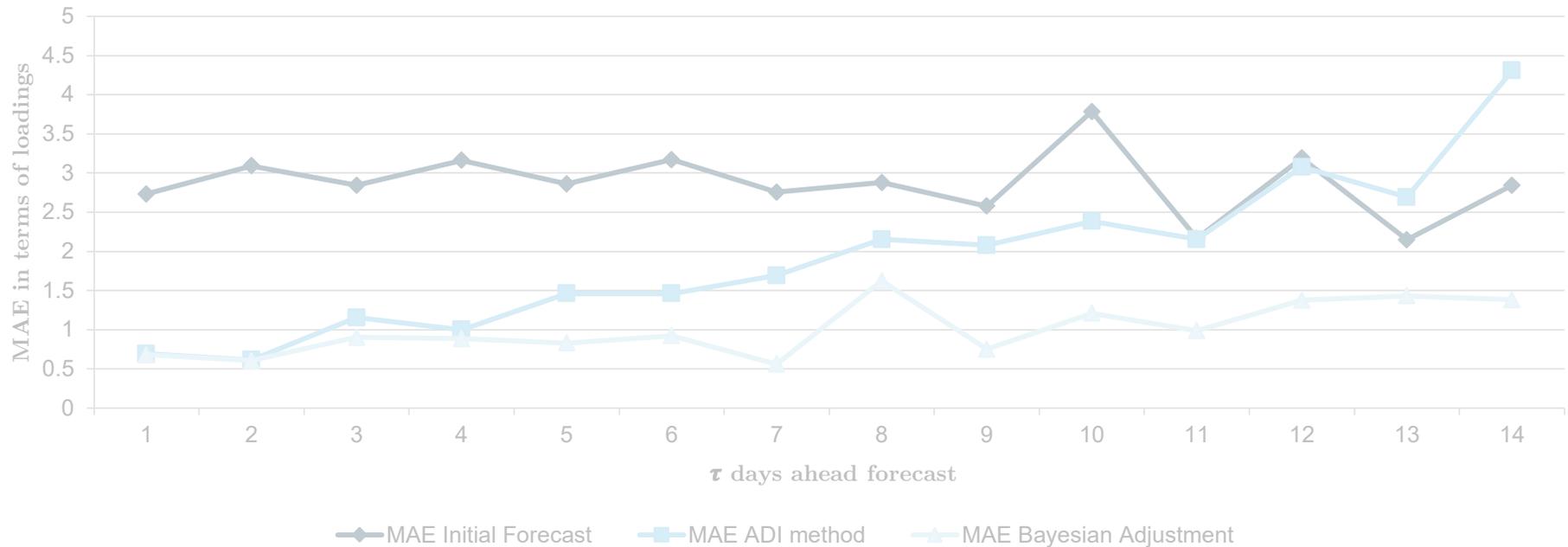
Accuracy averaged over $\tau$	
Method	Mean Absolute Error
Initial forecast	2.87
Only using advance demand information	9.97
Bayesian adjustment	2.08



# Accuracy of the Bayesian adjustment for the Belgium / France planning region: 21 days ahead (average over $\tau$ )

Accuracy Bayesian technique Belgium and Northern France

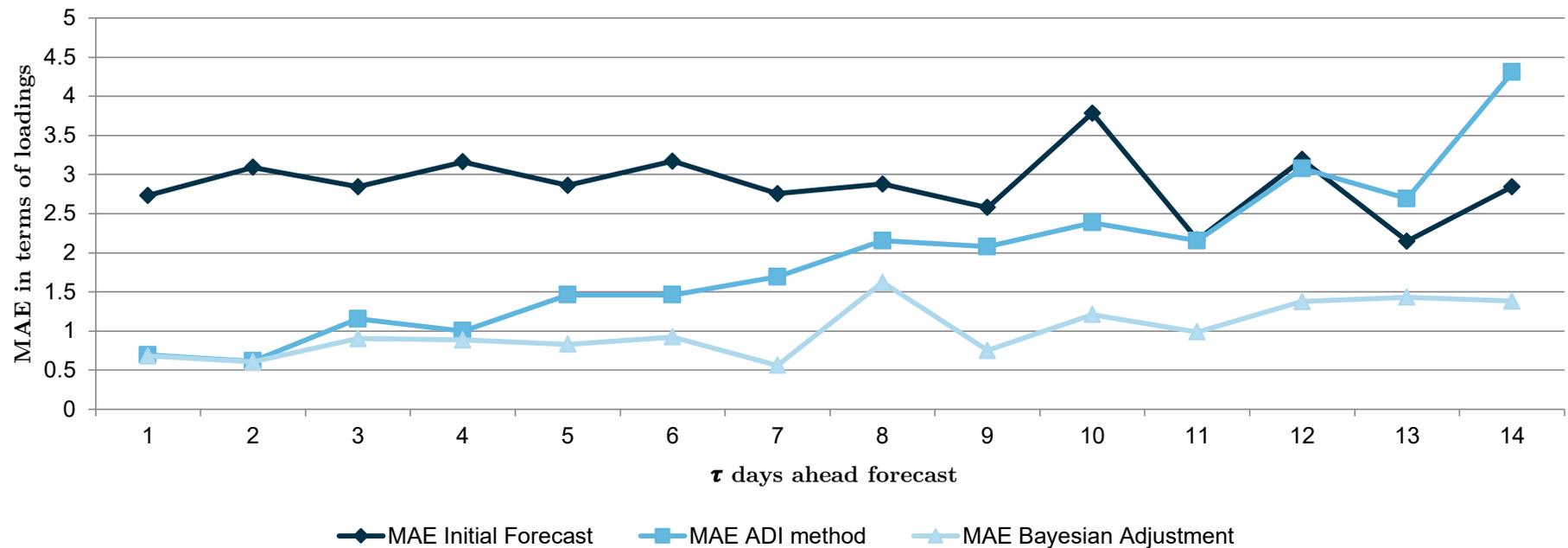
Accuracy averaged over $\tau$	
Method	Mean Absolute Error
Initial forecast	2.87
Only using advance demand information	1.92
Bayesian adjustment	1.01



# Accuracy of the Bayesian adjustment for the Belgium / France planning region: 21 days ahead

Accuracy Bayesian technique Belgium and Northern France

Accuracy averaged over $\tau$	
Method	Mean Absolute Error
Initial forecast	2.87
Only using advance demand information	1.92
Bayesian adjustment	1.01



# Using the Advance Demand Information

## *Method 2: The Combined Forecast*

### Combined Forecast

$\alpha$

Initial forecast  
from historical  
data

+ (1- $\alpha$ )

Forecast from  
inflater algorithm:

$$\frac{n_{a\tau}}{\theta_{\tau}}$$

The inflator algorithm utilizes advance demand information in a very easy and intuitive manner, but its variability increases if we forecast longer ahead

*Inflator algorithm*

## Inflator algorithm

Notation

$$\text{Forecast} = \frac{n_{a\tau}}{\theta_\tau}$$

Example

- 18 loadings in the system for 5 days in advance (i.e.  $n_{a\tau} = 18$ )
- Probability that a loading for 5 days in the future is already known at present is 50% (i.e.  $\theta_5 = 50\%$ )

---

Inflator algorithm forecast:  $18/50\% = 36$  loadings

(dis)advantages

- + Very easy and intuitive way to use the advance demand information
- Variability increases and accuracy decreases if we derive a forecast for longer in the future

# The inflator algorithm utilizes advance demand information in a very easy and intuitive manner, but its variability increases if we forecast longer ahead

*Inflator algorithm*

## Inflator algorithm

Notation

$$\text{Forecast} = \frac{n_{a\tau}}{\theta_\tau}$$

Example

- 18 loadings in the system for 5 days in advance (i.e.  $n_{a\tau} = 18$ )
- Probability that a loading for 5 days in the future is already known at present is 50% (i.e.  $\theta_5 = 50\%$ )

---

Inflator algorithm forecast:  $18/50\% = 36$  loadings

(dis)advantages

- + Very easy and intuitive way to use the advance demand information → for this reason used in practice
- Variability increases and accuracy decreases if we derive a forecast for longer in the future



# The combined forecast can be considered as an alternative to the more complex Bayesian adjustment

*Combined Forecast*

## Combined Forecast

Initial forecast  
based on  
historical data:

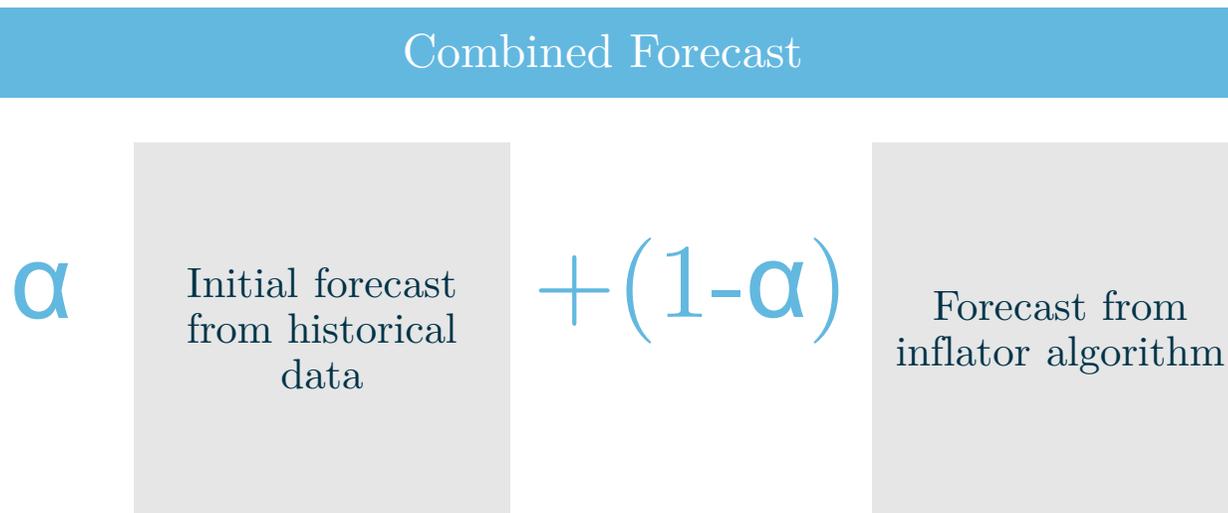
*e.g. the Simple  
mean method!*

Inflator algorithm:

$$\frac{n_{a\tau}}{\theta_\tau}$$

# The combined forecast can be considered as an alternative to the more complex Bayesian adjustment

*Combined Forecast*

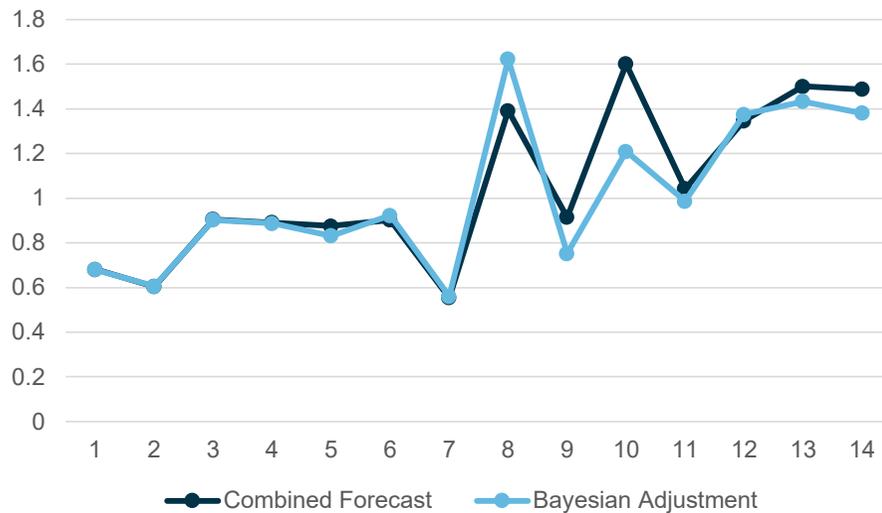


- The Combined Forecast utilizes both the initial forecast and the inflator algorithm
- The values of  $\alpha$  should increase for larger values of  $\tau$

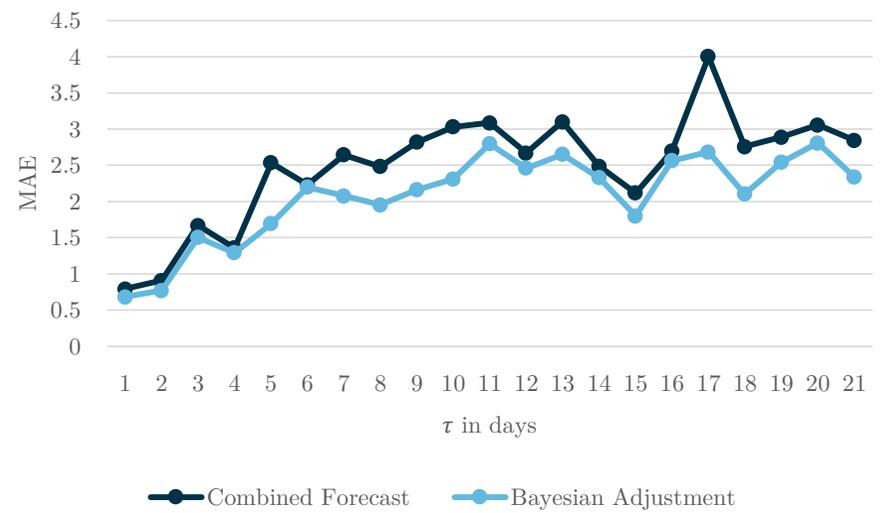
# Accuracy of the Combined Forecast as a function of tau

Method	MAE Belgium and North France loadings	MAE Rotterdam loadings
Initial Forecast	2.87	2.87
Bayesian Algorithm	1.01	2.08
Combined Forecast	1.05	2.50

BFN planning region

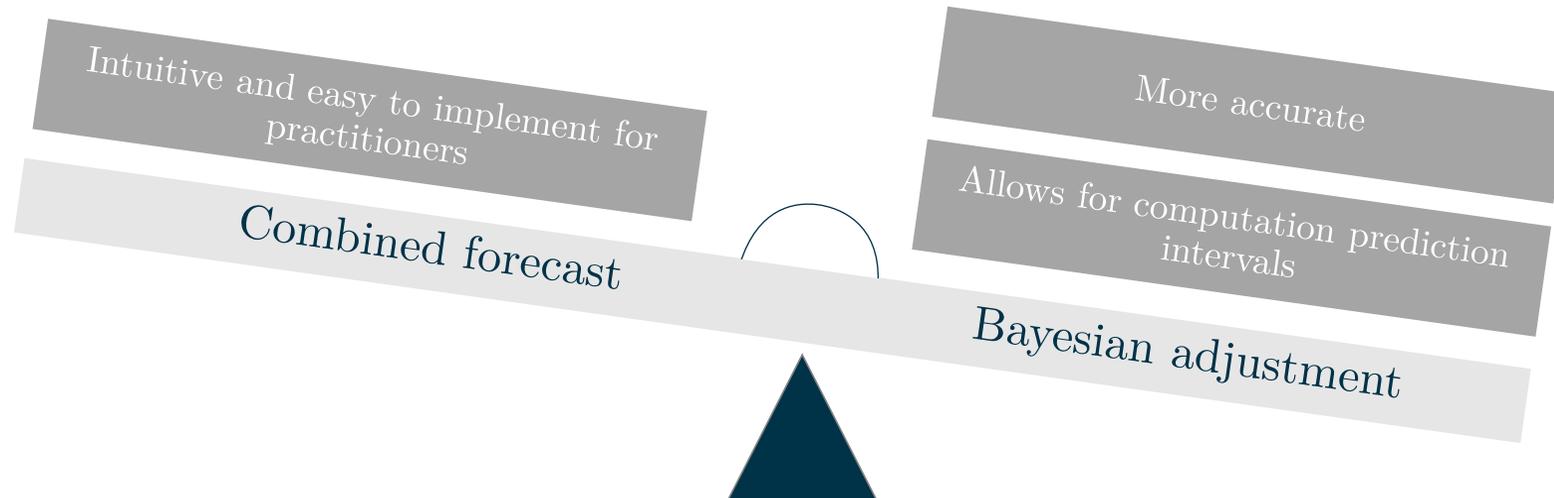


Rotterdam planning region



# Although more complex, the Bayesian adjustment might still be preferable over the combined forecast

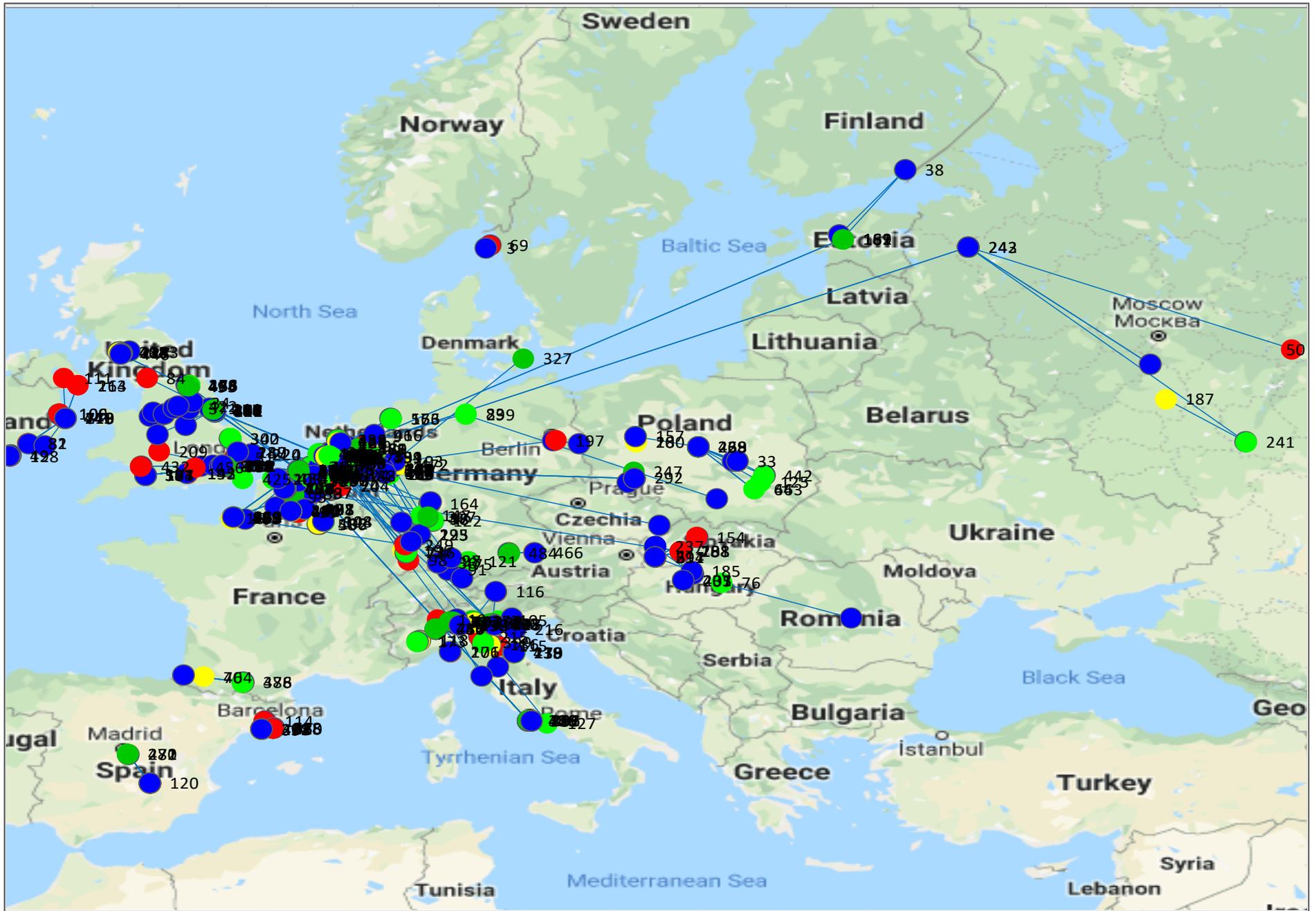
*Combined forecast vs. Bayesian adjustment*



Currently, the Bayesian model is being implemented by CQM

# APPENDIX C

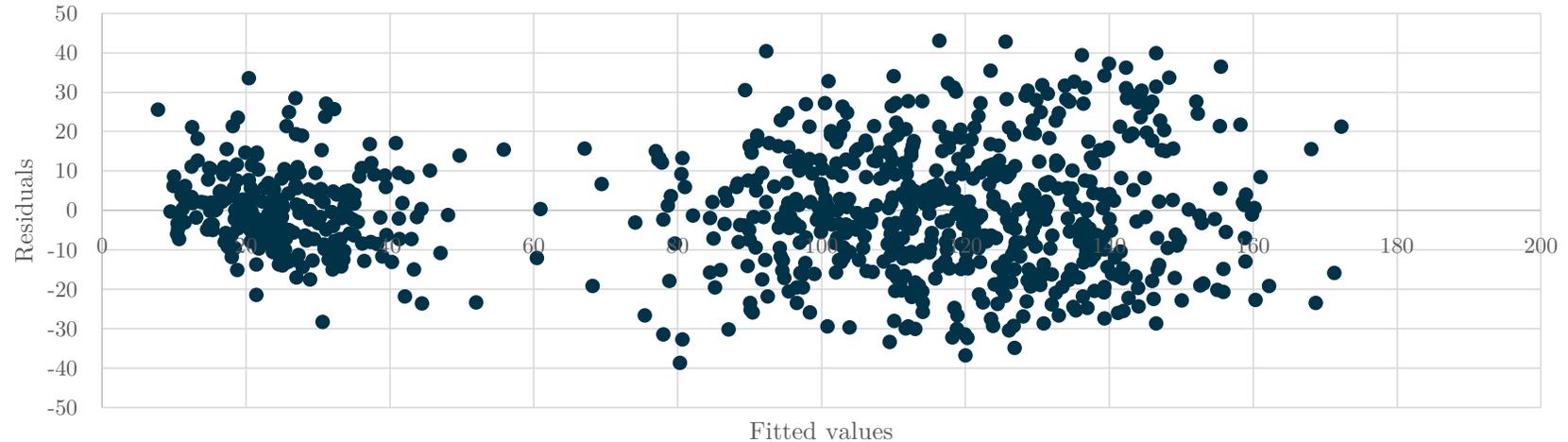
## *Trucking capacity*



All trucking actions 24/07/2019

# A Box Cox transformation was used to resolve the heteroscedasticity of the residuals

*Box Cox transformation*



Box Cox transformation

$$w_t = \begin{cases} \ln(\delta_t) & \text{if } \lambda = 0; \\ \frac{\delta_t^\lambda - 1}{\lambda} & \text{otherwise.} \end{cases}$$

Reverse Box Cox transformation

$$\delta_t = \begin{cases} \exp(w_t) & \text{if } \lambda = 0; \\ (\lambda w_t + 1)^{\frac{1}{\lambda}} & \text{otherwise.} \end{cases}$$

# Output multiple linear regression models GBN and BFN planning regions

*Parameters multiple linear regression*

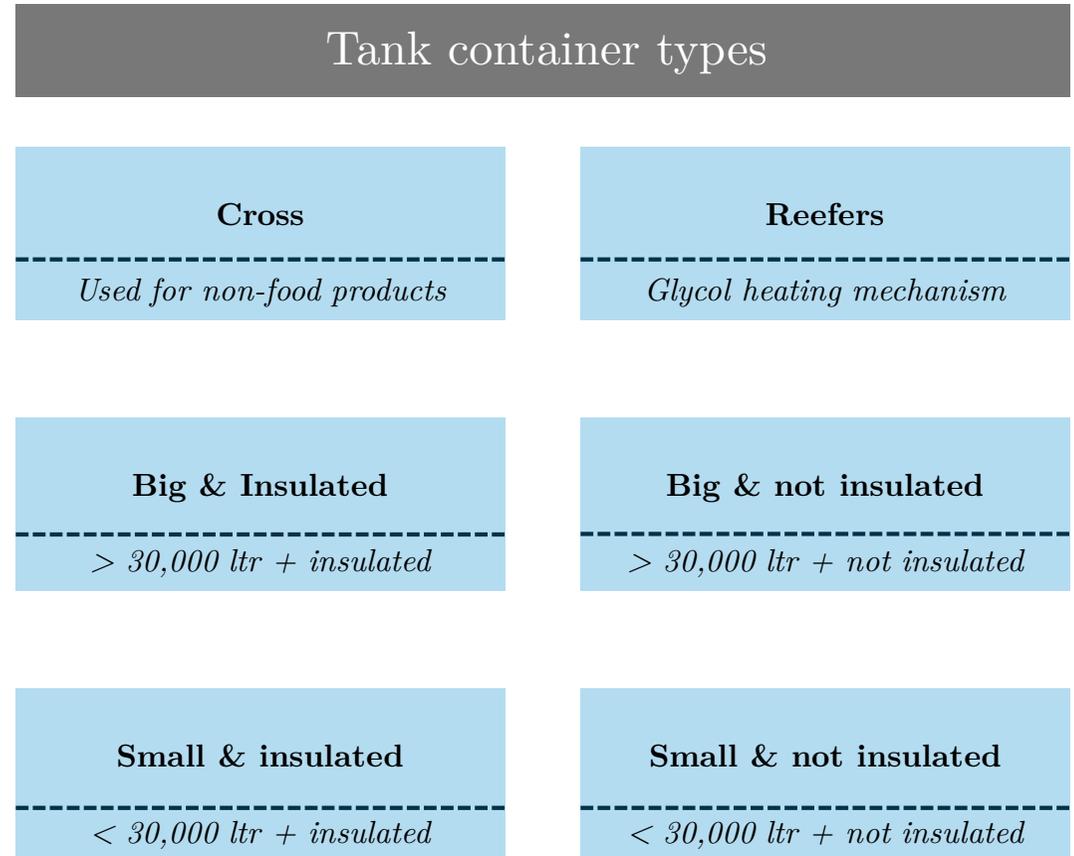
BFN region	Corresponding explanatory variable	Coefficient	Standard error	p-value	GBN region	Coefficient	Standard error	p-value
$\beta_0$	Intercept	-0.345	0.185	0.063	$\beta_0$	9.158	1.514	< 0,0001
$\beta_1$	$Lo(\tau)$	0.358	0.021	< 0,0001	$\beta_1$	0.822	0.252	0.001
$\beta_2$	$De(\tau)$	0.280	0.032	< 0,0001	$\beta_2$	2.197	0.124	< 0,0001
$\beta_3$	$Lo_D(\tau)$	0.116	0.021	< 0,0001	$\beta_3$	1.415	0.250	< 0,0001
$\beta_4$	$De_D(\tau)$	0.186	0.032	< 0,0001	$\beta_4$	2.220	0.127	< 0,0001
$\beta_5$	$\delta(\tau - 14)$	0.007	0.002	0.003	$\beta_5$	0.094	0.019	< 0,0001
$\beta_6$	$\delta(\tau - 28)$	0.004	0.002	0.113	$\beta_6$	0.088	0.019	< 0,0001
$\beta_7$	$x_1(\tau)$	10.416	0.512	< 0,0001	$\beta_7$	14.242	3.027	< 0,0001
$\beta_8$	$x_2(\tau)$	10.532	0.555	< 0,0001	$\beta_8$	5.070	3.172	0.110
$\beta_9$	$x_3(\tau)$	9.956	0.531	< 0,0001	$\beta_9$	5.512	3.253	0.091
$\beta_{10}$	$x_4(\tau)$	9.989	0.559	< 0,0001	$\beta_{10}$	8.235	3.091	0.008
$\beta_{11}$	$x_5(\tau)$	9.659	0.520	< 0,0001	$\beta_{11}$	6.546	2.695	0.015
$\beta_{12}$	$x_6(\tau)$	3.924	0.235	< 0,0001	$\beta_{12}$	-0.154	1.505	0.919
$\beta_{13}$	$x_7(\tau)$	-7.254	0.641	< 0,0001	$\beta_{13}$	-6.230	3.409	0.048
$\beta_{14}$	$x_8(\tau)$	-0.636	0.164	< 0,0001	$\beta_{14}$	-6.730	1.389	< 0,0001

# APPENDIX D

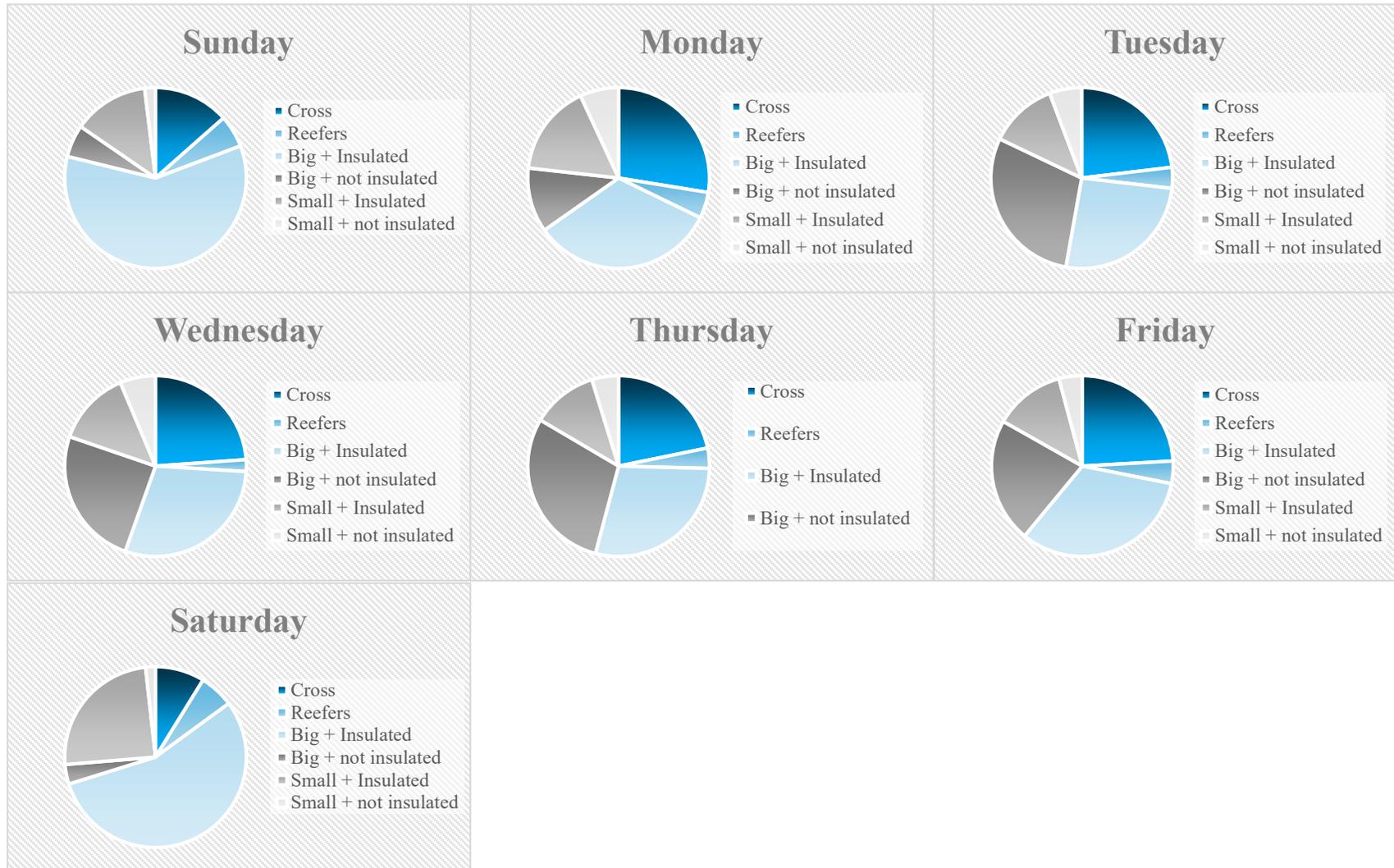
## *Tank container capacity*

# In consultation with the MMP department, six tank container types were defined

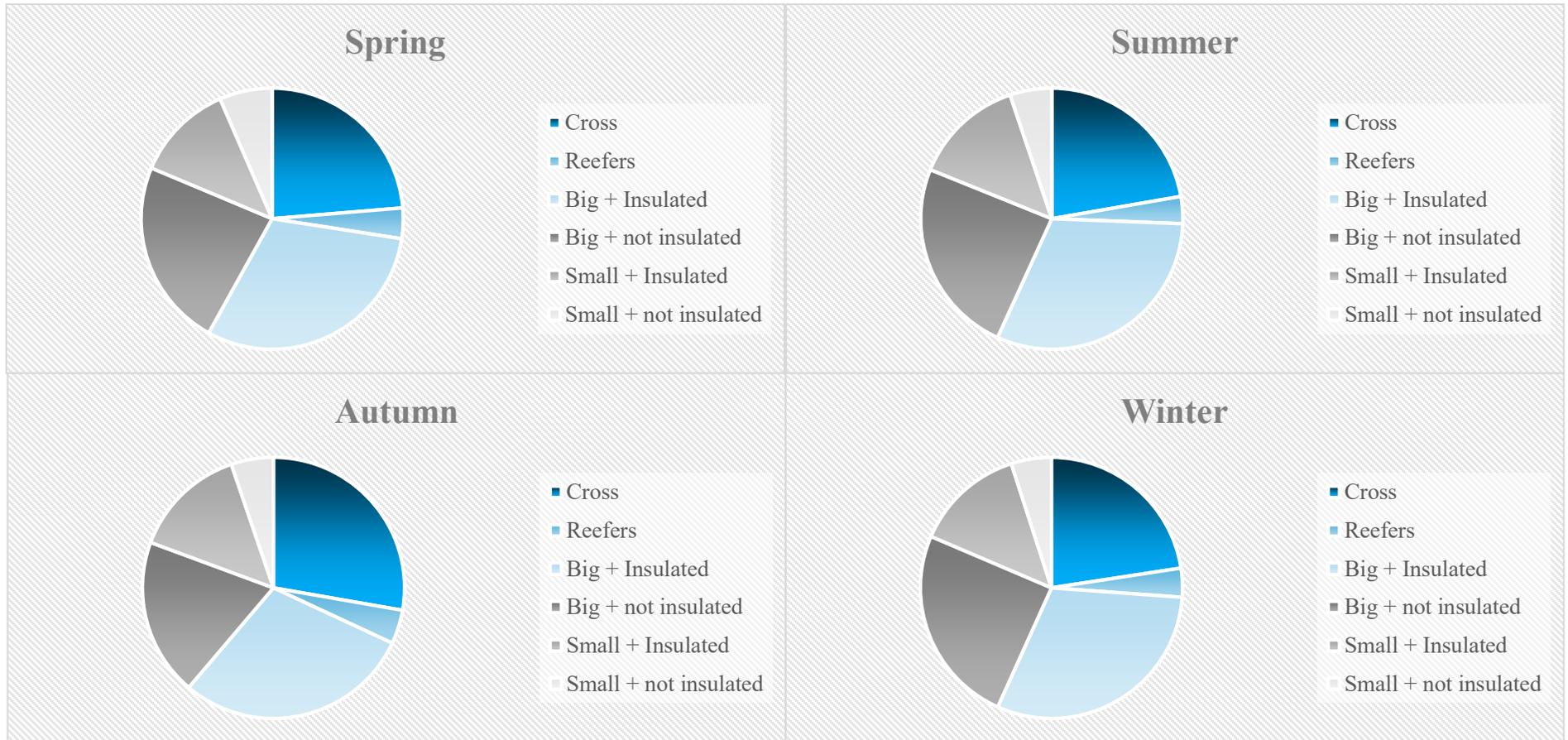
*Description of tank container fleet H&S*



# Day of the weak seasonality tank container use in the Rotterdam planning region

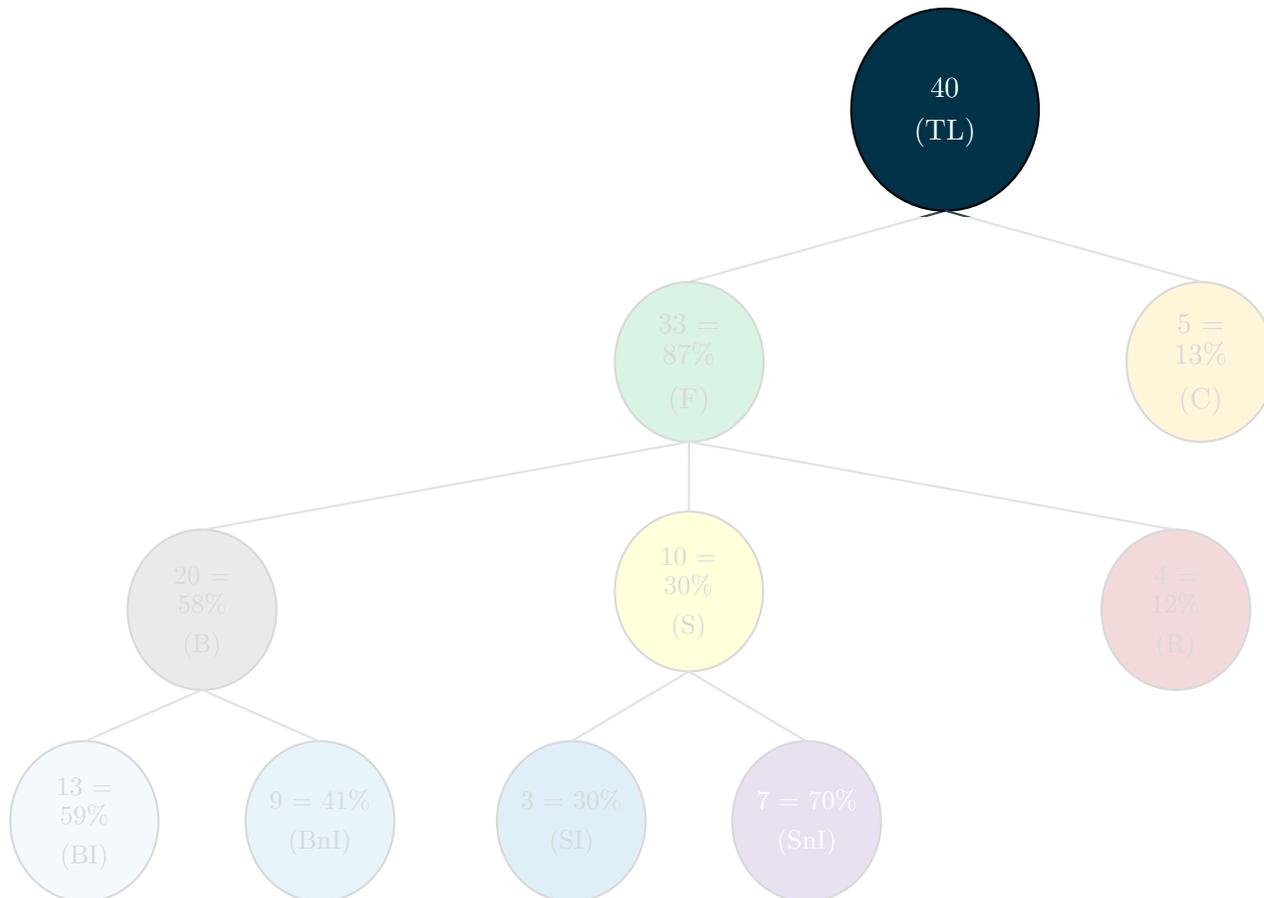


# Meteorological seasonality tank container use in the Rotterdam planning region

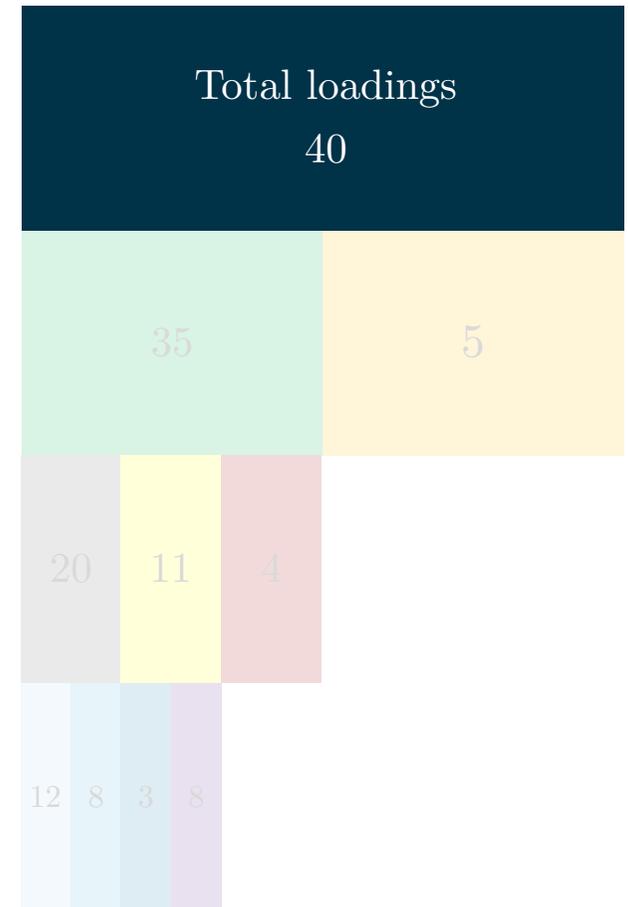


# Example: (1) predict the expected number of loadings → derived from the Bayesian technique

Forecast proportions for tank containers

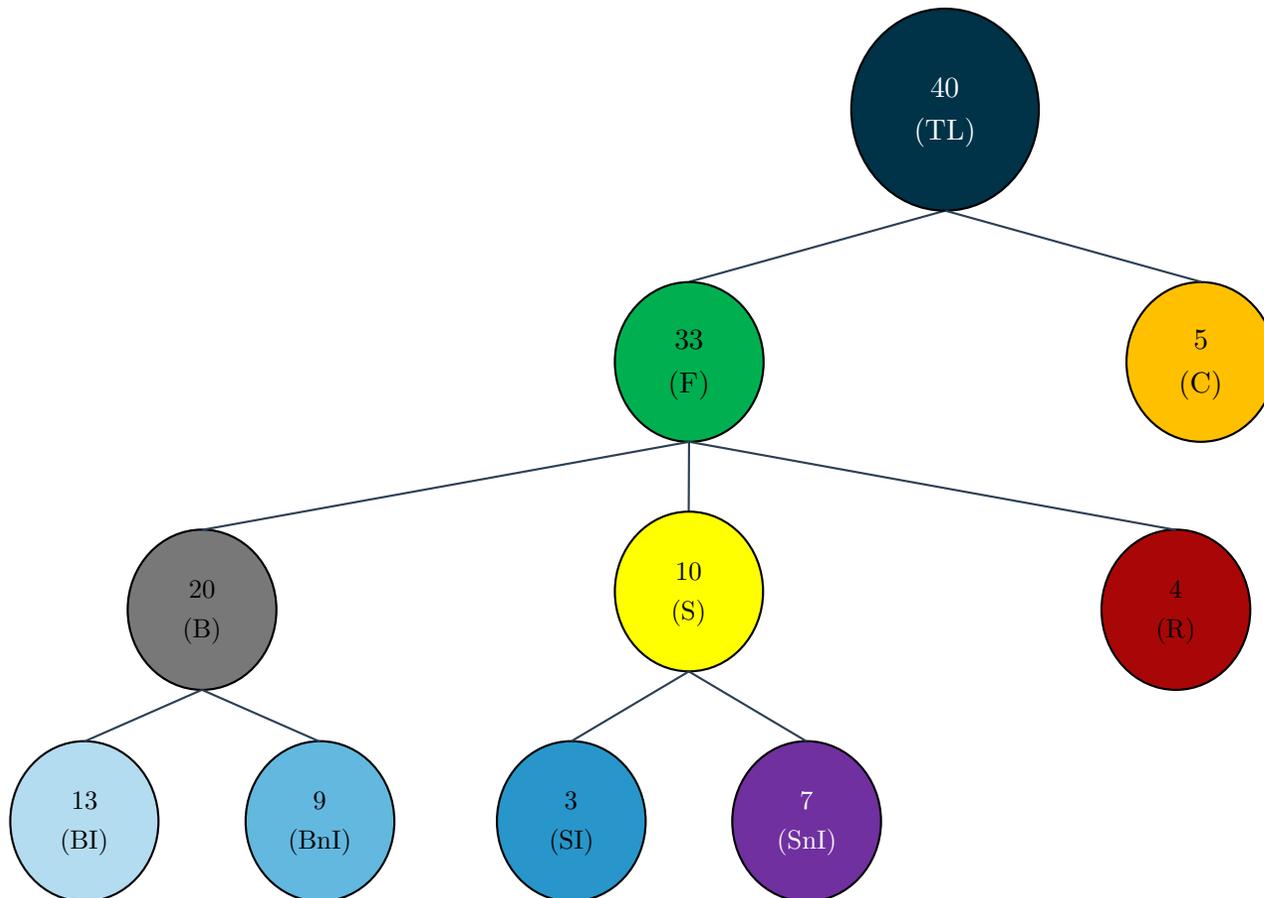


Final tank container forecast

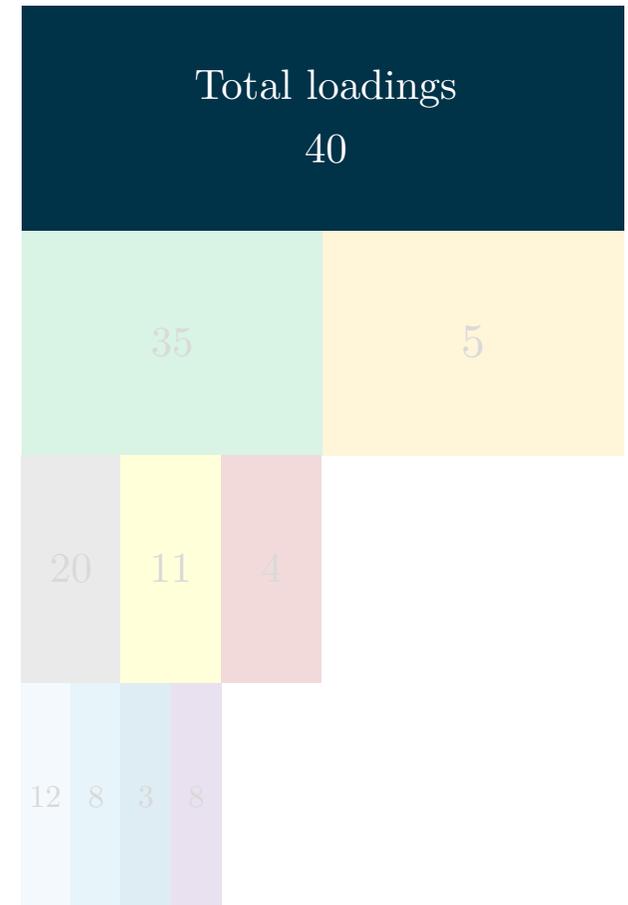


# Example: (2) Derive a forecast per container type (i.e. per aggregation level) and compute the forecasted proportions

Forecast proportions for tank containers

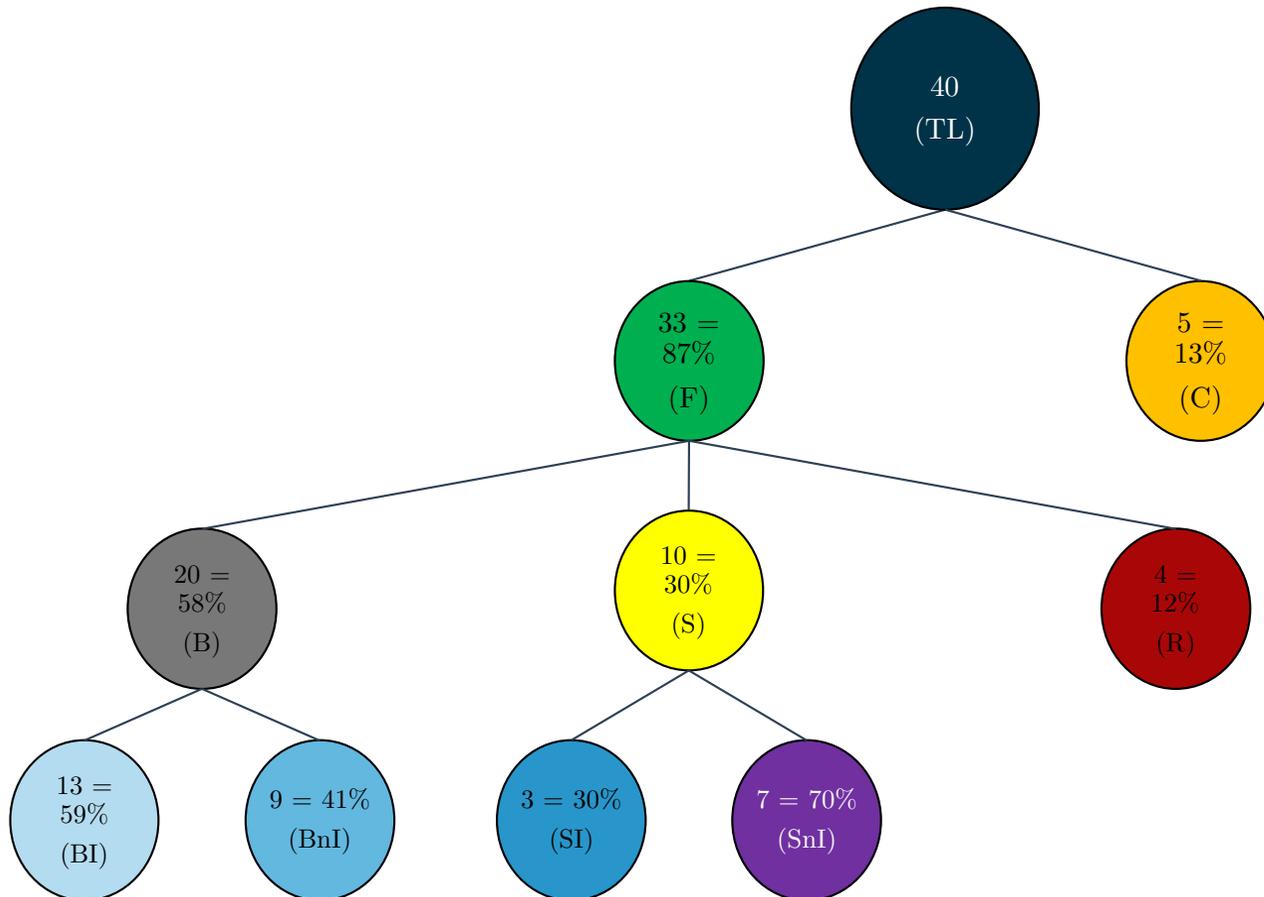


Final tank container forecast

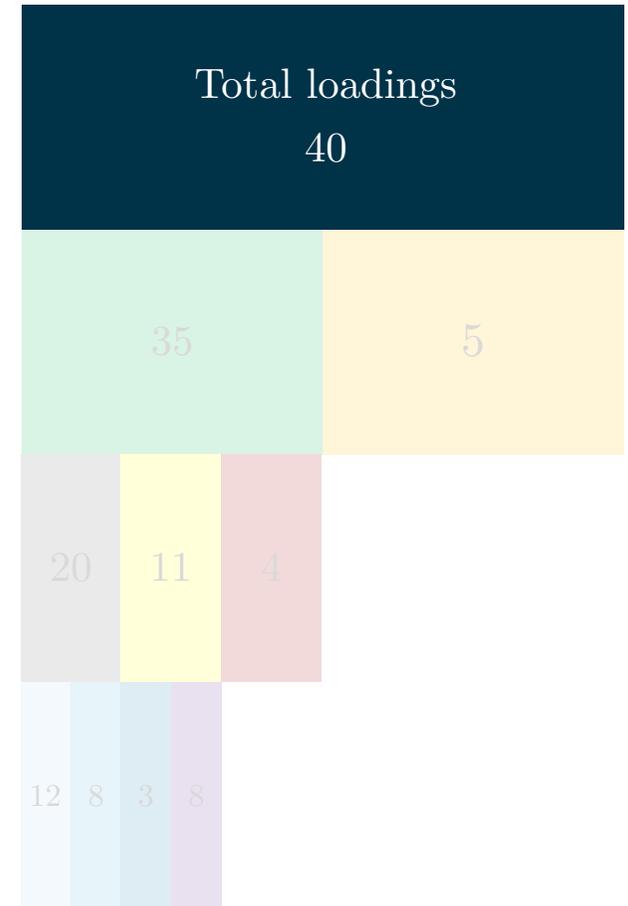


# Example: (2) Derive a forecast per container type (i.e. per aggregation level) and compute the forecasted proportions

Forecast proportions for tank containers

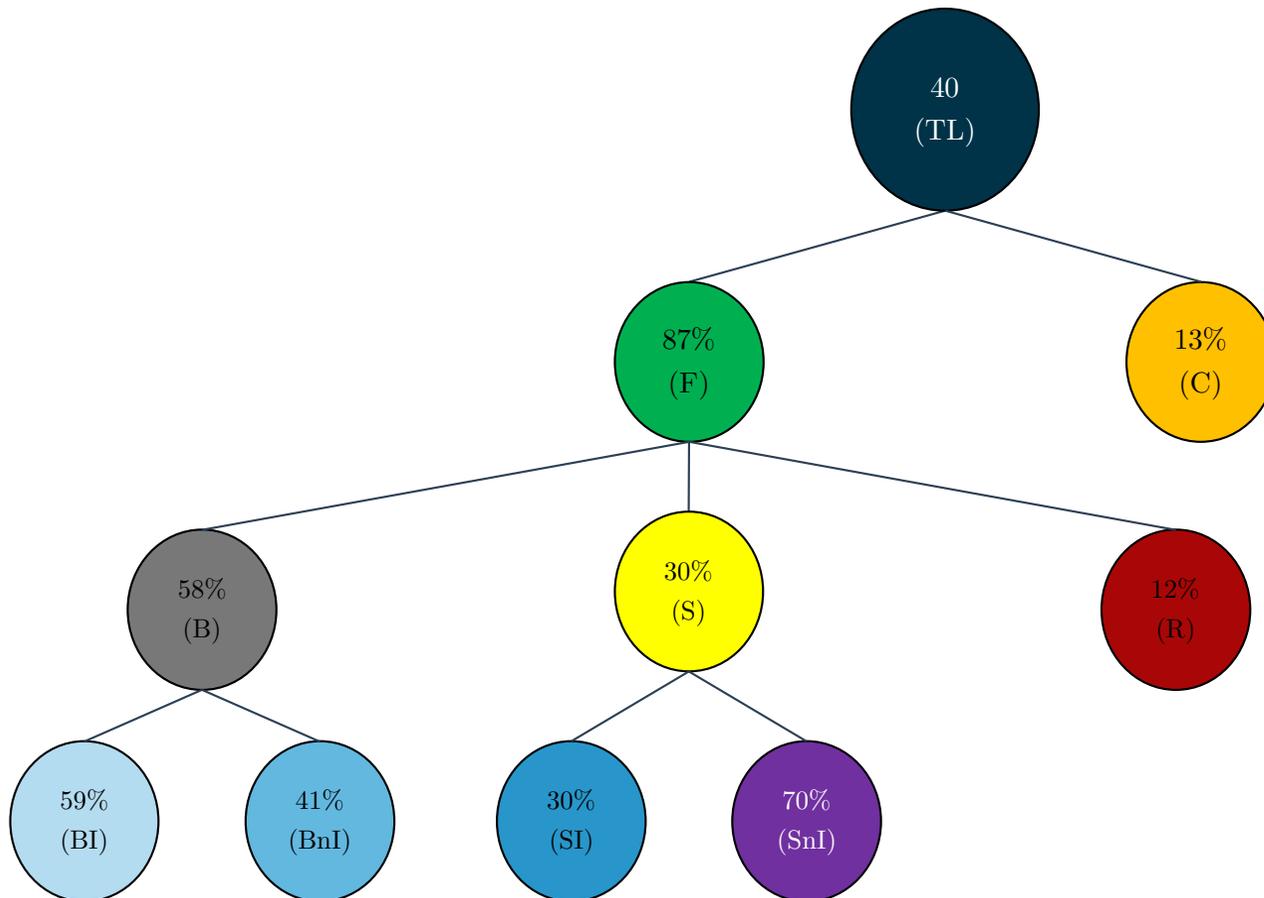


Final tank container forecast

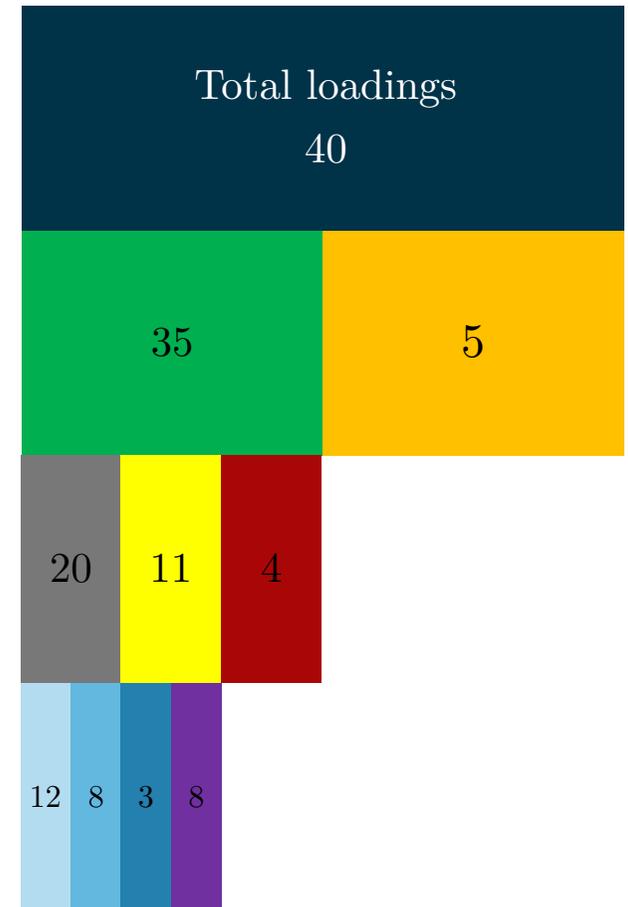


# Example: (3) Disaggregate the forecast of the total number of loadings down the hierarchy based on the forecasted proportions

Forecast proportions for tank containers



Final tank container forecast



# APPENDIX E

## *General*

# Challenge 1: proactive truck planning (i.e. drayage operations)

Operational challenges H&S



## Current truck planning

Occurs relatively ad hoc  
Charters booked at the very last moment → costly  
No smoothing of workload

## Truck planning in an *ideal* world

Truck planning should occur in a more **proactive** fashion:  
Book charters longer in advance  
Actively balancing workload

## What is needed to move to this *ideal* world?

Insight in the expected number of orders and the corresponding **trucking** capacity for a future time period



## Current container repositioning

Network imbalance → need to reposition empty containers  
Currently, repo decisions are made based on qualitative experience

## Container repo in an *ideal* world

Use the experience of the two planners but not rely on it exclusively  
Having a statistical model on which to base repositioning decisions

## What is needed to move to this *ideal* world?

Insight in the expected number of orders and the corresponding **tank container** capacity for a future time period

# Challenge 2: efficient empty tank container repositioning

Operational challenges H&S



## Current truck planning

Occurs relatively ad hoc  
Charters booked at the very last moment  
→ costly  
No smoothing of workload

## Truck planning in an *ideal* world

Truck planning should occur in a more **proactive** fashion:  
Book charters longer in advance  
Smooth workload

What is needed to move to this *ideal* world?

Insight in the expected number of orders and the corresponding **trucking** capacity for a future time period



## Current container repositioning

Network imbalance  
→ need to reposition empty containers  
Currently, repo decisions are made based on qualitative experience

## Container repo in an *ideal* world

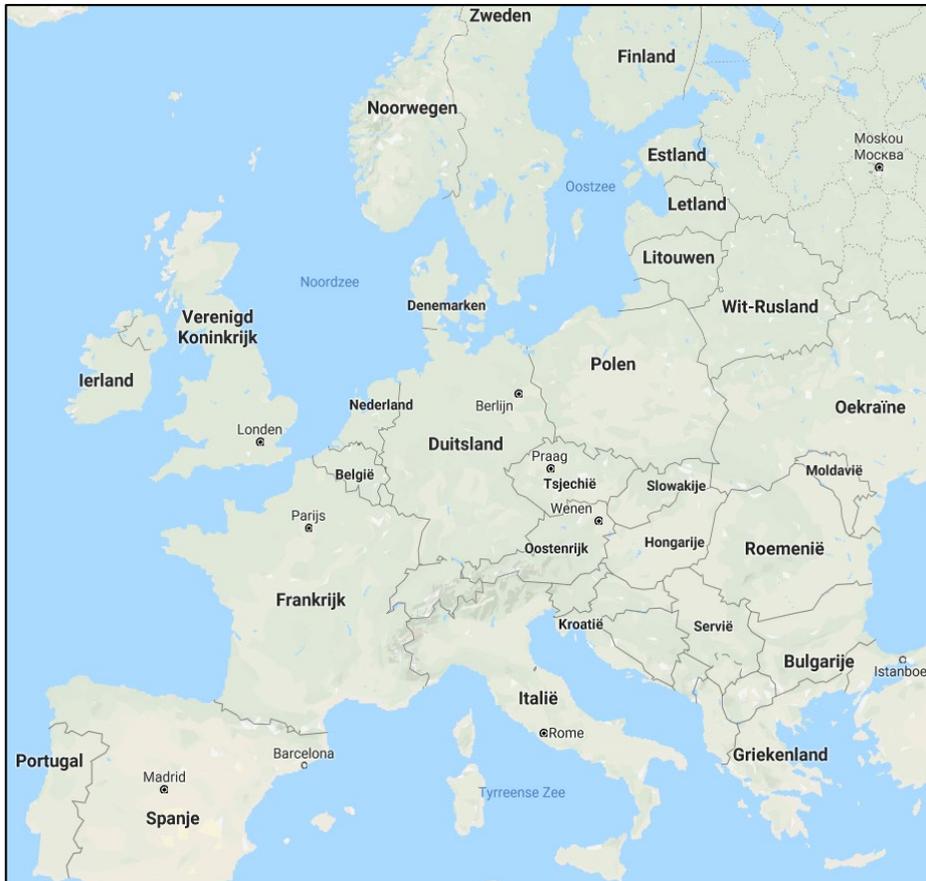
Use the experience of the two planners but not rely on it exclusively  
Having a statistical model on which to base repositioning decisions

What is needed to move to this *ideal* world?

Insight in the expected number of orders and the corresponding **tank container** capacity for a future time period

# In order to demarcate the scope of this research, three planning regions were selected to focus on

## Project deliverables and scope of the research



## Trucking capacity



### Focus regions:

- Belgium & northern part of France (**BFN**)
- Northern part of Great Britain (**GBN**)

### Forecast:

sub-daily (AM / PM)  
number of loadings and deliveries forecasted **1 week ahead**

## Tank container capacity



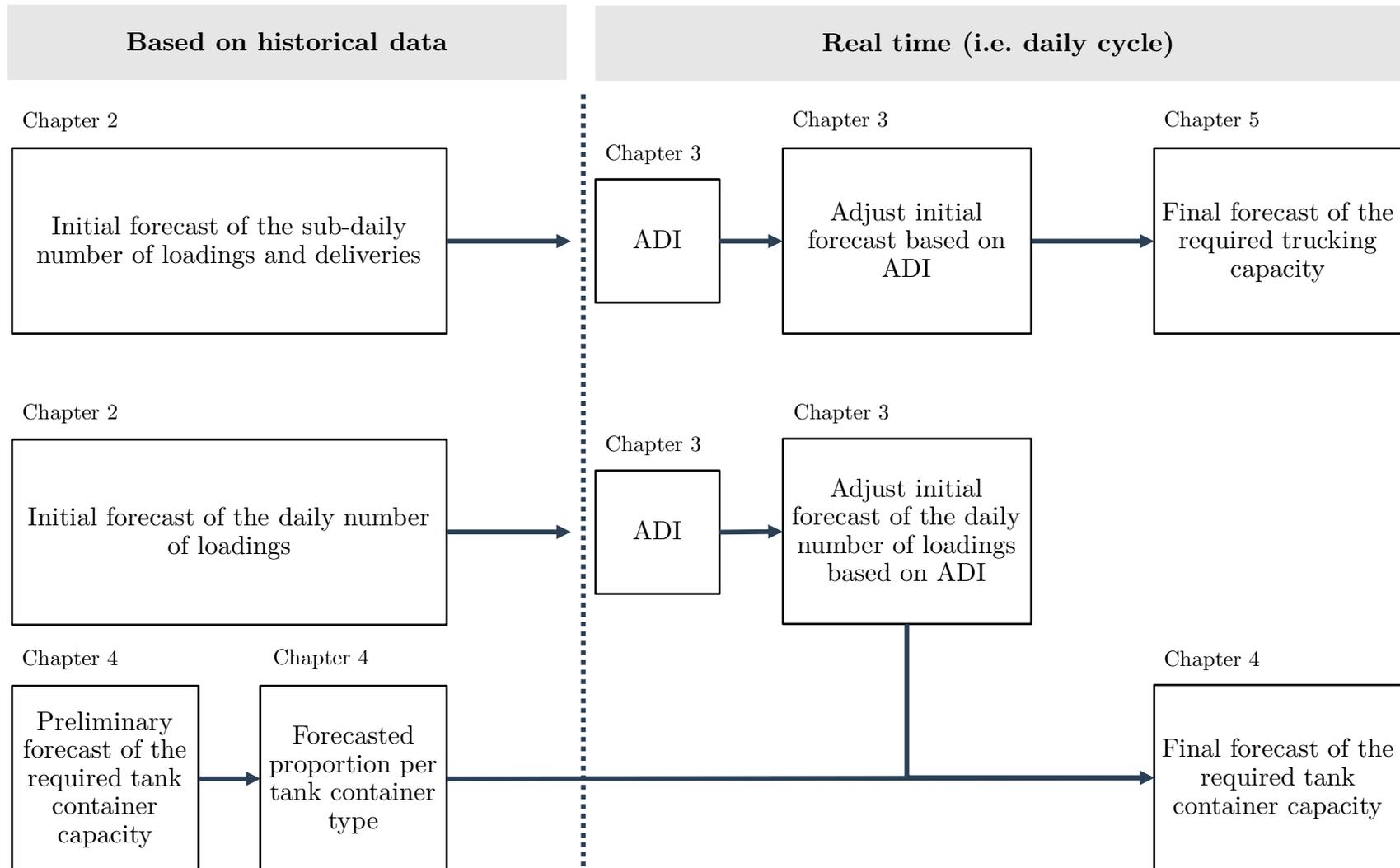
### Focus region:

- Rotterdam

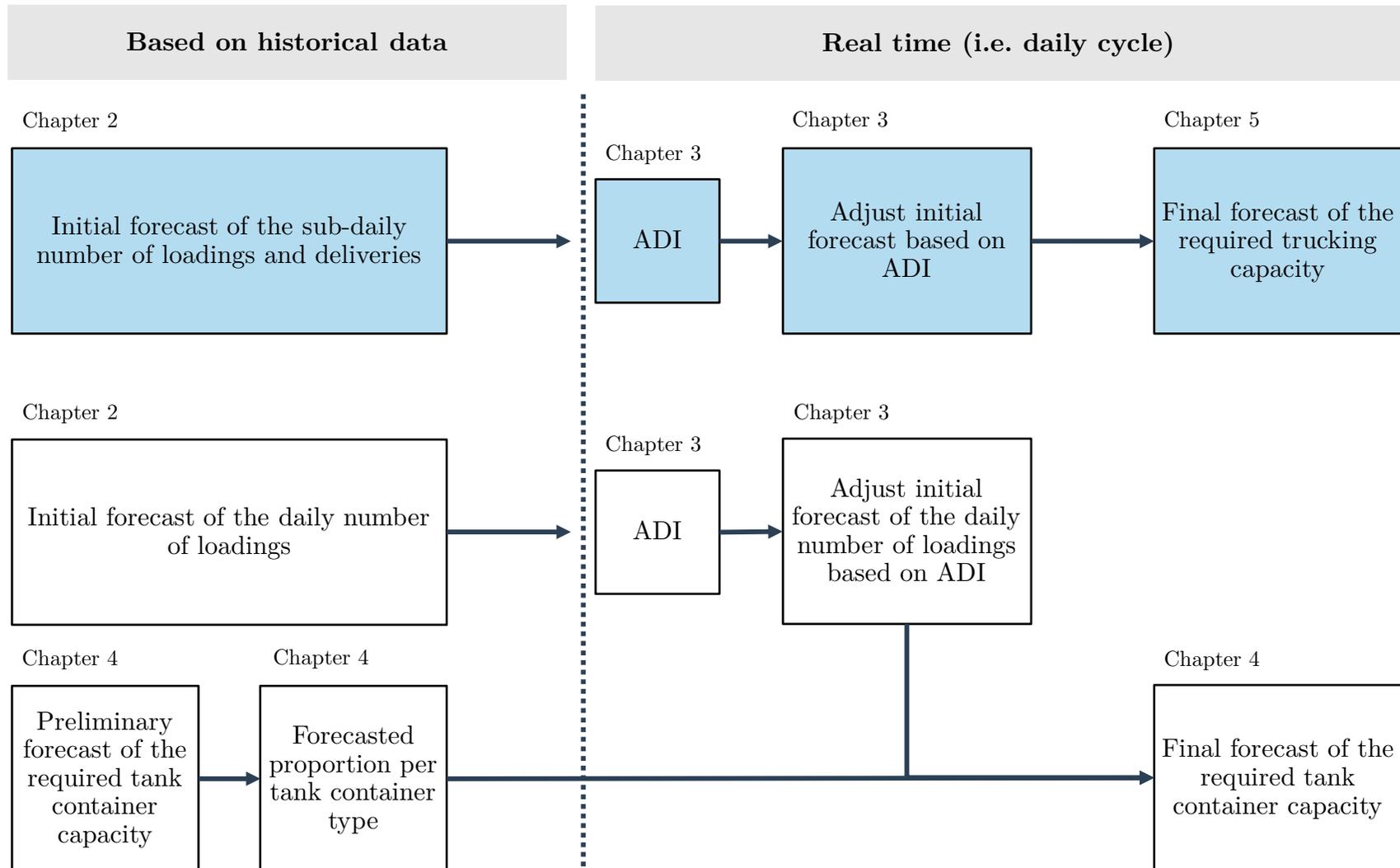
### Forecast:

daily number of loadings and deliveries forecasted **3 weeks ahead**

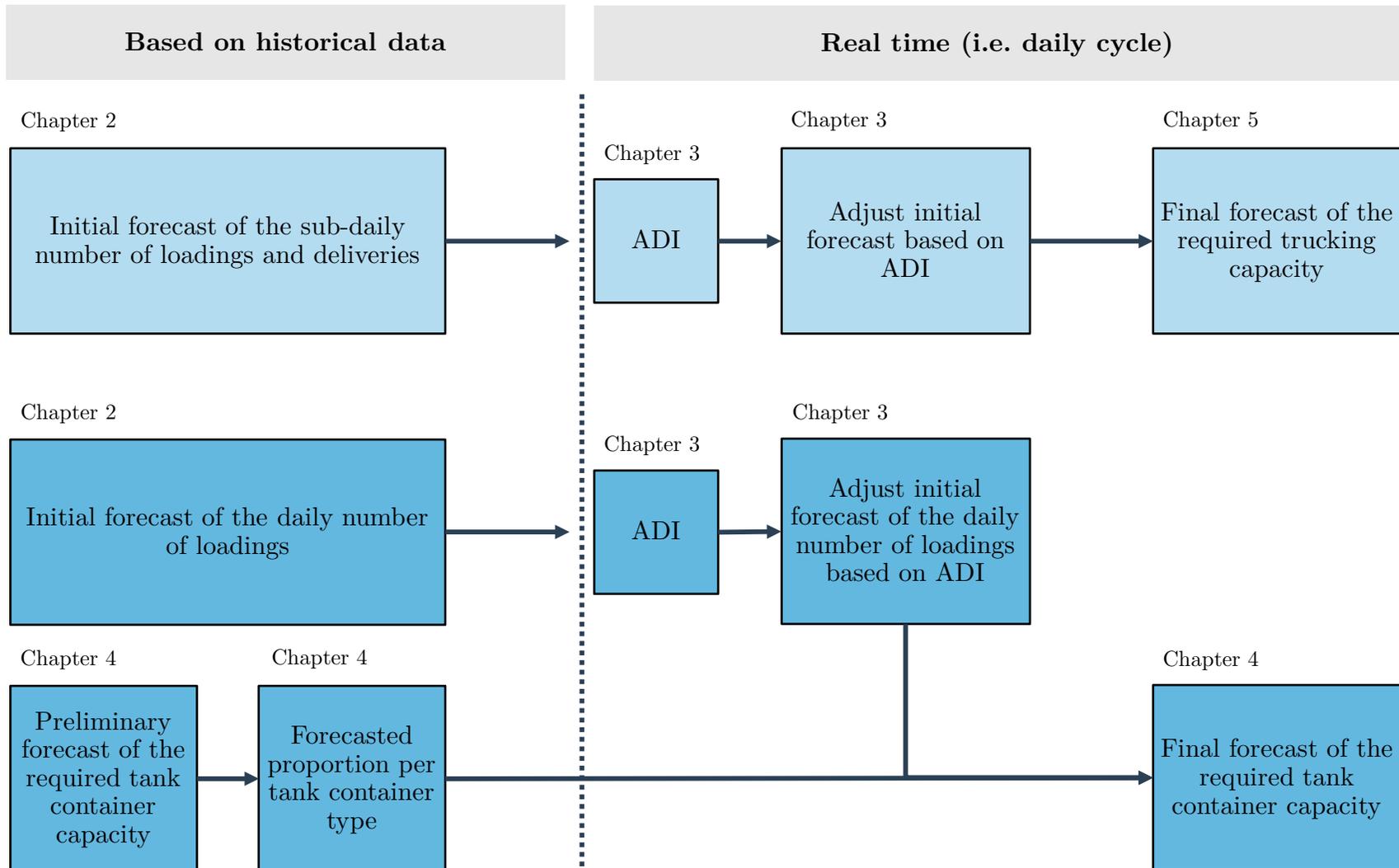
# Summary of the proposed forecasting methodology for predicting the number of orders and corresponding capacity requirements



# Summary of the proposed forecasting methodology for predicting the number of orders and corresponding capacity requirements

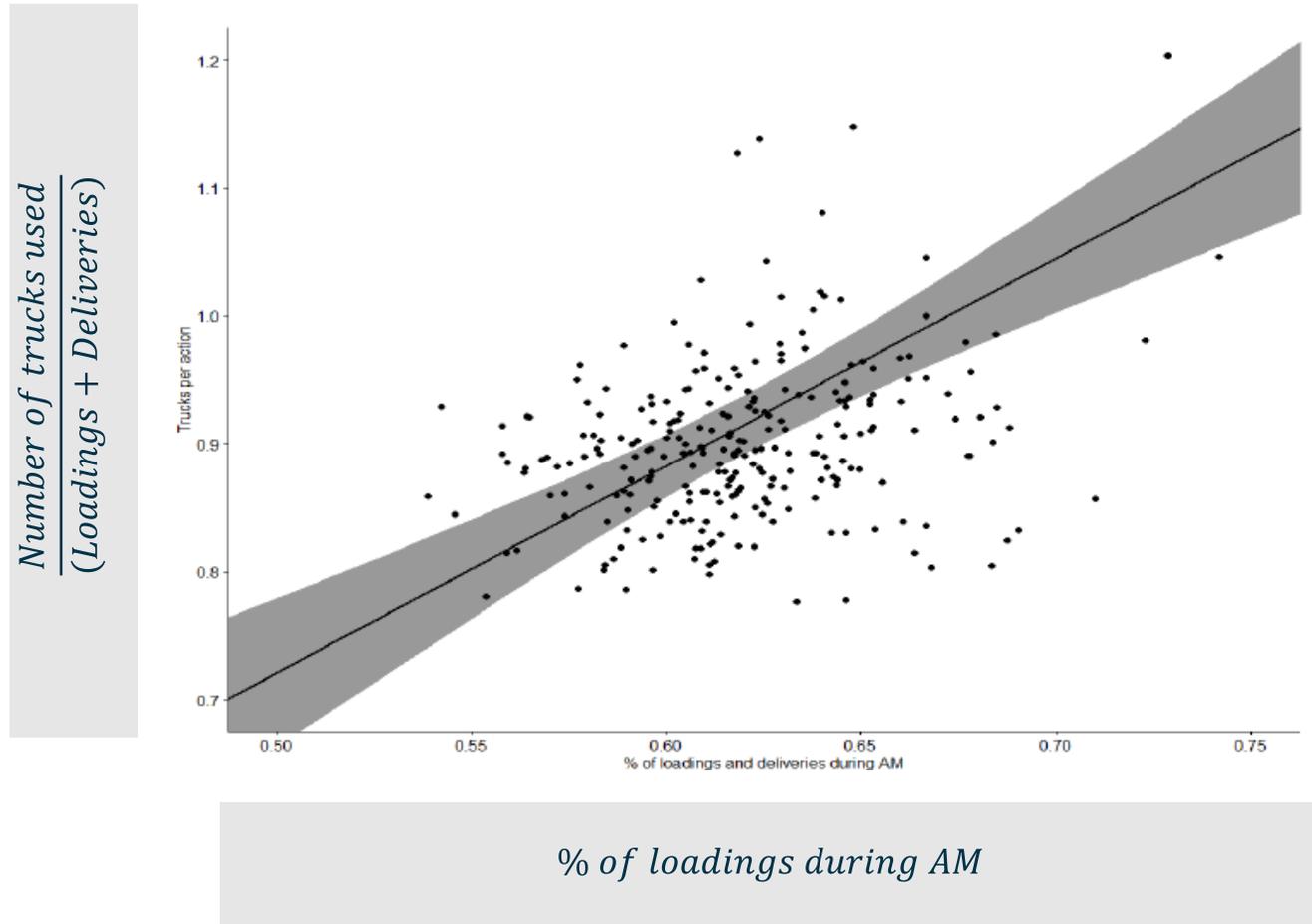


# Summary of the proposed forecasting methodology for predicting the number of orders and corresponding capacity requirements

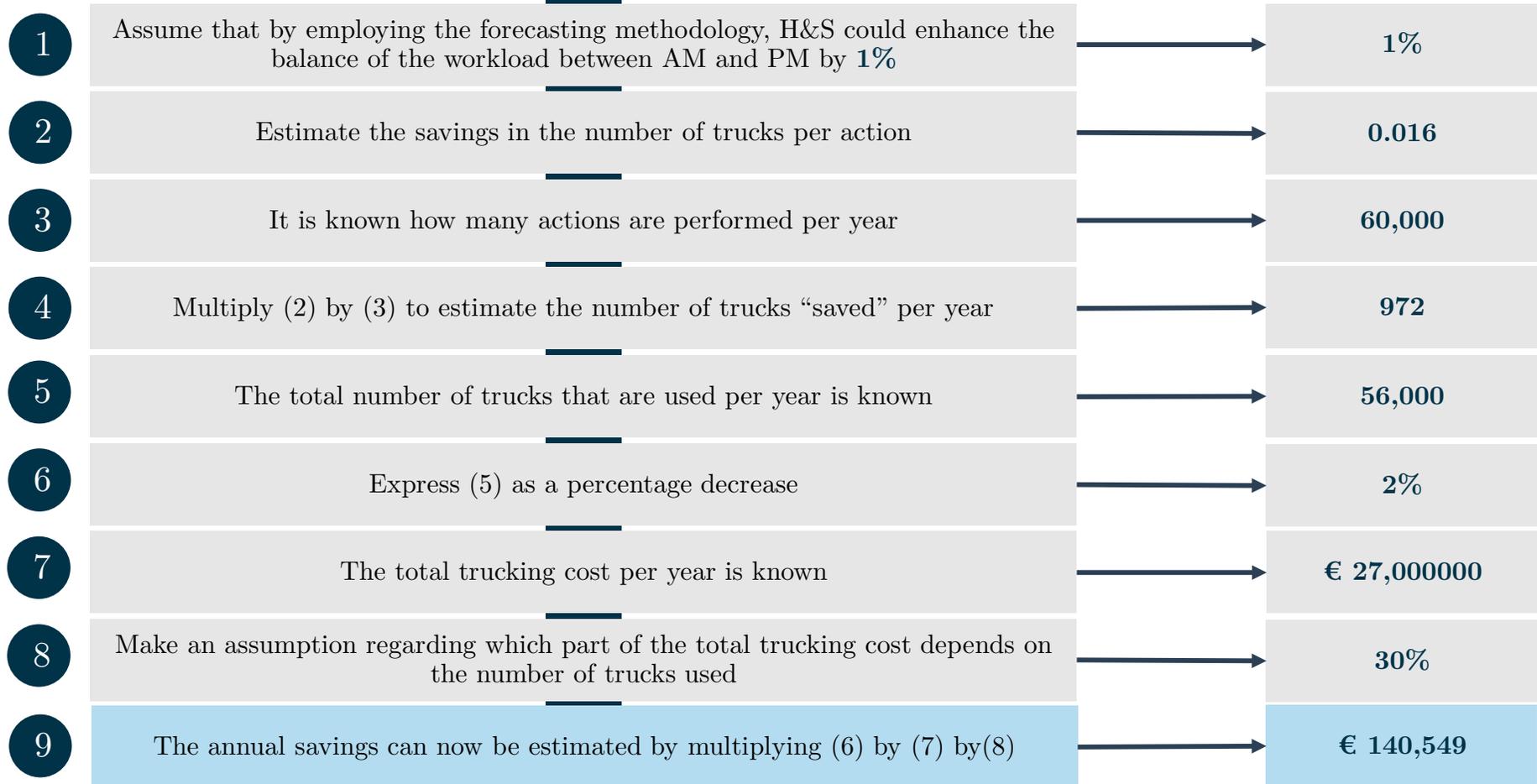


# There seems to be a correlation between the imbalance between AM & PM and the number of trucks per action on a given day

*Correlation between (im)balance and number of trucks per action*

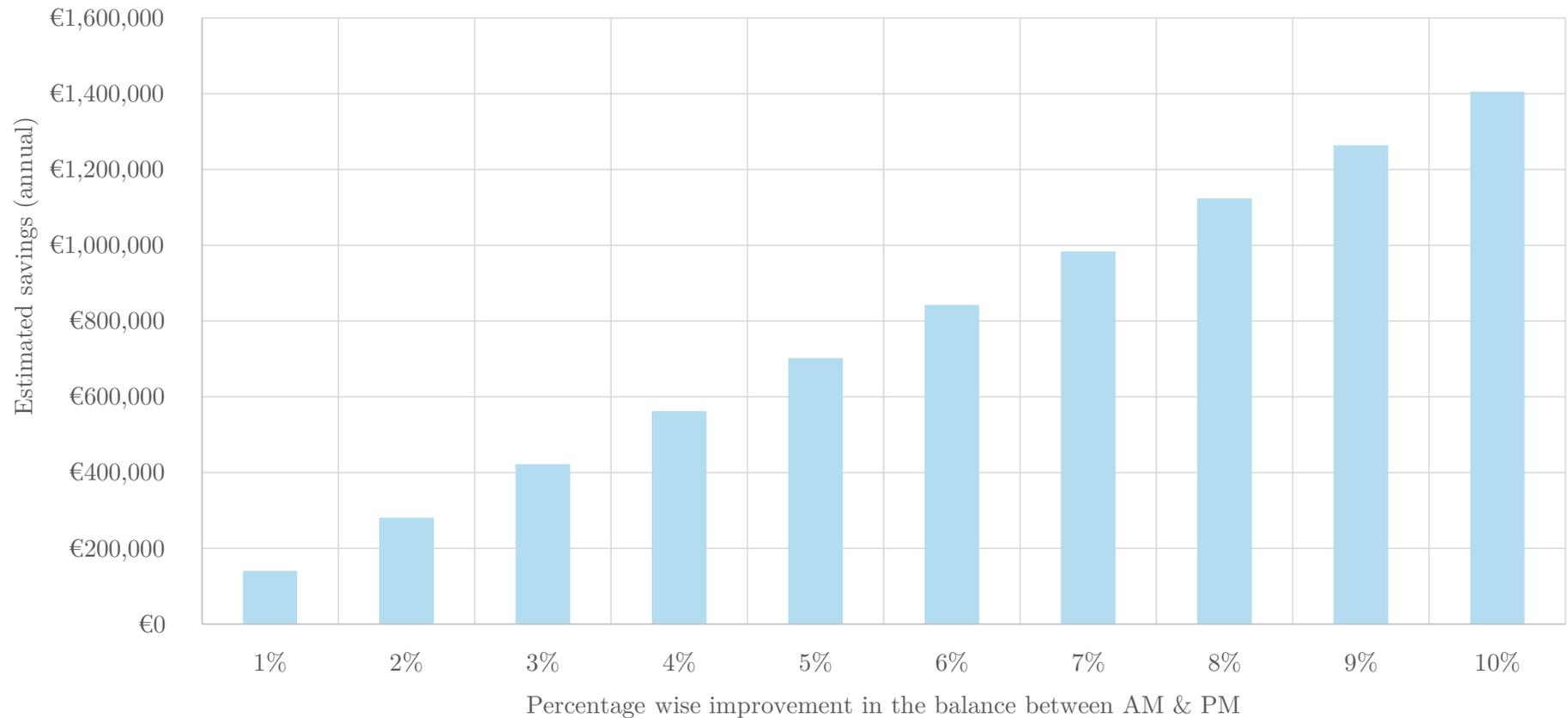


# A guesstimate was conducted to estimate the potential savings that might be expected if the balance between AM & PM would be improved



# By balancing the workload throughout the day it is expected that H&S can save a substantial amount of trucking costs

*Estimated savings for various scenario's*

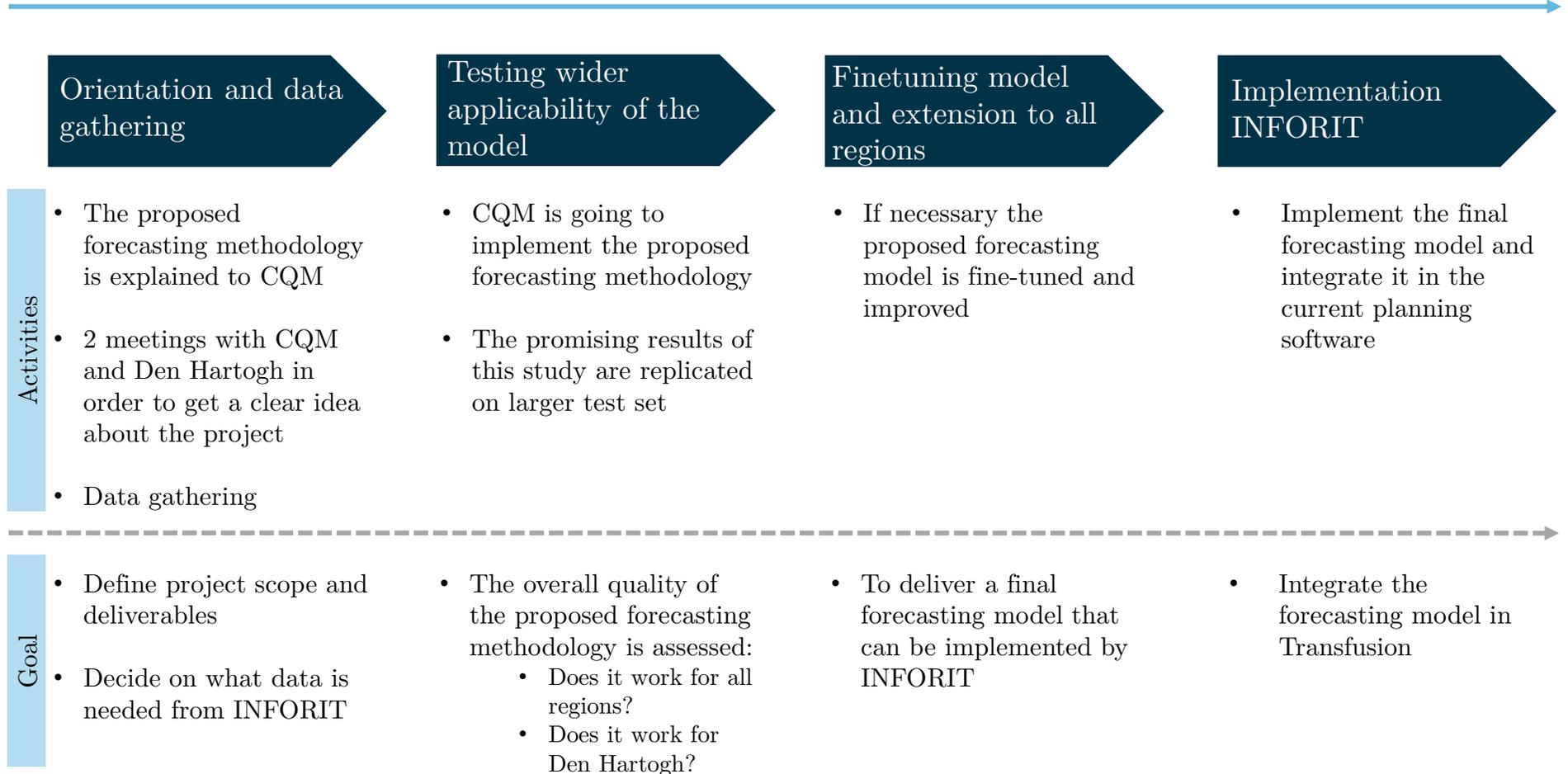


More balanced workload → less trucks per action → savings in trucking cost

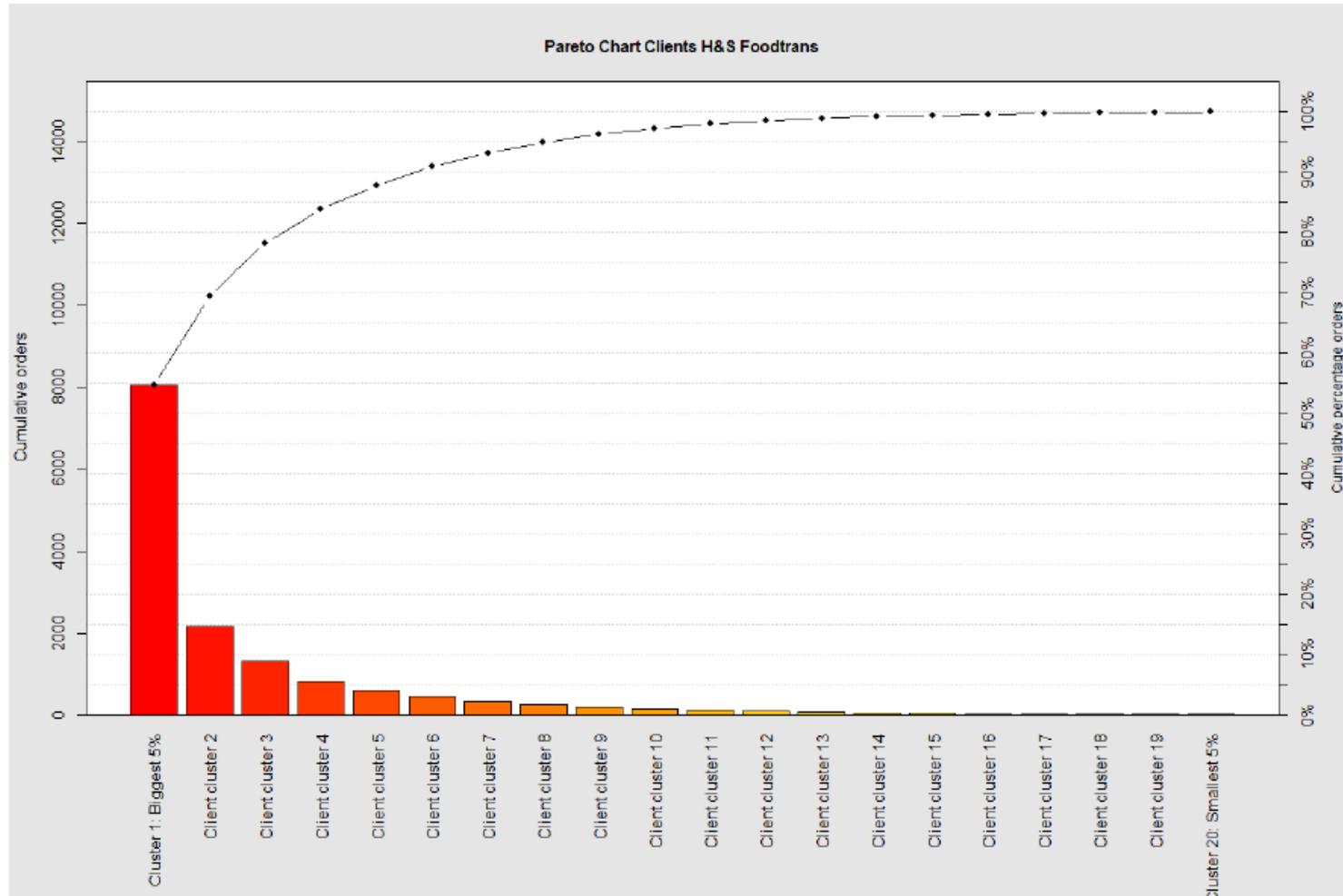
% improvement in balance throughout the day	Savings in number of trucks per action	Number of actions per year	Savings in trucks per year	Total number of trucks used per year	% decrease in number of trucks used per year	Total costs associated with trucking operations	% of trucking costs dependent on number of trucks	Total estimated savings from improvement of balance
1%	0.016	60,000	972	56,000	-2%	€ 27,000,000	30%	€ 140,549
2%	0.032	60,000	1,943	56,000	-3%	€ 27,000,000	30%	€ 281,099
3%	0.049	60,000	2,915	56,000	-5%	€ 27,000,000	30%	€ 421,648
4%	0.065	60,000	3,887	56,000	-7%	€ 27,000,000	30%	€ 562,198
5%	0.081	60,000	4,859	56,000	-9%	€ 27,000,000	30%	€ 702,747
6%	0.097	60,000	5,830	56,000	-10%	€ 27,000,000	30%	€ 843,297
7%	0.113	60,000	6,802	56,000	-12%	€ 27,000,000	30%	€ 983,846
8%	0.130	60,000	7,774	56,000	-14%	€ 27,000,000	30%	€ 1,124,396
9%	0.146	60,000	8,745	56,000	-16%	€ 27,000,000	30%	€ 1,264,945
10%	0.162	60,000	9,717	56,000	-17%	€ 27,000,000	30%	€ 1,405,495

# At this moment, the proposed forecasting methodology proposed by this research is being implemented at H&S

Timeline project



# The 5% largest clients account for 55% of all orders of H&S Foodtrans



# H&S Foodtrans is a logistics service provider engaged in intermodal transportation of liquid foodstuff

*Introduction to H&S*

